

1-10-2008

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17O and 51V NMR for the zigzag spin-1 chain compound CaV2O4

Abstract

51V NMR studies on CaV₂O₄ single crystals and 17O NMR studies on 17O-enriched powder samples are reported. The temperature dependences of the 17O NMR linewidth and nuclear spin-lattice relaxation rate give strong evidence for a long-range antiferromagnetic transition at $T_N=78$ K in the powder. Magnetic susceptibility measurements show that $T_N=69$ K in the crystals. A zero-field 51V NMR signal was observed at low temperatures ($f \approx 237$ MHz at 4.2 K) in the crystals. The field-swept spectra with the field in different directions suggest the presence of two antiferromagnetic substructures. Each substructure is collinear, with the easy axes of the two substructures separated by an angle of $19(1)^\circ$, and with their average direction pointing approximately along the b axis of the crystal structure. The two spin substructures contain equal numbers of spins. The temperature dependence of the ordered moment, measured up to 45 K, shows the presence of an energy gap E_G in the antiferromagnetic spin wave excitation spectrum. Antiferromagnetic spin wave theory suggests that E_G/k_B lies between 64 and 98 K.

Keywords

Physics and Astronomy, Materials Science and Engineering

Disciplines

Condensed Matter Physics | Metallurgy

Comments

This article is from *Physical Review B* 77 (2008): 014412, doi:[10.1103/PhysRevB.77.014412](https://doi.org/10.1103/PhysRevB.77.014412).

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(Received 14 September 2007; published 10 January 2008)

^{51}V NMR studies on CaV_2O_4 single crystals and ^{17}O NMR studies on ^{17}O -enriched powder samples are reported. The temperature dependences of the ^{17}O NMR linewidth and nuclear spin-lattice relaxation rate give strong evidence for a long-range antiferromagnetic transition at $T_N=78$ K in the powder. Magnetic susceptibility measurements show that $T_N=69$ K in the crystals. A zero-field ^{51}V NMR signal was observed at low temperatures ($f\approx 237$ MHz at 4.2 K) in the crystals. The field-swept spectra with the field in different directions suggest the presence of two antiferromagnetic substructures. Each substructure is collinear, with the easy axes of the two substructures separated by an angle of $19(1)^\circ$, and with their average direction pointing approximately along the b axis of the crystal structure. The two spin substructures contain equal numbers of spins. The temperature dependence of the ordered moment, measured up to 45 K, shows the presence of an energy gap E_G in the antiferromagnetic spin wave excitation spectrum. Antiferromagnetic spin wave theory suggests that E_G/k_B lies between 64 and 98 K.

DOI: 10.1103/PhysRevB.77.014412

PACS number(s): 76.60.-k, 75.50.Ee, 75.25.+z, 75.10.Pq

I. INTRODUCTION

Frustrated magnetic systems have attracted a lot of research interest because such systems often exhibit interesting low temperature properties.¹ The zigzag spin chain with antiferromagnetic interactions between nearest and next-nearest neighbors is about the most simple frustrated system. In a zigzag spin chain system with spin $S=1$, the ground state phase diagram (at temperature $T=0$) as a function of XXZ anisotropy and ratio between nearest-neighbor (NN) and next-nearest-neighbor (NNN) interactions exhibits six different phases.^{2,3} In addition to two Néel ordered phases and two phases with a Haldane gap, there exists a large phase region called a gapless chiral phase where the chirality exhibits long-range order without accompanying spin order, and a small phase region where there is a gapped chiral phase.

CaV_2O_4 is a possible candidate for a zigzag spin $S=1$ chain system.^{4,5} It has an orthorhombic crystal structure (space group $Pnam$) at room temperature as shown in Fig. 1. Vanadium moments at two crystallographically inequivalent sites respectively form two inequivalent zigzag spin chains along the c axis. In one of the two chains, the distances between NN and NNN vanadium atoms are 3.01 and 3.08 Å, respectively, while in the other chain, these two distances are 3.01 and 3.06 Å, respectively. The smallest interchain vanadium distances are 3.58 and 3.62 Å.⁶ Thus, one might expect a much smaller interchain coupling as compared to NN and NNN interactions within the chain.

Previous magnetization and ^{51}V NMR studies of CaV_2O_4 suggested that the ground state of the system might be a gapless chiral phase.^{4,5} However, this finding contradicts earlier powder neutron diffraction studies which showed that the system is in an antiferromagnetic state at 4.2 K.⁷ The neutron measurements indicated a magnetic unit cell in which the b and c lattice constants are doubled and the spin directions in each chemical unit cell are reversed relative to their orientations in neighboring chemical unit cells along the b and c

axes. Each chemical unit cell contains eight vanadium spins and the magnetic spin structure within each chemical unit cell could not be uniquely determined. The neutron diffraction pattern was found to be consistent with three different collinear models with spins parallel to the b axis. By assuming the same spin moment at all vanadium sites, the magnetic moment of each vanadium spin was determined to be $1.06(6)\mu_B$, only about half the value expected for a vanadium spin with g -factor $g\approx 2$ and $S=1$.⁷ The presence of a low temperature antiferromagnetic phase is also supported by recent magnetization measurements on annealed CaV_2O_4 single crystals, which showed a clear signature of an antiferromagnetic phase transition at temperature $T_N=69$ K.⁶

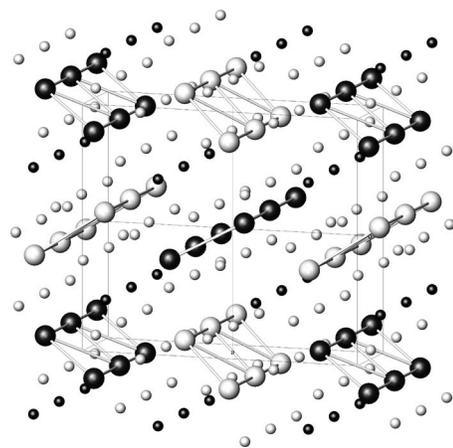


FIG. 1. The orthorhombic crystal structure of CaV_2O_4 at room temperature. Large spheres, two inequivalent V sites; small dark spheres, Ca; and small light spheres, O. The crystallographic a and b axes are along the vertical and horizontal directions in the plane of the page, respectively. The c axis is perpendicular to the page. The cuboid denotes the size of a unit cell.

In order to obtain further evidence of the magnetic phase transition and to study the magnetic properties in the ordered state, we performed ^{17}O and ^{51}V NMR studies on ^{17}O -enriched powder and single crystal samples, respectively. The ^{17}O NMR spectrum and the nuclear spin-lattice relaxation rate measurements give strong evidence for a magnetic transition at $T_N=78$ K in the powder sample. In contrast to early ^{51}V NMR measurements,^{4,5} we could not detect a ^{51}V NMR signal in the powder sample around the normal Larmor frequency in an applied field of 1.67 T in the temperature range of $4.2\text{ K} < T < 296\text{ K}$. Instead, we observed a *zero-field* ^{51}V NMR signal at $T < 45\text{ K}$ ($f \approx 237\text{ MHz}$ at 4.2 K).

