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Upper critical field of KFe₂As₂ under pressure: A test for the change in the superconducting gap structure

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Received 2 April 2014; revised manuscript received 4 June 2014; published 25 June 2014

We report measurements of electrical resistivity under pressure to 5.8 GPa, magnetization to 6.7 GPa, and ac susceptibility to 7.1 GPa in KFe₂As₂. The previously reported change of slope in the pressure dependence of the superconducting transition temperature $T_c(p)$ at a pressure $p^* \sim 1.8$ GPa is confirmed, and $T_c(p)$ is found to be nearly constant above $p^*$ up to 7.1 GPa. The $T_c$-$p$ phase diagram is very sensitive to the pressure conditions as a consequence of the anisotropic uniaxial pressure dependence of $T_c$. Across $p^*$, a change in the behavior of the upper critical field is revealed through a scaling analysis of the slope of $H_c^*$ with the effective mass as determined from the $A$ coefficient of the $T^2$ term of the temperature-dependent resistivity. We show that this scaling provides a quantitative test for the changes of the superconducting gap structure and suggests the development of a $k_z$ modulation of the superconducting gap above $p^*$ as a most likely explanation.

DOI: 10.1103/PhysRevB.89.220509

Since the discovery of superconductivity in LaFe₄₃(Ο₁₋ₓFₓ) [1], the iron-based superconductors have been the focus of numerous experimental and theoretical studies. Taking advantage of the lessons learned from the cuprate high-temperature superconductors, the investigation of the symmetry of the superconducting state has been given priority [2]. However, unlike the cuprates, the gap function of the iron-based superconductors is not universal and several gap symmetries have been proposed both experimentally and theoretically [3]. The stoichiometric compound KFe₂As₂, which has a superconducting transition temperature $T_c \approx 3.5$ K, is one of the cleanest examples where different gap structures appear likely [4–15]. Recently, it has been suggested that a change of pairing symmetry from $d$ wave to $s$ wave occurs upon applying pressure to KFe₂As₂ [9]. The argument was based on the experimental observation of a change in the pressure dependence of $T_c$ from negative to positive at $p^* \approx 1.8$ GPa. Following this study, ac magnetic susceptibility and de Haas–van Alphen (dHvA) oscillations under pressure confirmed the change of slope in $T_c(p)$ at $p^*$ and supported the earlier inference that this change is not due to drastic modifications of the Fermi surface [16]. A similar change of slope of $T_c(p)$ was also observed in CsFe₂As₂ [17]. Although there have been theoretical predictions that the $d$-wave and $s$-wave states are very close in energy [14,18,19], the experimental data available so far do not provide information about the changes in the superconducting gap function at $p^*$.

In this study we significantly extend the pressure range of previous studies (~2.5 GPa [9,16]) to 7.1 GPa. We confirm the observation of a change of slope in $T_c(p)$ but find that the phase diagram is very sensitive to the hydrostaticity of the pressure medium in this high-pressure range. In addition, we report on the temperature dependence of the upper critical field $H_c^*$ with the magnetic field applied along the $c$ axis under pressure. By scaling $(-dH_c^*/dT)_{T_c}/H_c^*$ versus the $A$ coefficient of the $T^2$ term of the resistivity, we find a change at $p^*$ which allows for a quantitative test of the modification of the superconducting gap structure. The present data are not able to test whether a change in symmetry between $d$ wave and $s$ wave actually takes place at 1.8 GPa. We find, however, that such a change alone would not be sufficient to account for our results. We suggest that a $k_z$ modulation of the superconducting gap is involved in the slope change at $p^*$.

The Fermi surface of KFe₂As₂ has been investigated experimentally by dHvA oscillation [16,20] and angle-resolved photoemission spectroscopy (ARPES) [4,21,22] experiments. The Fermi surface consists of three hole cylinders at the $\Gamma$ point [$\alpha$ (inner), $\zeta$ (middle), and $\beta$ (outer) bands], and four small hole cylinders near the $X$ point ($\epsilon$ band). ARPES experiments down to 2 K indicate that the gap is nodeless on the $\alpha$ and $\beta$ bands, and nodal with octet line nodes on the $\zeta$ (middle) band [4]. The nodes have also been detected by thermal conductivity [5,6], penetration depth [7], and nuclear quadrupole resonance [8]. The question of whether those nodes are accidental with an $s$-wave state [4] or imposed by symmetry in a $d$-wave state [6,9] is still under debate [10]. Other possibilities include a time-reversal symmetry breaking $s+i\sigma$ state [11–14], or an $s+is$ state between two kinds of $\pm \pm$ states which has been proposed upon Ba doping in Ba₁₋ₓKₓFe₂As₂ [15] in the vicinity of $\chi \sim 0.7$ where deviations in the jump in specific heat have been observed [23,24]. In this context, the evidence for a change of gap function under pressure in KFe₂As₂ illustrates the near degeneracy of these states and the possibility of studying the interplay between different superconducting states. Our results suggest that, in addition to the considered possible in-plane symmetry of the gap functions, a $k_z$ modulation of the superconducting gap is involved in the slope change at $p^*$. 

