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Linear Time Construction of Suffix Arrays

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Abstract
We present a linear time algorithm to sort all the suffixes of a string over a large alphabet of integers. The sorted order of suffixes of a string is also called suffix array, a data structure introduced by Manber and Myers that has numerous applications in computational biology. Though the suffix tree of a string can be constructed in linear time and the sorted order of suffixes derived from it, a direct algorithm for suffix sorting is of great interest due to the space requirements of suffix trees. Our result improves upon the best known direct algorithm for suffix sorting, which takes \(O(n \log n)\) time. We also show how to construct suffix trees in linear time from our suffix sorting result. Apart from being simple and applicable for alphabets not necessarily of fixed size, this method of constructing suffix trees is more space efficient.

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Theory and Algorithms
Linear Time Construction of Suffix Arrays *

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Abstract

We present a linear time algorithm to sort all the suffixes of a string over a large alphabet of integers. The sorted order of suffixes of a string is also called suffix array, a data structure introduced by Manber and Myers that has numerous applications in computational biology. Though the suffix tree of a string can be constructed in linear time and the sorted order of suffixes derived from it, a direct algorithm for suffix sorting is of great interest due to the space requirements of suffix trees. Our result improves upon the best known direct algorithm for suffix sorting, which takes $O(n \log n)$ time. We also show how to construct suffix trees in linear time from our suffix sorting result. Apart from being simple and applicable for alphabets not necessarily of fixed size, this method of constructing suffix trees is more space efficient.

1 Introduction

Suffix trees and suffix arrays are important fundamental data structures useful in many applications in computational biology. The suffix tree of a string is a compacted trie of all the suffixes of the string. The suffix tree of a string of length $n$ over an alphabet $\Sigma$ can be constructed in $O(n \log |\Sigma|)$ time and $O(n)$ space, or in $O(n)$ time and $O(n|\Sigma|)$ space [McC76, Ukk95, Wei73]. These algorithms are suitable for small, fixed size alphabets. Subsequently, Farach [FM96] presented an $O(n)$ time and space algorithm for the more general case of constructing suffix trees over integer alphabets. For numerous applications of suffix trees in computational biology, see [Gus97].

The suffix array of a string is the lexicographically sorted list of all its suffixes. In 1993, Manber and Myers introduced the suffix array data structure [MM93] as a space-efficient substitute for suffix trees. As a lexicographic-order traversal of a suffix tree can be used to produce the sorted list of suffixes, suffix arrays can be constructed in linear time and space using suffix trees. However, this

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defeats the whole purpose if the goal is to avoid suffix trees. Hence, Manber and Myers presented
direct construction algorithms that run in $O(n \log n)$ worst-case time and $O(n)$ expected time,
respectively. Since then, the study of algorithms for constructing suffix arrays and for using suffix
arrays in computational biology applications has attracted considerable attention.

The suffix array is often used in conjunction with another array, called $lcp$ array, containing
the lengths of the longest common prefixes between every pair of consecutive suffixes in sorted
order. Manber and Myers also presented algorithms for constructing $lcp$ array in $O(n \log n)$ worst-
case time and $O(n)$ expected time, respectively [MM93]. More recently, Kasai et al. [KLA+01]
presented a linear time algorithm for constructing the $lcp$ array directly from the suffix array. While
the classic problem of finding a pattern $P$ in a string $T$ of length $n$ can be solved in $O(|P|)$ time
for fixed size $\Sigma$ using a suffix tree of $T$, Manber and Myers’ pattern matching algorithm takes
$O(|P| + \log n)$ time, without any restriction on $\Sigma$. Recently, Abouelhoda et al. [AOK02] have
improved this to $O(|P|)$ time using additional linear time preprocessing, thus making the suffix
array based algorithm superior. In fact, many problems involving top-down or bottom-up traversal
of suffix trees can now be solved with the same asymptotic run-time bounds using suffix arrays
[AKO02, AOK02]. Such problems include many queries used in computational biology applications
including finding exact matches, maximal repeats, tandem repeats, maximal unique matches and
finding all shortest unique substrings. For example, the whole genome alignment tool MUMmer
[DKF+99] uses the computation of maximal unique matches.