The zero-field ^{51}V NMR signal is observed because of a strong local field at ^{51}V nuclear sites ($H_{\text{loc}}=21.2\text{ T}$ at 4.2 K) in the ordered state. The local field arises mainly from interaction between nuclei and vanadium core electrons, which are polarized by the ordered $3d$ electronic spins.^{9,10} This local field points antiparallel to the direction of the local electronic spin moment. By studying how the resonance frequency changes as a function of the direction and magnitude of the applied magnetic field, one can obtain information on the vanadium spin structure, as will be demonstrated below. We measured the temperature dependence of the ordered moment to study the anisotropy gap of the antiferromagnetic spin wave excitations. We also attempted to measure the temperature dependence of the ^{51}V nuclear spin-lattice relaxation rate $1/T_1$. However, due to the very broad line and the presence of nuclear quadrupole splitting (the nuclear spin of ^{51}V is $I=7/2$), the relaxation curves are highly nonexponential and depend strongly on the saturation condition. Thus, a reliable measurement of the ^{51}V $1/T_1(T)$ was not achieved.

The remainder of the paper is organized as follows. Experimental details are explained in Sec. II. ^{17}O and ^{51}V NMR results are presented in Secs. III and IV, respectively. In Sec. V, we give a summary of the main results of the paper.

II. EXPERIMENTAL DETAILS

Polycrystalline single phase CaV_2O_4 (sample an-2-116) was synthesized via the solid-state route by reacting V_2O_3 (99.995%, MV Labs) with CaO obtained by calcining CaCO_3 (99.995%, Aithaca Chemicals) at $1100\text{ }^\circ\text{C}$. The chemicals were ground inside a He glovebox, then pressed and sintered at $1200\text{ }^\circ\text{C}$ for 96 h in flowing 4.5% H_2 -He with intermediate grindings. Phase purity was confirmed by powder x-ray diffraction (XRD) on a Rigaku Geigeflex diffractometer using $\text{Cu } K\alpha$ radiation in the 2θ range of 10° – 90° .⁶ ^{17}O -enriched oxygen (MSD Isotopes) of 72.1 at. % was used for ^{17}O enrichment. About 1 g of the precursor CaV_2O_4 was placed in a Pt foil-lined alumina boat in an evacuated furnace tube, which was then preheated to $750\text{ }^\circ\text{C}$ under dynamic vacuum. The pumping line was then closed and the tube backfilled with the ^{17}O -enriched O_2 . The mass gain on oxidation indicated a nominal composition of $\text{CaV}_2\text{O}_{5.94}$. This was placed in flowing 4.5% H_2 -He and reduced as before to CaV_2O_4 (sample an-2-180E). The final ^{17}O content of the enriched CaV_2O_4 was about 25%. Powder XRD was used to confirm that the sample was single phase.

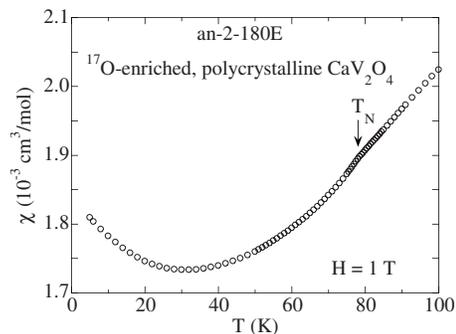


FIG. 2. Magnetic susceptibility χ versus temperature T of the ^{17}O -enriched CaV_2O_4 powder sample measured in a field of $H = 1\text{ T}$. The vertical arrow indicates the position of the antiferromagnetic transition temperature $T_N=78\text{ K}$.

^{17}O NMR measurements were performed utilizing a phase-coherent pulse spectrometer in applied fields of 3.0 and 4.7 T. The typical $\pi/2$ pulse length is $6\text{ }\mu\text{s}$. The echo signal was produced by a sequence of a $\pi/2$ and a $\pi/3$ pulse, which produces the maximum echo signal intensity. The separation between these two echo-generating pulses was $40\text{ }\mu\text{s}$. The ^{17}O NMR spectra were measured by either Fourier transform of half the echo signal or by plotting the area of the echo as a function of the rf (frequency sweep). The nuclear spin-lattice relaxation rates were measured by monitoring the recovery of the echo intensity following a comb sequence of $\pi/2$ saturation pulses. Static magnetization versus temperature was measured in a Quantum Design superconducting quantum interference device magnetometer in a field of 1 T and in the temperature range of 5–100 K to confirm the low temperature magnetic behavior and the ordering temperature $T_N=78\text{ K}$. The magnetic susceptibility of the powdered ^{17}O -enriched sample is shown in Fig. 2. The transition temperature is revealed by a small kink in the $\chi(T)$ data at T_N .

Two CaV_2O_4 crystals were used in ^{51}V NMR measurements. Crystal 1 was grown in an optical floating zone furnace, while crystal 2 was grown using a tri-arc crystal pulling method.^{6,11} The sizes of crystals 1 and 2 are about $5 \times 5 \times 10$ and $1 \times 1 \times 2\text{ mm}^3$, respectively. Both crystals were annealed at $1200\text{ }^\circ\text{C}$ under 4.5% H_2 -He flow, and the antiferromagnetic phase transition temperatures of the annealed crystals were found from magnetic susceptibility and heat capacity measurements to be 69 K.⁶ The difference in T_N between the powder and single crystal samples may be related to different unit cell volumes of these samples. The unit cell volumes in the powder and single crystal CaV_2O_4 samples are $296.0(5)$ and $298.0(5)\text{ \AA}^3$, respectively. The reason for this difference is, however, unknown at present. A similar correlation between T_N and the lattice volume was observed in EuCu_2Ge_2 .⁸ The magnetic susceptibility of crystal 2 is shown in Fig. 3, with the field along a and b directions. The antiferromagnetic transition temperature T_N is clearly seen as a bifurcation in the susceptibilities along the two directions. We note that, when the field is along the b direction, a splitting between zero-field-cooled and field-cooled susceptibilities is observed below $T=20\text{ K}$.

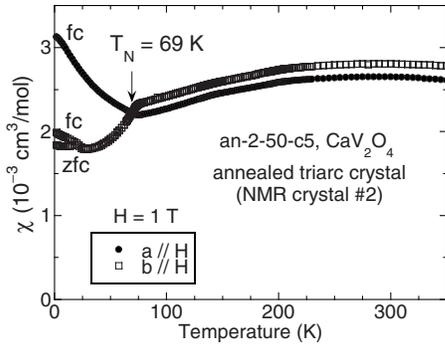


FIG. 3. Magnetic susceptibility χ versus temperature T of CaV_2O_4 crystal 2 measured with the applied field $H=1$ T along the a and b directions. The vertical arrow indicates the antiferromagnetic transition temperature $T_N=69$ K. The measurements were carried out under either field-cooled or zero-field-cooled conditions, as indicated.