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In this study, several high-quality single crystals of KFe$_2$As$_2$ were grown from KAs flux as detailed in Ref. [25]. For the electrical resistivity measurements, pressure was applied at room temperature using a modified Bridgman cell [26] with a 1:1 mixture of n-pentane:isopentane as a pressure medium. The ac susceptibility measurements to hydrostatic pressures as high as 7 GPa were carried out in a membrane-loaded diamond-anvil cell [27]. Helium was used as pressure medium. To promote hydrostaticity, pressure was increased at temperatures well above the melting curve of helium, unless stated otherwise. Further experimental details are given in the Supplemental Material [28] (see also Refs. [9,16,26,27,29–49]) together with other measurements using less hydrostatic pressure media.

The superconducting phase diagram obtained from ac susceptibility and resistivity measurements is shown in Fig. 1. The previously reported change of slope in $T_c(p)$ at $p^* \approx 1.8$ GPa [9,16] is confirmed. $T_c$ increases very slowly above $p^*$ up to 7.1 GPa. A remarkable property of this phase diagram is its strong sensitivity on the pressure conditions. As shown by the open symbols in Fig. 1, $T_c$ is increased when the pressure is applied on solid helium by comparison with liquid helium. As expected, the effect is even more dramatic with less hydrostatic media. When using a 1:1 mixture of Fluorinert FC70:FC77, $T_c$ is only slowly reduced with pressure and $T_c \approx 3.19$ K at our pressure limit of 5.8 GPa [28]. In our dc magnetization measurements using Daphne 7474, a second superconducting dome is even obtained with a maximum $T_c$ as high as 3.8 K at 5.5 GPa, which is above the room temperature solidification point of this medium [28].

Such a large sensitivity to the hydrostaticity is most likely a consequence of the anisotropic uniaxial pressure dependence of $T_c$. In KFe$_2$As$_2$, $\partial T_c/\partial p_{a\perp} \approx -1.9$ K GPa$^{-1}$ along the $a$ axis, whereas $\partial T_c/\partial p_{c\perp} \approx +2.1$ K GPa$^{-1}$ along the $c$ axis [49]. Under hydrostatic conditions, the three axes will contribute equally to give rise to the phase diagram presented in Fig. 1. However, under nonhydrostatic conditions, as already explained in Refs. [32,42], the pressure will be larger along the $c$ axis and smaller in the $ab$ plane. This results in larger values of $T_c$ and a modification of the superconducting phase diagram [28]. Not only do we confirm the kink in $T_c(p)$ previously reported [9,16], but we observe that $T_c$ remains roughly constant up to 7.1 GPa. A Lifshitz transition can produce such a kink in $T_c(p)$. In that case, the observed increase of $T_c$ just above $p^*$ is consistent with the formation of a new Fermi-surface pocket [50]. However, no anomaly was observed in the Hall coefficient to support this mechanism [9], and dHvA oscillations indicate no drastic change in the Fermi surface up to $\sim 2.5$ GPa [16].

We note that the change in slope at the characteristic pressure of 1.8 GPa could be a simple consequence of the fact that the uniaxial pressure dependences of $T_c$ are of opposite sign and large. At ambient pressure, $\partial T_c/\partial p_{a\perp} \approx -1.9$ K GPa$^{-1}$ and $\partial T_c/\partial p_{c\perp} \approx +2.1$ K GPa$^{-1}$ in Ref. [49] or $\partial T_c/\partial p_{\perp} \approx +1.1$ K GPa$^{-1}$ in Ref. [42]. These partial derivatives cancel each other to a considerable degree, yielding a hydrostatic pressure derivative that is negative. Any nonlinearity in $T_c(p)$ or $T_c(p^*)$ would generate a much larger relative nonlinearity in the dependence of $T_c$ on hydrostatic pressure $T_c(p)$. For example, were the magnitude of $\partial T_c/\partial p_{\perp}$ to gradually decrease by a factor of $\sim 3$ under 3 GPa hydrostatic pressure, $\partial T_c/\partial p_{\perp}$ remaining constant, the hydrostatic pressure dependence $T_c(p)$ would be forced to pass through a minimum. We also note that, even though the modulus of elasticity is almost identical along the $a$ and $c$ axis, the first derivative of the modulus is over an order of magnitude smaller along the $c$ axis [17]. This implies a larger compression along the $a$ axis, so that the effect of pressure on $T_c$ may become dominated by the $p_{c\perp}$ component. In such a scenario, a theoretical explanation of the uniaxial pressure dependencies of $T_c$ would be the key to understanding the slope change at $p^*$.