While considerable advances are made in designing optimal algorithms for queries using suf-
fix arrays and for computing auxiliary information that is required along with suffix arrays, the
complexity of direct construction algorithms for suffix arrays remained $O(n \log n)$ so far. Several
alternative algorithms for suffix array construction have been developed, each improving the previ-
ous best algorithm by an additional constant factor [LS99, IT99]. We close this gap by presenting
a direct linear time algorithm for constructing suffix arrays over integer alphabets.

It is well known that the suffix tree of a string can be constructed from the sorted order of
its suffixes and the $lcp$ array [FM96]. Because the $lcp$ array can be inferred from the suffix array
in linear time [KLA+01], our algorithm can also be used to construct suffix trees in linear time
for integer alphabets, and of course, for the special case of fixed size alphabets. Our algorithm is
simpler and more space efficient than Farach’s linear time algorithm for constructing suffix trees for
integer alphabets. In fact, it is simpler than linear time suffix tree construction algorithms for fixed
size alphabets [McC76, Ukk95, Wei73]. A noteworthy feature of our algorithm is that it does not
construct or use suffix links, resulting in additional space advantage. To the best of our knowledge,
this is the first suffix tree construction algorithm that achieves linear run-time without exploiting
the use of suffix links.

The remainder of this paper is organized as follows: In Section 2, we present our linear time
suffix sorting algorithm. An implementation strategy that further improves the run-time in practice is presented in Section 3. Section 4 concludes the paper.

2 Suffix Sorting Algorithm

Consider a string $T = t_1t_2 \ldots t_n$ over the alphabet $\Sigma = \{1 \ldots n\}$. Without loss of generality, assume the last character of $T$ occurs nowhere else in $T$, and is the lexicographically smallest character. We denote this character by ‘$’.

Let $T_i = t_it_{i+1} \ldots t_n$ denote the suffix of $T$ starting with $t_i$. To store the suffix $T_i$, we only store the starting position number $i$. For strings $\alpha$ and $\beta$, we use $\alpha \prec \beta$ to denote that $\alpha$ is lexicographically smaller than $\beta$.

We classify the suffixes into two types: Suffix $T_i$ is of type $S$ if $T_i \prec T_{i+1}$, and is of type $L$ if $T_{i+1} \prec T_i$. The last suffix $T_n$ does not have a next suffix, and is classified as both type $S$ and type $L$.

Lemma 2.1 All suffixes of $T$ can be classified as either type $S$ or type $L$ in $O(n)$ time.

Proof Consider a suffix $T_i$ ($i < n$).

Case 1: If $t_i \neq t_{i+1}$, we only need to compare $t_i$ and $t_{i+1}$ to determine if $T_i$ is of type $S$ or type $L$.

Case 2: If $t_i = t_{i+1}$, find the smallest $j > i$ such that $t_j \neq t_i$.

if $t_j > t_i$, then suffixes $T_i, T_{i+1}, \ldots, T_{j-1}$ are of type $S$.

if $t_j < t_i$, then suffixes $T_i, T_{i+1}, \ldots, T_{j-1}$ are of type $L$.

Thus, all suffixes can be classified using a left to right scan of $T$ in $O(n)$ time.

The type of each suffix of the string MISSISSIPPI$ is shown in Figure 1. An important property of type $S$ and type $L$ suffixes is proved below.
Lemma 2.2 In the suffix array of $T$, among all suffixes that start with the same character, the type $S$ suffixes appear after the type $L$ suffixes.

Proof We prove this by contradiction. Suppose a type $S$ suffix $T_i$ and a type $L$ suffix $T_j$ be two suffixes that start with the same character $c$, such that $T_i \prec T_j$. We can write $T_i = c\alpha c_1 \beta$ and $T_j = c\alpha c_2 \gamma$, where $c_1 \neq c_2$ and $\alpha$, $\beta$, and $\gamma$ are (possibly empty) strings.