A search for a zero-field ^{51}V NMR echo signal was performed at 4.2 K and was found to be located close to a frequency of 237 MHz at that temperature. The echo was produced by a sequence of two pulses with the same pulse length, which was typically 4 μs and about half the length of a $\pi/2$ pulse. The separation between the pulses was fixed to 18 μs . ^{51}V NMR spectra were measured by plotting the echo intensity as a function of the magnetic field. A variable magnetic field from 0 to 2.0 T was produced by an electromagnet. The value of the magnetic field was measured by a Hall magnetometer attached to one of the two magnet pole caps. The difference between the measured field and the field at the position of the sample (measured by the resonance frequency of protons in water) was less than 0.005 T over the whole field range. Individually, the crystals were placed inside copper solenoid coils with the crystal c axis parallel to the coil axis. Measurements of crystal 1 involved rotation of the field in the a - b and b - c planes. Measurements of crystal 2 involved rotation of the field in the a - b plane. The rotation of the field was achieved by rotating the cryostat together with the crystal about the crystallographic axes, perpendicular to the field plane. The misalignment between the rotation axis and the intended crystallographic axis is estimated to be less than 5° .

III. ^{17}O NMR IN POWDER SAMPLE OF CaV_2O_4

Figure 4 displays the ^{17}O NMR spectra for the ^{17}O -enriched powder sample of CaV_2O_4 in $H=3$ T at three different temperatures. The spectrum at $T=296$ K was obtained via Fourier transform of half the echo signal, while the spectra at $T=80$ and 77 K were obtained by frequency sweep. ^{17}O nuclei have spin 5/2 and, thus, possess a nonzero electric quadrupole moment. Since the local environments of all oxygen sites do not possess cubic symmetry (point group m), one expects a quadrupole splitting of the ^{17}O resonance frequencies. We attribute the lack of a powder pattern of the first order quadrupole splitting in the observed spectra to a smaller quadrupole splitting compared to the magnetic

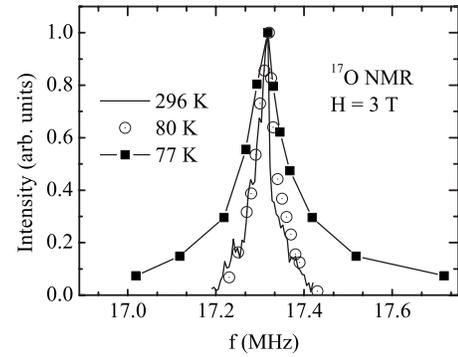


FIG. 4. Absorption spectrum of the ^{17}O NMR signal for an ^{17}O -enriched powder sample of CaV_2O_4 at three different temperatures in an applied magnetic field $H=3.0$ T. A strong inhomogeneous broadening is observed close to the magnetic transition temperature $T_N=78$ K. The solid line at 77 K is a guide for the eye.

broadening of the spectra. The positions of the spectrum peak position show negligible field dependence. The chemical shift K of the peak position is given by $K=A_{\text{hf}}\chi$, where A_{hf} is the isotropic hyperfine coupling constant and χ is the magnetic susceptibility. Using the data in Figs. 2 and 4 and additional $\chi(T)$ data (not shown), we obtain the upper limit $A_{\text{hf}} \lesssim 1.7$ kG/ μ_B .

The line gets broader below T_N with decreasing temperature. As shown in Fig. 4, the absorption line at $T=77$ K is much broader than the lines at $T=80$ and 296 K. As will be further shown below, this broadening is a signature of an antiferromagnetic phase transition at $T_N=78$ K, where the nuclear spin-lattice relaxation rate $1/T_1$ exhibits a peak. As the temperature approaches the phase transition temperature, the electronic vanadium spins slow down dramatically and, thus, induce an inhomogeneous static (on the NMR time scale) dipolar or transferred hyperfine field on neighboring ^{17}O sites and broaden the ^{17}O NMR line. Due to the fast decrease of signal intensity below T_N with decreasing temperature, detailed measurements of the temperature dependence of the line broadening in this temperature range were not pursued.

The recovery of the ^{17}O longitudinal nuclear magnetization $M(t)$ following the saturation pulses is a single exponential function at $T > 100$ K. This shows that all the ^{17}O NMR transitions are saturated and, thus, there are no satellite peaks located away from the main peaks displayed in Fig. 4, consistent with a small quadrupole splitting as discussed above. Below 100 K, deviation from single exponential behavior is observed, indicating a distribution of $1/T_1$ values. In order to extract a characteristic relaxation rate at all temperatures, we fitted the recovery curves to a stretched exponential function

$$1 - \frac{M(t)}{M(\infty)} = \exp\left[-\left(\frac{t}{T_1^*}\right)^\beta\right]. \quad (1)$$

The relation of the parameters $1/T_1^*$ and β to the $1/T_1$ distribution underlying a stretched exponential function has been discussed in a recent paper.¹² Figure 5 shows the temperature dependence of $1/T_1^*$ and β in $H=3.0$ and 4.7 T. At

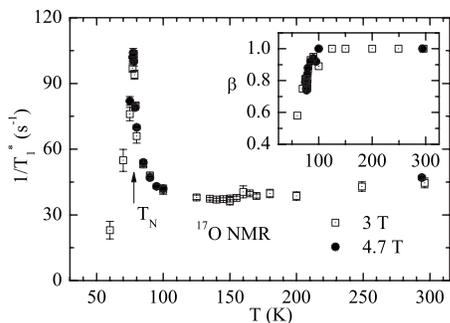


FIG. 5. Temperature T dependence of the ^{17}O nuclear spin-lattice relaxation rate $1/T_1^*$ [see Eq. (1)] of ^{17}O -enriched powder CaV_2O_4 in applied magnetic fields $H=3.0$ and 4.7 T. A strong peak is observed close to the antiferromagnetic transition temperature $T_N=78$ K, as labeled by the arrow. Inset: The stretching exponent β versus T .

$T > 100$ K, the relaxation rate is almost temperature independent. Below 100 K, $1/T_1^*$ exhibits a strong enhancement and reaches a peak at $T_N=78$ K. Combining the above NMR results with magnetization studies of powder and single crystals,⁶ and with the magnetic susceptibility data in Fig. 2, we identify the $1/T_1^*$ peak temperature as the temperature of an antiferromagnetic phase transition T_N . The peak in the nuclear spin-lattice relaxation rate at T_N results from an enhancement and slowing down of the electronic spin fluctuations at wave vectors close to the antiferromagnetic ordering vector as the temperature approaches T_N from either side.¹³

IV. ^{51}V NMR BELOW T_N IN SINGLE CRYSTALS OF CaV_2O_4

A. Spin structure at 4.2 K

In an external magnetic field \mathbf{H} , the resonance frequency f of the ^{51}V nuclear spins is given by

$$f = |A\langle\mathbf{S}\rangle + \mathbf{H}|\gamma_v/2\pi, \quad (2)$$

where A is the hyperfine coupling constant between the nuclear spin and the vanadium electronic spins \mathbf{S} , γ_v is the gyromagnetic ratio of ^{51}V nuclear spins, and $\langle\mathbf{S}\rangle$ denotes the average electronic spin value in thermal equilibrium. In our experiments, the local field is much larger than the applied field: $A|\langle\mathbf{S}\rangle| \gg H$. Depending on whether the applied field component along $\langle\mathbf{S}\rangle$ is parallel or antiparallel to $\langle\mathbf{S}\rangle$, the resonance frequency shifts to higher or lower values, respectively. If CaV_2O_4 is a collinear antiferromagnet at low temperatures, where opposite spin directions exist, upon application of an external field along the ordering axis, the zero-field spectrum should split into two peaks. These peaks should be symmetrically displaced above and below the zero-field peak frequency.