Another possibility that may even induce the previous idea is a transition to a superconducting phase of a different symmetry. In such a case, changes in other thermodynamic quantities, such as the thermal expansion or the specific heat, are also expected. However, the combination of high pressures and low temperatures makes the experimental investigations of these quantities challenging. Figure 2 shows the temperature dependence of $H_c2$ for the magnetic field applied along the $c$ axis at different pressures. At ambient pressure, the upper critical field along the $c$ axis is known to be due to the orbital limit with negligible effect due to the Pauli limit [49,52]. With increasing pressure, as $T_c$ decreases, $H_c2$ is also decreasing. Interestingly, above $p^*$ where $T_c$ remains roughly constant or increases very slowly, $H_c2$ decreases to continue (see inset of Fig. 2). In the following, we will relate this decrease with a commensurate decrease of the electrons’ effective mass.

Figure 3 shows the low-temperature dependence of the resistivity as a function of $T^2$ at various pressures (full lines). For each pressure, we performed fits with a Fermi liquid behavior $\rho = \rho_0 + AT^2$ up to 8 K (dashed lines). The pressure dependence of the $A$ coefficient is shown in the inset. At ambient pressure, $A \approx 0.02 \mu\Omega$ cm K$^{-2}$, in agreement with previous reports [5,52–54]. Under pressure, $A$ decreases smoothly, which is consistent with the decreasing trend in effective mass observed in dHvA oscillations [16].
In Ref. [55], the Helfand-Werthamer theory is examined for the case of uniaxial anisotropy with an anisotropic superconducting gap. For \( H || c \) (one-band case, clean limit):

\[
\frac{1}{T_c} \left( -\frac{d\mu_0 H_{c2}^{orb}}{dT} \right) = \frac{8}{7\xi(3)(\Omega^2\mu_c)} \frac{\phi_0 2\pi k_R^2}{\hbar^2 v_0^2}. \tag{1}
\]

The function \( \Omega(k_F) \) which determines the \( k_F \) dependence of the superconducting gap \( \Delta = \Psi(r, T)\Omega(k_F) \) is normalized so that \( \langle \Omega^2 \rangle = 1 \). The averages over the Fermi surface are shown as \( \langle \cdots \rangle \).

\[
\mu_c = \langle v_s^2 + v_i^2 \rangle / v_0^2 \quad \text{and} \quad v_0^3 = \frac{2E_F^2}{\pi^2\hbar^3 N(0)}.
\]

where \( N(0) \) is the total DOS at the Fermi level \( E_F \) per spin. Assuming that the \( A \) coefficient of the \( T^2 \) term of the resistivity, when resistivity is measured along \( x \), obeys \( A \propto n/(v_i^2) \), the \( A \) coefficient in the tetragonal case will reflect the dependence on \( 1/(v_i^2(\mu_c)) \):

\[
\frac{1}{T_c} \left( -\frac{d\mu_0 H_{c2}^{orb}}{dT} \right) \propto \langle \mu_c \rangle \frac{A}{\langle \Omega^2 \mu_c \rangle n}. \tag{2}
\]

where the carrier density \( n \) can be estimated from Hall measurements. A more detailed expression for \( A \) can be found in various publications \([56,57]\) and would lead to a more complicated expression than that given in Eq. (2). A refinement to the case of several bands would certainly be of interest. In the present form, Eq. (2) shows a proportionality between the slope of \( H_{c2} \) at \( T_c \) and the \( A \) coefficient. This result is known for heavy fermions, both quantities being proportional to the square of the effective mass \([58,59]\).