Case 1: $\alpha$ contains a character other than $c$. Let $c_3$ be the leftmost character in $\alpha$ that is different from $c$. Because $T_i$ is a type $S$ suffix, it follows that $c_3 > c$. Similarly, for $T_j$ to be a type $L$ suffix, $c_3 < c$, a contradiction.

Case 2: $\alpha$ does not contain any character other than $c$. In this case, we have the following:

- $T_i$ of type $S \Rightarrow c_1 \geq c$
- $T_j$ of type $L \Rightarrow c_2 \leq c$
- $c_2 \leq c$ and $c \leq c_1 \Rightarrow c_2 \leq c_1$

But $T_i \prec T_j \Rightarrow c_1 < c_2$, a contradiction. $\blacksquare$

Let $A$ be an array containing all suffixes of $T$, not necessarily in sorted order. Create an array $R$ such that $R[i] = k$ if $A[k] = i$, i.e., $R[i]$ indicates the position where suffix $T_i$ is stored in $A$. We need to keep $R$ up-to-date, thus any change made to $A$ is also reflected in $R$. Let $B$ be an array of all suffixes of type $S$, sorted in lexicographic order. Using $B$, we can compute the lexicographically sorted order of all suffixes of $T$ as follows:

1. Bucket all suffixes of $T$ according to their first character in array $A$. Each bucket consists of all suffixes that start with the same character. This step takes $O(n)$ time.

2. Scan $B$ from right to left. For each suffix encountered in the scan, move the suffix to the current end of its bucket in $A$, and update the current end. This step takes $O(|B|)$ time, which is bounded by $O(n)$. By Lemma 2.2, all type $S$ suffixes are now in their correct positions in $A$.

3. Scan $A$ from left to right. For each entry $A[i]$, if $T_{A[i]-1}$ is a type $L$ suffix, move it to the current front of its bucket in $A$, and advance the front of the bucket by one. This takes $O(n)$ time. At the end of this step, $A$ contains all suffixes of $T$ in sorted order.

The following lemma proves the correctness of the procedure in Step 3.
Lemma 2.3 In step 3, when the scan reaches $A[i]$, then suffix $T_{A[i]}$ is already in its sorted position in $A$.

Proof By induction on $i$. To begin with, the smallest suffix in $T$ must be of type $S$ and hence in its correct position $A[1]$. By inductive hypothesis, assume that $A[1], A[2], \ldots, A[i]$ are the first $i$ suffixes in sorted order. We now show that when the scan reaches $A[i+1]$, then the suffix in it, i.e., $T_{A[i+1]}$ is already in its sorted position. Suppose not. Then there exists a suffix referenced by $A[k] (k > i + 1)$ that should be in $A[i+1]$ in sorted order, i.e., $T_{A[k]} \prec T_{A[i+1]}$. As all type $S$ suffixes are already in correct positions, both $T_{A[k]}$ and $T_{A[i+1]}$ must be of type $L$. Because $A$ is bucketed by the first character of the suffixes prior to step 3, and a suffix is never moved out of its bucket, $T_{A[k]}$ and $T_{A[i+1]}$ must begin with the same character, say $c$. Let $T_{A[i+1]} = c\alpha$ and $T_{A[k]} = c\beta$. Since $T_{A[k]}$ is type $L$, $\beta \prec T_{A[k]}$. From $T_{A[k]} \prec T_{A[i+1]}$, $\beta \prec \alpha$. Since $\beta \prec T_{A[k]}$, and the correct sorted position of $T_{A[k]}$ is $A[i+1]$, $\beta$ must occur in $A[1] \ldots A[i]$. Because $\beta \prec \alpha$, $T_{A[k]}$ should have been moved to the current front of its bucket before $T_{A[i+1]}$. Thus, $T_{A[k]}$ can not occur to the right of $T_{A[i+1]}$, a contradiction.

So far, we showed that if all type $S$ suffixes are sorted, then the sorted position of all suffixes of $T$ can be determined in $O(n)$ time. In a similar manner, the sorted position of all suffixes of $T$ can also be determined from the sorted order of all suffixes of type $L$. To do this, we bucket all suffixes of $T$ based on their first characters into an array $A$. We then scan the sorted order of type $L$ suffixes from left to right and determine their correct positions in $A$ by moving them to the current front of their respective buckets. We then scan $A$ from right to left and when $A[i]$ is encountered, if $T_{A[i-1]}$ is of type $S$, it will be moved to the current end of its bucket.