Figure 6 shows the field-swept spectra with the field at different angles in the $a-b$ plane, measured with rf both higher and lower than the zero-field peak frequency $f_0=236.7$ MHz. All measurements in this section were performed on CaV_2O_4 crystal 1. In contrast to a single peak

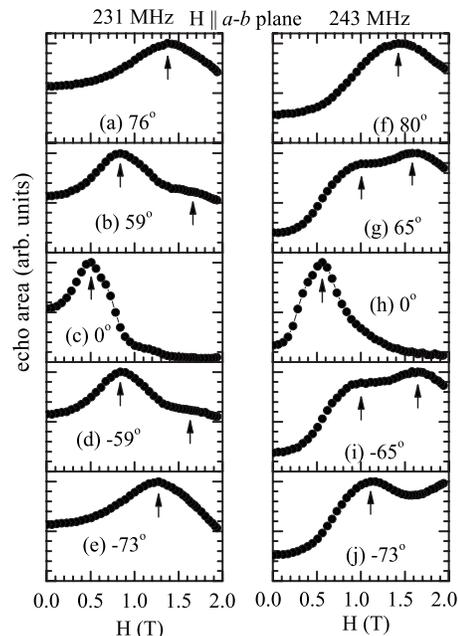


FIG. 6. Field-swept spectra with the applied magnetic field parallel to the $a-b$ plane at rf of 231 MHz (left panels) and 243 MHz (right panels). The angles between the field and the average of the two projections of the two spin directions onto the $a-b$ plane (S'_m in Fig. 10) are labeled in each panel. The arrows indicate the positions of the peaks. S'_m is approximately parallel to the crystallographic b axis. The spectra were measured at 4.2 K on crystal 1.

above and a single peak below the zero-field peak frequency f_0 when an applied field is present, as expected for a collinear antiferromagnet, instead we see two peaks above f_0 and two peaks below f_0 in applied fields as shown by the vertical arrows in Fig. 6. Whether each set of two peaks is resolved depends on the angle of the applied field in the $a-b$ plane as shown. We infer below that the spectra in Fig. 6 (and Fig. 8) are consistent with a magnetic structure at 4.2 K that consists of two antiferromagnetic substructures, each of which is a collinear antiferromagnetic arrangement where the angle between the ordering axes of the two substructures is $19(1)^\circ$. The angle labeled in each panel of Fig. 6 is the angle between the applied field and the axis S'_m , which is the average of the projections onto the $a-b$ plane of the two spin ordering directions (see Fig. 10 below). S'_m is approximately parallel to the b axis and is determined by fitting the peak positions versus angle, as will be explained below.

In our discussions of the ^{51}V NMR results, we assume that the applied magnetic field only shifts the NMR frequency without affecting the electronic spins. In fact, the ordered electronic moments can be tilted by the applied field due to the presence of a torque. However, we can show that the tilting angle is indeed negligibly small. From the magnetization measurements,⁶ at 4.2 K, the susceptibility χ of single crystal CaV_2O_4 with applied field in the a , b , or c direction is $\chi \sim 0.003$ cm³/mol, which corresponds to an induced moment of $0.005\mu_B$ for each vanadium spin in a 2 T field. The tilting angle required to produce such a moment is only 0.3° , assuming an ordered moment of $1.06\mu_B$.⁷ Both this angle and the induced moment are negligible to our studies.

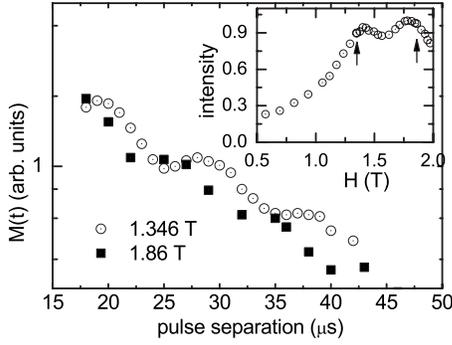


FIG. 7. Semilogarithmic plot of nuclear spin-spin relaxation curves at rf $f=222$ MHz and external magnetic fields of 1.346 and 1.86 T. The errors on the data points are smaller than the sizes of the symbols. The fields are parallel to the $a-b$ plane and form an angle of 31° from the S'_m direction. Inset: The field-swept spectrum measured at a fixed pulse separation of $18 \mu\text{s}$ and $f=222$ MHz in the same field direction. The vertical arrows show the field positions of 1.346 and 1.86 T. The measurements were performed at 4.2 K on crystal 2.

The spectra in Fig. 6 exhibit a two-peak structure when the field points away from the S'_m axis. When measured by a field swept at a fixed frequency f , each peak i ($=1, 2$) should appear at the field value

$$H_{\text{peak } i} = |-f_0 \cos \alpha_i + \sqrt{f^2 - f_0^2 \sin^2 \alpha_i}| / (\gamma_v / 2\pi), \quad (3)$$

where α_i is the angle between the field and the respective electronic spin ordering direction of a magnetic substructure noted above. The observed two-peak structures for $f > f_0$ and $f < f_0$ strongly indicate the presence of these two different antiferromagnetic spin ordering directions in the system. The ability to resolve the two peaks at the larger angles in Fig. 6 (and Fig. 8) is related to the larger partial derivative of $|\partial H_{\text{peak } i} / \partial \alpha_i|$ of Eq. (3) at the larger α_i values for $\alpha_i < \pi/2$ rad.

The two peaks in the same spectrum have different heights, as can be clearly seen in Figs. 6(b), 6(d), 6(g), and 6(i). The reason behind this difference is currently not understood. It may be due to the change of the nuclear spin-spin relaxation times at different field values, since we fix the separation between the two rf pulses for echo generation to be $18 \mu\text{s}$. In fact, we observed a field-dependent oscillation of the spin echo intensity as a function of the separation between the two echo-generating pulses. Figure 7 displays two nuclear spin-spin relaxation curves measured under identical conditions except for different external magnetic fields of 1.346 and 1.86 T, respectively. The oscillation pattern shows a clear field dependence. However, without knowing the detailed functional form of the decay curves, we cannot extrapolate the signal intensity back to zero pulse separation to correct for the nuclear spin-spin relaxation effect.