Figure 4 shows the plot of \( -d\mu_0 H_{c2}^{orb}/dT|_{T_c} \) versus \( A \). All measured points fall onto two straight lines of different slope corresponding to \( p < p^* \) and \( p > p^* \). It is remarkable that both lines go through the origin as expected from the proportionality relation in Eq. (2). Equation (2) indicates that a change of slope when plotting \( -d\mu_0 H_{c2}^{orb}/dT|_{T_c} \) versus \( A \) implies a change in either \( n \), \( \Omega \), or \( \mu_c \). In KFe\(_2\)As\(_2\), the carrier density does not change significantly with pressure as inferred from Hall resistivity measurements \([9]\) and from the smooth pressure variation of the \( A \) coefficient. Therefore, the observed change of slope is more likely due to a change in \( \langle \Omega^2 \mu_c \rangle \). We note that a change of the superconducting gap symmetry is not the only possible explanation, since a change of the Fermi surface will also modify the value of \( \langle \Omega^2 \mu_c \rangle \). However, dHvA oscillations experiments indicate that the global structure of the Fermi surface hardly changes up to \( p \sim 2.5 \) GPa. We mention that \( \langle \mu_c \rangle /\langle \Omega^2 \mu_c \rangle = 1 \) for any \( \Omega \) that does not depend on \( k_z \). Therefore, a simple change between \( s \) wave and \( d \) wave would...
not be able to explain the change of slope of nearly a factor of two observed in Fig. 4.

On the other hand, the appearance of a $k_z$ modulation of the superconducting gap at $P^*$ can explain an increase of nearly a factor two in $\langle \mu \rangle / (\Omega^2 \mu_0)$. Let us assume a superconducting gap with a modulation along $k_z$ \cite{55,60,61}:

$$\Delta = \Delta_0 [1 + \eta \cos(k_c c^*)], \quad (3)$$

where $c^* = h v_0 / (2 E_F)$ is the length scale \cite{55}. Let us also assume a prolate ellipsoidal Fermi surface ($\epsilon = 0.1$ in the notations of Ref. \cite{55}). We find that $\langle \mu \rangle / (\Omega^2 \mu_0)$ changes from 1 to $\sim 1.9$ if $\eta$ changes from 0 to $-0.8$. Therefore, if we assume that the Fermi surface does not change at $P^*$, the appearance of a $k_z$ modulation of the superconducting gap at $P^*$ can be a possible explanation of our experimental observations. A $k_z$ dependence of the superconducting gap has been observed by ARPES in Ba$_{0.6}$K$_{0.4}$Fe$_2$As$_2$ \cite{61}, in agreement with a theoretical prediction for the pairing strength \cite{62}. The pairing between the layers is predominantly responsible for the gap dispersion with $k_z$. In contrast, in Ba$_{0.6}$K$_{0.4}$Fe$_2$As$_2$, the superconducting gap size on all the $\Gamma$-centered hole Fermi surfaces does not vary much along $k_z$ \cite{63}. This is consistent with the near two-dimensionality of KFe$_2$As$_2$ by comparison with the other members of the 122 family \cite{22,64–67}. It is possible that, by applying pressure on KFe$_2$As$_2$, the pairing between the layers induces a $k_z$ modulation of the superconducting gap. This is also consistent with dHvA oscillations measurements showing that three-dimensionality increases with pressure \cite{16}.

In conclusion we have shown that there is very likely a change in the $k_z$ modulation of the SC gap at $P^* \sim 1.8$ GPa. We base this conclusion on a change in the scaling of $(-d \mu_0 H_{c2}/dT |_{T_c})/T_c$ with the $A$ coefficient of the $T^2$ term of the resistivity. We have shown that this indicates either a change of the Fermi surface, of the carrier density, and/or of the superconducting gap symmetry. In addition, we significantly extended the pressure temperature phase diagram from $\sim 2.5$ to 7.1 GPa. For $P > 2.5$ GPa we found that $T_c$ increases only slightly up to 7.1 GPa. By using various pressure cells and several different pressure-transmitting media, we have demonstrated the extreme sensitivity of KFe$_2$As$_2$ to nonhydrostaticity \cite{28} and propose that it is due to the anisotropic dependence of $T_c$ on strain.

We would like to thank A. Jesche, L. Howald, D. Finnemore, T. Kong, and F. F. Tafti for useful discussions. This work was carried out at the Iowa State University and supported by AFSOR-MURI Grant No. FA9550-09-1-0603. Part of this work was performed at the Ames Laboratory, US DOE, under Contract No. DE-AC02-07CH11358. The ac susceptibility measurements in a diamond anvil cell were carried out at Washington University in St. Louis and supported by the National Science Foundation (NSF) through Grant No. DMR-1104742 and by the Carnegie/DOE Alliance Center (CDAC) through NNSA/DOE Grant No. DE-FC52-08NA28554.