Once the suffixes of $T$ are classified into type $S$ and type $L$, we choose to sort those type of suffixes which are fewer in number. Without loss of generality, assume that type $S$ suffixes are fewer. We now show how to recursively sort these suffixes.

Define position $i$ of $T$ to be a type $S$ position if the suffix $T_i$ is of type $S$, and similarly to be a type $L$ position if the suffix $T_i$ is of type $L$. The substring $t_i \ldots t_j$ is called a type $S$ substring if both $i$ and $j$ are type $S$ positions, and every position between $i$ and $j$ is a type $L$ position.

Our goal is to sort all the type $S$ suffixes in $T$. To do this we first sort all the type $S$ substrings. The sorting generates buckets where all the substrings in a bucket are identical. The buckets are numbered using consecutive integers starting from 1. We then generate a new string $T'$ as follows: Scan $T$ from left to right and for each type $S$ position in $T$, write the bucket number of the type $S$ substring starting from that position. This string of bucket numbers forms $T'$. Observe that each type $S$ suffix in $T$ naturally corresponds to a suffix in the new string $T'$. In Lemma 2.4, we prove that sorting all type $S$ suffixes of $T$ is equivalent to sorting all suffixes of $T'$. We sort $T'$ recursively.

We first show how to sort all the type $S$ substrings in $O(n)$ time. Consider the array $A$,
Step 1. Record the S-distances

<table>
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<th>M</th>
<th>I</th>
<th>S</th>
<th>S</th>
<th>I</th>
<th>S</th>
<th>S</th>
<th>I</th>
<th>P</th>
<th>P</th>
<th>I</th>
<th>$</th>
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<td>7</td>
<td>8</td>
<td>9</td>
<td>10</td>
<td>11</td>
<td>12</td>
</tr>
</tbody>
</table>

Step 2. Construct S-distance Lists

| 1 | 9 | 3 | 6 |
| 2 | 10 | 4 | 7 |
| 3 | 5 | 8 | 11 |
| 4 | 12 |

Step 3. Sort all type S substrings

Original

| 12 | 2 | 5 | 8 |

Sort according to list 1

| 12 | 8 | 5 | 2 |

Sort according to list 2

| 12 | 8 | 5 | 2 |

Sort according to list 4

| 12 | 8 | 5 | 2 |

Figure 2: Illustration of the sorting of type S substrings of the string MISSISSIPPI$.

consisting of all suffixes of T bucketed according to their first characters. For each suffix $T_i$, define its $S$-distance to be the distance from its starting position $i$ to the nearest type $S$ position to its left (excluding position $i$). If no type $S$ position exists to the left, the $S$-distance is defined to be 0. Thus, for each suffix starting on or before the first type $S$ position in $T$, its $S$-distance is 0. The type $S$ substrings are sorted as follows (illustrated in Figure 2):

1. For each suffix in $A$, determine its $S$-distance. This is done by scanning $T$ from left to right, keeping track of the distance from the current position to the nearest type $S$ position to the left. While at position $i$, the $S$-distance of $T_i$ is known and the position of $T_i$ in $A$ can be found using $R[i]$. Hence, the $S$-distances for all suffixes in $A$ can be recorded in linear time.

2. Let $m$ be the largest $S$-distance. Create $m$ lists such that list $j$ ($1 \leq j \leq m$) contains all the suffixes with an $S$-distance of $j$, listed in the order in which they appear in array $A$. This can be done by a scan of $A$ from left to right in linear time.

3. We now sort the type $S$ substrings using the lists created above. The sorting is done by repeated bucketing using one character at a time. To begin with, the bucketing based on first character is determined by the order in which type $S$ suffixes appear in array $A$. Suppose the type $S$ substrings are bucketed according to their first $j - 1$ characters. To extend this to $j$ characters, we scan list $j$. For each suffix $T_i$ encountered, move the type $S$ substring starting at $t_{i-j}$ to the current front of its bucket. Because the total size of all the lists is $O(n)$, the sorting of type $S$ substrings only takes $O(n)$ time.