We further note that the different heights of the two peaks cannot be attributed to the different percentages of spins in the two spin substructures. In such a scenario, the spins contributing to the left peaks in Figs. 6(b) and 6(g) should con-

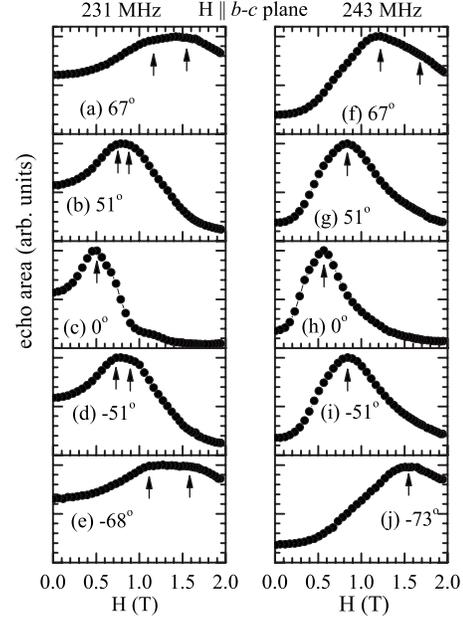


FIG. 8. Field-swept spectra with the applied magnetic field parallel to the $b-c$ plane at rf of 231 MHz (left panels) and 243 MHz (right panels). The angles between the field and the average of the two projections of the two spin directions onto the $b-c$ plane (S''_m in Fig. 10) are labeled in each panel. The arrows indicate the positions of the peaks. The spectra were measured at 4.2 K on crystal 1.

tribute to the right peaks in Figs. 6(d) and 6(i) (see Fig. 11), and the left peaks should be higher in one orientation while lower in the other in Figs. 6(b) and 6(d) and in Figs. 6(g) and 6(i), respectively. However, the spectra in Figs. 6(b) and 6(d) and in Figs. 6(g) and 6(i), are almost the same. The symmetry in the spectra with the field on opposite sides of S'_m , such as in Figs. 6(b) and 6(d) and in Figs. 6(g) and 6(i), indicates that the number of spins in the two substructures are the same.

Since the above two-peak structure is observed with the field in the $a-b$ plane, these measurements can only detect the difference of the spin projections of the two substructures onto the $a-b$ plane. In order to determine whether or not the projections onto the $b-c$ plane are also different, we also measured the spectra with the field in the $b-c$ plane. Some representative spectra with the field in different directions are displayed in Fig. 8, where the angles listed are described in the caption. As one can see, a two-peak structure is still observed when the field is at a large angle from the S''_m axis. However, the separations between the two peaks are smaller than in Fig. 6, indicating a smaller angle between the two easy axis projections onto the $b-c$ plane than onto the $a-b$ plane.

In order to study whether there exists canting and/or an imbalance in the number of spins in opposite directions for each of the two ordered magnetic substructures, we compared the spectra with those measured with the field rotated by 180° . Figure 9 displays two spectra measured at $f = 222$ MHz, with the field parallel to the $a-b$ plane and -31° and 149° away from the S'_m direction, respectively. These two spectra are identical within experimental error, indicat-

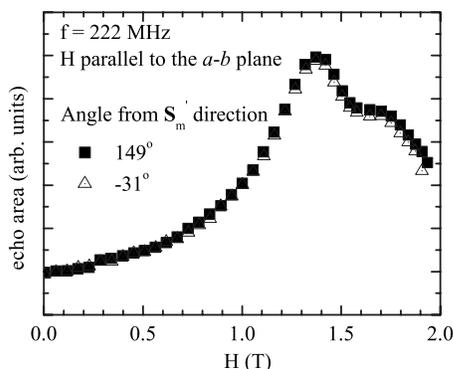


FIG. 9. Comparison of two spectra measured at rf $f = 222$ MHz with and without the field direction reversed. The fields are parallel to the a - b plane and form angles of -31° and 149° from the S'_m direction, respectively. The spectra were measured at 4.2 K on crystal 1.

ing the absence of spin canting and the same number of spins in opposite directions within each magnetic substructure.

Thus, we propose a model of the spin structure as shown in Fig. 10. Various notations used in the model are explained in the caption of Fig. 10. There are equal numbers of spins in the two antiferromagnetic substructures, each of which consists of collinear antiparallel spins also with equal number. The plane defined by the two ordering directions is parallel neither to the a - b nor the b - c plane. The average ordered moment direction S_m is approximately parallel to the b axis. This is consistent with single crystal anisotropic magnetization measurements versus temperature which showed that below T_N , the average easy axis of the magnetic structure is approximately the b axis.⁶ Note that in our NMR study, we cannot determine the location in the lattice of the two different magnetic substructures.

To extract the angle between the spin ordering directions of the two substructures, we measured the dependence of the

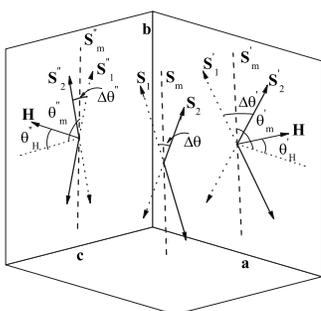


FIG. 10. The proposed ordered spin structure in CaV_2O_4 . There are two different antiferromagnetic ordering substructures with equal numbers of spins, each of which has a collinear antiferromagnetic spin arrangement. $\Delta\theta$, $\Delta\theta'$, and $\Delta\theta''$ are the angles between these two directions, and their projections on a - b and b - c planes, respectively. S_m , S'_m , and S''_m are the average of the two directions and their projections on a - b and b - c planes, respectively. θ'_H (θ''_H) and θ'_m (θ''_m) are the angles formed between a fixed arbitrary experimental reference direction in the a - b (b - c) plane and the applied field H and S'_m (S''_m), respectively.

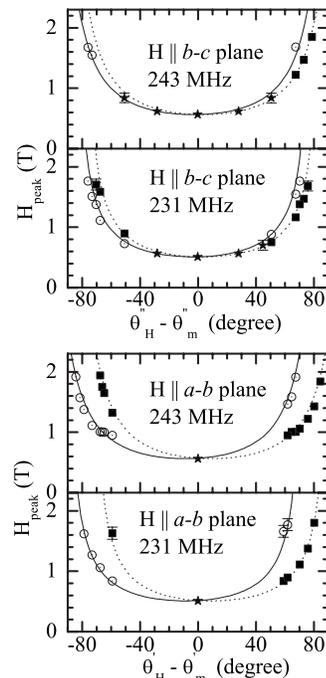


FIG. 11. Dependence of the peaks in the spectra at 4.2 K on the direction of the applied magnetic field, with the field in the b - c (top two panels) and a - b (bottom two panels) planes of crystal 1, where the rf are equal to 231 and 243 MHz, respectively. For definitions of the angles θ'_H , θ'_m , θ''_H , and θ''_m , see Fig. 10. Circles and filled squares correspond to the two different spin ordering directions of the two magnetic substructures, respectively. The symbol \star is used when the two peaks from the two spin directions overlap and only a single peak can be observed. The error in H_{peak} is comparable to the size of the symbols unless shown explicitly. The solid and dotted lines represent the fits by the theoretical prediction in Eq. (3).

peak positions versus the field directions at rf of 231 and 243 MHz. The results are shown in Fig. 11. For small angles between H and S'_m or S''_m , only one peak is observed. At larger angles, the positions of two peaks can be resolved. Two different symbols are used to represent the two different spin substructures, while for spectra with single peaks, a third symbol is used. Since the angle between the spin direction and the b axis is much less than 1 rad, $\cos \alpha_i$ in Eq. (3) for the field in the a - b plane can be approximated by

$$\cos \alpha_{1,2} \approx \cos(\theta'_m \pm \Delta\theta'/2 - \theta'_H), \quad (4)$$

where $\alpha_{1,2}$ are the angles between the field and the two spin directions S_1 and S_2 , respectively. Similarly, for the field in the b - c plane, one has

$$\cos \alpha_{1,2} \approx \cos(\theta''_m \pm \Delta\theta''/2 - \theta''_H). \quad (5)$$

We fitted Eq. (3) with $\cos \alpha_{1,2}$ given by Eqs. (4) and (5) to the data in Fig. 11. The free parameters in the fit were f_0 , θ'_m , θ''_m , $\Delta\theta'$, and $\Delta\theta''$. The best fit results are $f_0 = 236.7(2)$ MHz, $\Delta\theta' = 18(1)^\circ$, and $\Delta\theta'' = 6(1)^\circ$. The fits are shown in Fig. 11. Since the angles between the spins and the b axis are much less than 1 rad, we have

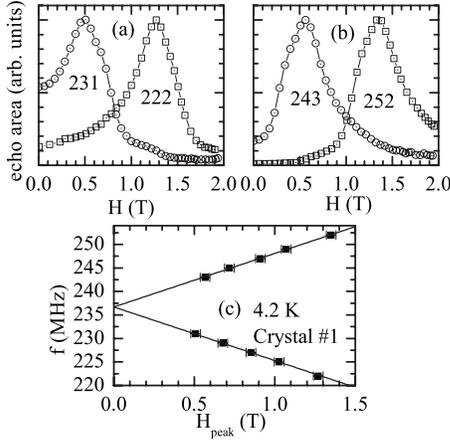


FIG. 12. [(a) and (b)] Field-swept ^{51}V NMR spectra at four different frequencies at 4.2 K. The frequencies are given under each spectrum in units of MHz. The field is applied parallel to the S''_m direction. (c) The frequency versus the peak field of the spectra. The solid lines are linear fits by Eq. (7). The measurements were done on crystal 1 at 4.2 K.

$$\sin \Delta\theta \approx \sqrt{\sin^2 \Delta\theta' + \sin^2 \Delta\theta''}, \quad (6)$$

from which one obtains the angle between the easy axes of the two magnetic substructures to be $\Delta\theta=19(1)^\circ$.

In addition to the study of the angular dependence of the peak positions, we also measured their frequency dependences to further confirm the proposed spin structure. Figures 12(a) and 12(b) show the field-swept spectra with the field H pointing along the S''_m direction, at rf lower and higher than $f_0=236.7$ MHz, respectively. Note that when $H\parallel S''_m$, the two magnetic substructures have the same peak positions of the spectra (see the zero-angle data in Fig. 11). The peaks in Figs. 12(a) and 12(b) both shift to higher fields when the frequency shifts further away from f_0 , respectively. The peak positions H_{peak} versus rf are plotted in Fig. 12(c). The two sets of data points can be well fitted by the two linear equations

$$f = f_0 \pm H_{\text{peak}}\gamma/2\pi, \quad (7)$$

where f_0 is the peak frequency of the spectrum at zero applied field. A fit of Eq. (7) to the data gives $\gamma/2\pi = 11.4(2)$ MHz/T and $f_0=236.7(1)$ MHz. Assuming S_m to be parallel to the b axis, the value of γ should be $\gamma/2\pi = (\gamma_v/2\pi)\cos(\Delta\theta/2)=11.07$ MHz/T, where $\Delta\theta=19^\circ$ is the above angle between the ordering directions of the two magnetic substructures. This value of $\gamma/2\pi$ is very close to the above fitting result.

B. Ordered moment and its temperature dependence

In this section, we will study the temperature dependence of the vanadium ordered moment, which provides evidence for an energy gap in the antiferromagnetic spin wave excitation spectrum, arising from anisotropy effects. Then we will discuss the value of the saturation vanadium spin moment at low temperatures. Measurements in this section were per-

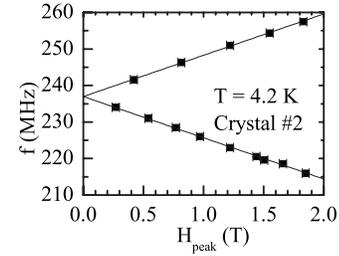


FIG. 13. rf f versus peak H_{peak} in field-swept spectrum in crystal 2 at 4.2 K. The field is applied along the S'_m direction. The solid lines are fits with Eq. (7).

formed on crystal 2. The experiment was set up to allow field rotation in the a - b plane. By rotating the field in the a - b plane, the S'_m direction (see Fig. 10) is identified as the direction along which the peak position in the spectrum is a minimum at a fixed rf away from f_0 (see Fig. 11). After identifying the S'_m direction, all subsequent measurements of the spectra were performed versus H at fixed rf with the field along the S'_m direction.

With the field along S'_m , only a single peak is observed in the spectrum at each frequency (see Fig. 12). In Fig. 13, we display the frequency dependence of the peak position at 4.2 K. Similar to the case of crystal 1 (Fig. 12), the data points can be well fitted by two straight lines. A fit of Eq. (7) to the data gives $f_0=236.98(8)$ MHz and $\gamma/2\pi = 11.3(1)$ MHz/T. This value of γ is in agreement with the fitting value in crystal 1. However, the value of f_0 is slightly larger than in crystal 1. This slight difference may be due to sample-dependent differences.

Figure 14 displays representative spectra measured at four different temperatures. For comparison between the different spectra, the x axis has been converted to the quantity $f + H\gamma/2\pi$, with $\gamma/2\pi=11.3$ MHz/T. As the temperature increases, the signal intensity decreases rapidly and the spectra can only be measured below 45 K. In order to more accurately determine the peak position of the spectra, we fitted

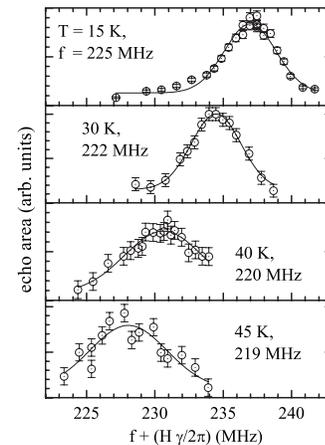


FIG. 14. Field-swept spectra at different temperatures on crystal 2. The temperature and the rf for each measurement are labeled in each panel. The solid lines are fits by Eq. (8) to extract the peak positions.