The sorting of type $S$ substrings using the above algorithm respects lexicographic ordering of type $S$ substrings, with the following important exception: If a type $S$ substring is the prefix of
another type $S$ substring, the bucket number assigned to the shorter substring will be larger than
the bucket number assigned to the larger substring. This anomaly is designed on purpose, and is
exploited later in Lemma 2.4.

As mentioned before, we now construct a new string $T'$ corresponding to all type $S$ substrings
in $T$. Each type $S$ substring is replaced by its bucket number and $T'$ is the sequence of bucket
numbers in the order in which the type $S$ substrings appear in $T$. Because every type $S$ suffix in $T$
starts with a type $S$ substring, there is a natural one-to-one correspondence between type $S$
suffixes of $T$ and all suffixes of $T'$. Let $T_i$ be a suffix of $T$ and $T'_i$ be its corresponding suffix in $T'$.
Note that $T'_i$ can be obtained from $T_i$ by replacing every type $S$ substring in $T_i$ with its corresponding
bucket number. Similarly, $T_i$ can be obtained from $T'_i$ by replacing each bucket number with the
substring and removing the duplicate instance of the common character shared by
two consecutive type $S$ substrings. This is because the last character of a type $S$ substring is also
the first character of the next type $S$ substring along $T$.

**Lemma 2.4** Let $T_i$ and $T_j$ be two suffixes of $T$ and let $T'_i$ and $T'_j$ be the corresponding suffixes of
$T'$. Then, $T_i < T_j$ $\iff$ $T'_i < T'_j$.

**Proof** We first show that $T'_i < T'_j$ $\Rightarrow$ $T_i < T_j$. The prefixes of $T_i$ and $T_j$
corresponding to the longest common prefix of $T'_i$ and $T'_j$ must be identical. This is because if two bucket numbers
are the same, then the corresponding substrings must be the same. Consider the leftmost position
in which $T'_i$ and $T'_j$ differ. Such a position exists and the characters (bucket numbers) of $T'_i$ and $T'_j$
in that position determine which of $T'_i$ and $T'_j$ is lexicographically smaller. Let $k$ be the
bucket number in $T'_i$ and $l$ be the bucket number in $T'_j$ at that position. Let $\alpha$ be the substring
corresponding to $k$ and $\beta$ be the substring corresponding to $l$. Note that $\alpha$ and $\beta$ can be of different
lengths. Without loss of generality, assume $|\alpha| \leq |\beta|$.

Case 1: $\alpha$ is not a prefix of $\beta$. In this case, the relative order of $k$ and $l$ determines the lexicographic
order of $\alpha$ and $\beta$, which is the same as the lexicographic order of $T_i$ and $T_j$.

Case 2: $\alpha$ is a prefix of $\beta$. Let the last character of $\alpha$ be $c$. The corresponding position in $T$ is a
type $S$ position. The position of the corresponding $c$ in $\beta$ must be a type $L$ position.

Since the two suffixes that begin at these positions start with the same character, by Lemma
2.2, the type $L$ suffix must be lexicographically smaller then the type $S$ suffix. Thus, $T_j < T_i$.

Because of the way type $S$ substrings are sorted, $l < k$. Thus the relative order of the bucket
numbers correctly determines the relative order the original suffixes in this case as well.

From the one-to-one correspondence between the suffixes of $T'$ and the type $S$ suffixes of $T$, it also
follows that $T_i < T_j$ $\Rightarrow$ $T'_i < T'_j$. $\blacksquare$
Corollary 2.5 The sorted order of the suffixes of $T'$ determines the sorted order of the type $S$ suffixes of $T$.