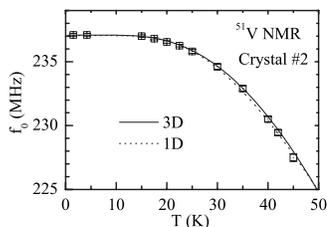


FIG. 15. Temperature dependence of the ^{51}V NMR spectra peak position in zero applied field in CaV_2O_4 crystal 2. The dotted and solid curves are fits by Eq. (19) with one-dimensional spin wave dispersion and Eq. (20) with three-dimensional dispersion, respectively.

the original field-swept spectra (with the x axis being H) by a Gaussian function

$$I(H) = A + B \exp[-2(H - H_{\text{peak}})^2/W^2], \quad (8)$$

with A , B , H_{peak} , and W as fitting parameters. The zero-field peak frequency f_0 is then determined from

$$f_0 = f \pm H_{\text{peak}} \gamma/2\pi,$$

where $\gamma/2\pi = 11.3$ MHz/T, and the $+$ and $-$ signs correspond to the cases of $f < f_0$ and $f > f_0$, respectively. In order to determine whether $f < f_0$ or $f > f_0$, spectra were measured with at least two different frequencies at each temperature. With the correct choices of the $+$ or $-$ signs, the obtained f_0 values for different spectra as in Fig. 14 are the same within experimental error at each temperature. The final f_0 value is an average over all calculated f_0 values for various spectra at the same given temperature.

Figure 15 shows the temperature dependence of f_0 . Since the temperature dependence of the hyperfine coupling constant can be ignored,¹⁴ $f_0(T)$ is directly proportional to the ordered local moment. The ordered moment is almost temperature independent at $T < 15$ K. In the spin wave theory of a three-dimensional antiferromagnet *without anisotropy*, the initial decrease of the ordered moment with temperature T should follow a T^2 dependence.¹⁵ Fitting the data by a power law gives an exponent ≥ 3.5 , an unphysically large value (not shown). The temperature independence below $T < 15$ K, thus, indicates the presence of an anisotropy-induced energy gap for spin wave excitations.¹⁶

Before estimating the gap energy, we will first estimate the value of the saturation moment at $T=0$ K. The local moments reach their saturation value at $T < 15$ K. From the value of $f_0 = 237$ MHz at $T < 15$ K, one obtains a local field value of $H_{\text{loc}} = f_0/(\gamma_0/2\pi) = 21.2$ T. In order to infer the value of local moment from the local field value, the hyperfine coupling constant A and the g -factor have to be determined. With known values of A and g , the ordered moment $\langle \mu_z \rangle$ is $|\langle \mu_z \rangle| = g\mu_B H_{\text{loc}}/A$. The local field is dominated by the contact interaction through the polarized core electrons, which is approximately proportional to the number of unpaired electronic spins in the $3d$ orbitals with a proportionality constant of 12.5 T per unpaired electron to within 20%.⁹ However, besides the contact interaction, orbital effects¹⁰ and transferred hyperfine coupling with the neigh-

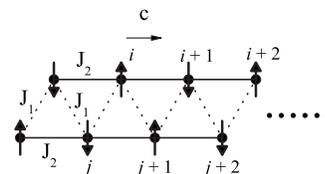


FIG. 16. Zigzag spin structure in CaV_2O_4 . Due to the alternation of the spin directions along the c axis, the interaction between the spins in the two legs of the zigzag chain is essentially decoupled. The possible misalignment of 19° between spins in the two legs of the zigzag chain is ignored. J_1 and J_2 are the nearest-neighbor interleg and intraleg exchange interactions, respectively.

boring V^{3+} ions¹⁷ may also contribute significantly to the local field at the ^{51}V nuclear site.

In the absence of a knowledge of the orbital effects and transferred interactions, we will estimate a possible range of the $A/g\mu_B$ value in CaV_2O_4 using the known values of $A/g\mu_B$ in other V^{3+} compounds. The values of $A/g\mu_B$ in LaVO_3 , YVO_3 , and V_2O_3 are 16.8, 20.8, and 15.5 T/μ_B , respectively.¹⁸ For V^{3+} in Al_2O_3 , electron paramagnetic resonance measurements gave $A/g\mu_B = 13.3$ T/μ_B .¹⁹ The range of $A/g\mu_B$ in the above four compounds is between 13.3 and 20.8 T/μ_B . Assuming $A/g\mu_B$ in CaV_2O_4 lies in the same range, the low temperature ordered vanadium moment in CaV_2O_4 is, thus, in the range of 1.02–1.59 μ_B . This $|\langle \mu_z \rangle|$ range is consistent with the value 1.06(6) μ_B extracted from the previous neutron powder diffraction study.⁷

Next we estimate the energy gap for the spin wave excitations. From the neutron diffraction studies,⁷ we know that the spins reverse their ordering direction upon moving along the c axis. Therefore, the spin structure in the ordered state within a zigzag chain should look as in Fig. 16, where we ignore the possible small misalignment of 19° between spins in the two magnetic substructures discussed above. Because each spin in one leg of the chain couples by the same exchange constant J_1 to two spins in the other leg that are ordered in opposite directions, we expect that the effective coupling between the two legs within a zigzag chain is greatly reduced in the ordered state. As a result, we will consider the nearest-neighbor interactions within the leg J_2 as the only dominant magnetic interaction and treat the effect of interleg interaction within a zigzag chain as a weak interchain interaction. For simplicity, we will use a single exchange constant J' to characterize the effect of the interchain interactions. To include the effect of anisotropy, we assume a single ion anisotropy in the system with a single direction of easy axis. Then, the Hamiltonian can be written as

$$H = \sum_i \left(2J_2 \mathbf{S}_i \cdot \mathbf{S}_{i+1} - \frac{1}{2} K S_{iz}^2 \right) + 2 \sum_{\langle i,j \rangle} J' \mathbf{S}_i \cdot \mathbf{S}_{j+1}, \quad (9)$$

where K is the anisotropy constant, the index i runs through the spins in one leg of the chain, and the summation $\langle i,j \rangle$ runs through all interleg and interchain nearest-neighbor pairs.