Proof Let $T'_{i_1}', T'_{i_2}', T'_{i_3}'$ be the sorted order of suffixes of $T'$. Let $T_{i_1}, T_{i_2}, T_{i_3}, \ldots$ be the sequence obtained by replacing each suffix $T'_{i_k}'$ with the corresponding type $S$ suffix $T_{i_k}$. Then, $T_{i_1}, T_{i_2}, T_{i_3}, \ldots$ is the sorted order of type $S$ suffixes of $T$. The proof follows directly from Lemma 2.4.

Hence, the problem of sorting the type $S$ suffixes of $T$ reduces to the problem of sorting all suffixes of $T'$. Note that the characters of $T'$ are consecutive integers starting from 1. Hence our suffix sorting algorithm can be recursively applied to $T'$.

If the string $T$ has fewer type $L$ suffixes than type $S$ suffixes, the type $L$ suffixes are sorted using a similar procedure — Call the substring $t_i, \ldots, t_j$ a type $L$ substring if both $i$ and $j$ are type $L$ positions, and every position between $i$ and $j$ is a type $S$ position. Now sort all the type $L$ substrings and construct the corresponding string $T'$ obtained by replacing each type $L$ substring with its bucket number. Sorting $T'$ gives the sorted order of type $L$ suffixes.

Thus, the problem of sorting the suffixes of a string $T$ of length $n$ can be reduced to the problem of sorting the suffixes of a string $T'$ of size at most $\lceil \frac{n}{2} \rceil$, and $O(n)$ additional work. This leads to the recurrence

$$T(n) = T \left( \left\lceil \frac{n}{2} \right\rceil \right) + O(n)$$

Theorem 2.6 The suffixes of a string of length $n$ can be lexicographically sorted in $O(n)$ time and space.

3 Reducing the Size of $T'$

In this section, we present an implementation strategy to further reduce the size of $T'$. Consider the result of sorting all type $S$ substrings of $T$. Note that a type $S$ substring is a prefix of the corresponding type $S$ suffix. Thus, sorting type $S$ substrings is equivalent to bucketing type $S$ suffixes based on their respective type $S$ substring prefixes. The bucketing conforms to the lexicographical ordering of type $S$ suffixes. The purpose of forming $T'$ and sorting its suffixes is to determine the sorted order of type $S$ suffixes that fall into the same bucket. If a bucket contains only one type $S$ substring, the position of the corresponding type $S$ suffix in the sorted order is already known.

Let $T' = b_1b_2\ldots b_m$. Consider a maximal substring $b_i \ldots b_j$ such that each $b_k$ ($i \leq k \leq j$) contains only one type $S$ substring. We can shorten $T'$ by replacing each such maximal substring
$b_i \ldots b_j$ with its first character $b_i$. It is easy to directly compute the shortened version of $T'$, instead of first computing $T'$ and then shortening it. Shortening $T'$ will have the effect of eliminating some of the suffixes of $T'$, and also modifying each suffix that contains a substring that is shortened. We already noted that the final positions of the eliminated suffixes are already known. It remains to be shown that the sorted order of other suffixes is not affected by the shortening.

Consider any two suffixes $T'_k = b_k \ldots b_m$ and $T'_l = b_l \ldots b_m$, such that at least one of the suffixes contains a substring that is shortened. Let $j \geq 0$ be the smallest integer such that either $b_{k+j}$ or $b_{l+j}$ (or both) is the beginning of a shortened substring. The first character of a shortened substring corresponds to a bucket containing only one type $S$ substring. Hence, the bucket number occurs nowhere else in $T'$. Therefore $b_{k+j} \neq b_{l+j}$, and the sorted order of $b_k \ldots b_m$ and $b_l \ldots b_m$ is determined by the sorted order of $b_k \ldots b_{k+j}$ and $b_l \ldots b_{l+j}$. In other words, the comparison of any two suffixes never extends beyond the first character of a shortened substring.

4 Conclusions

In this paper we present a linear time algorithm for sorting the suffixes of a string over integer alphabet, or equivalently, for constructing the suffix array of the string. Our algorithm can also be used to construct suffix trees in linear time. Apart from being the first direct algorithm for constructing suffix arrays in linear time, the simplicity and space advantages of our algorithm are likely to make it useful in suffix tree construction as well.

References