The Fourier transform of the exchange interactions is

$$\mathcal{J}(q) = \sum_j J(\mathbf{r}_{ij}) \exp(-iq \cdot \mathbf{r}_{ij}),$$

where \mathbf{r}_{ij} connects two spins in opposite sublattices, $J(\mathbf{r}_{ij}) > 0$ is the nearest-neighbor exchange constant, and the index j runs through all the nearest-neighbor spins of spin i in the opposite sublattice (each sublattice consists of spins in the same direction). The spin wave dispersion relation is given by²⁰

$$E_q = \{[2S\mathcal{J}(0) + KS]^2 - [2S\mathcal{J}(q)]^2\}^{1/2}, \quad (10)$$

where we ignored interactions between spins in the same sublattice. The spin wave gap value is given by the value of E_q at $q=0$. In the limit of small anisotropy $K \ll 2\mathcal{J}(0) \approx 4J_2$, the gap energy is given by

$$E_G = 2S[\mathcal{J}(0)K]^{1/2}. \quad (11)$$

In the spin wave theory, the decrease of sublattice magnetization is due to the thermal activation of spin wave excitations. In the above bipartite antiferromagnetic system,²⁰

$$\langle S_z(0) \rangle - \langle S_z(T) \rangle = \frac{V}{(2\pi)^3} \int \langle n_q \rangle \frac{2\mathcal{J}(0)S + KS}{E_q} d^3q, \quad (12)$$

where the integral is limited to the first Brillouin zone of one sublattice, V is the sample volume per sublattice site, and

$$\langle n_q \rangle = \frac{1}{e^{E_q/k_B T} - 1}$$

is the number of thermally excited antiferromagnetic magnons.

The dispersion relation in Eq. (10) depends on the spin lattice structure and the exchange interactions $J(\mathbf{r})$. For a quasi-one-dimensional chain with interchain coupling J' , at temperatures $T \gg J'/k_B$, one can ignore the dispersion perpendicular to the chain direction. Then for small values of q_c , which is the \mathbf{q} vector component along the chain, one can perform a Taylor series expansion of $|\mathcal{J}(q)|^2$ as

$$|\mathcal{J}(q)|^2 \approx |\mathcal{J}(0)|^2 [1 - l^2 q_c^2], \quad (13)$$

where l is the nearest-neighbor distance within the leg.

At $T \ll J_2/k_B$, only spin waves at small q_c values have significant contributions to the integral in Eq. (12), so one can change the limits of integral for q_c in Eq. (12) to $\pm\infty$. The small q approximation is valid only at temperatures where $1 - |\langle S_z(T) \rangle|/|\langle S_z(0) \rangle| < 0.1$,¹⁶ which is satisfied within our experimental temperature range. Substituting Eq. (13) into Eq. (10), and changing the limits of integral for q_c in Eq. (12) to $\pm\infty$, one obtains in the limit of small anisotropy $K \ll 2\mathcal{J}(0)$ and $T \ll E_G$,

$$1 - \frac{\langle S_z(T) \rangle}{\langle S_z(0) \rangle} \approx B e^{-E_G/k_B T} (E_G/k_B T)^{-1/2}, \quad (14)$$

where

$$B \approx \frac{2}{\sqrt{2\pi}} = 0.80. \quad (15)$$

Equation (14) is valid at temperatures $J'/k_B \ll T \ll J_2/k_B$. In CaV_2O_4 , J'/k_B might fall within the experimental temperature range in Fig. 15 ($1.5 \leq T \leq 45$ K). So it is useful to consider the other limit of $T \ll J'/k_B \ll J_2/k_B$, where a three-dimensional dispersion is more appropriate. Applying a small q approximation, one obtains

$$|\mathcal{J}(q)|^2 \approx |\mathcal{J}(0)|^2 \{1 - \eta^2 (V/2)^{2/3} [q_c^2 + j'(q_a^2 + q_b^2)]\}, \quad (16)$$

where, for simplicity, we assumed an isotropic dispersion in the a - b plane, η is a geometrical factor of order 1 which depends on the spin structure,²¹ and j' is of the order of J'/J_2 . By combining Eqs. (10), (12), and (16), and changing the three limits of integrations to $\pm\infty$ in Eq. (12), then instead of Eq. (14), we have in the limit of small anisotropy $K \ll 2\mathcal{J}(0)$ and $T \ll E_G$,¹⁶

$$1 - \frac{\langle S_z(T) \rangle}{\langle S_z(0) \rangle} \approx B e^{-E_G/k_B T} (E_G/k_B T)^{-3/2}, \quad (17)$$

where

$$B \approx \frac{\sqrt{2\alpha}}{\pi^{3/2} \eta^3 j'}, \quad (18)$$

with $\alpha \equiv K/[2\mathcal{J}(0)]$.

Using Eqs. (14) and (17) and the relation

$$f_0(T)/f_0(0) = |\langle S_z(T) \rangle|/|\langle S_z(0) \rangle|,$$

one obtains the variation of the zero-field ⁵¹V NMR resonance frequency f_0 as (for one dimension)

$$f_0(T) = f_0(0) [1 - B e^{-E_G/k_B T} (E_G/k_B T)^{-1/2}] \quad (19)$$

or (for three dimensions)

$$f_0(T) = f_0(0) [1 - B e^{-E_G/k_B T} (E_G/k_B T)^{-3/2}], \quad (20)$$

depending on whether a one-dimensional (1D) or three-dimensional (3D) dispersion is used for E_q . We fitted Eqs. (19) and (20) to the $f_0(T)$ versus T data in Fig. 15 at $T \leq 45$ K, with $f_0(0)$, B , and E_G as free parameters. The best fit results are $f_0(0) = 237.04(5)$ MHz, $E_G = 98(5)$ K, and $B = 0.51(7)$ for the 1D dispersion with Eq. (19), and $f_0(0) = 237.08(6)$ MHz, $E_G = 64(5)$ K, and $B = 0.27(6)$ for the 3D dispersion with Eq. (20). The best fit curves are shown as the dotted and solid curves in Fig. 15, respectively. Since Eqs. (19) and (20) are derived under the two limiting conditions of $T \gg J'/k_B$ and $T \ll J'/k_B$, respectively, one can expect that the actual E_G value might lie somewhere between 64 and 98 K. Given a value of E_G , we can make a rough estimate of the anisotropy constant K . From the magnetization study, one estimates the intrachain nearest-neighbor exchange constant to be of the order of $J_2/k_B \sim 200$ K.⁶ Taking $S=1$, $E_G = 81$ K, and $\mathcal{J}(0) \approx 2J_2$, we thus have from Eq. (11) that $K/k_B \sim 4$ K.

The above fitting value of $B=0.51(7)$ from 1D dispersion is similar to the calculated value of 0.80. The fitting value of $B=0.27(6)$ from the 3D dispersion constrains the value of J' in the 3D model. Taking $\alpha \approx K/4J_2 \sim 0.01$, $\eta \sim 1$, and $B = 0.27$, then from Eq. (18) one has $j' \sim 0.01$ and J'/k_B

$\sim j'J_2/k_B \sim 2$ K. However, this value of J' seems inconsistent with the initial assumption of $T \ll J'/k_B$ required for the three-dimensional model to be valid. Therefore, Eq. (19) of the 1D model might provide a better approximation to the $f_0(T)$ data.

V. SUMMARY AND CONCLUSIONS

We have presented ^{17}O and ^{51}V NMR results on the zigzag spin chain compound CaV_2O_4 . The strong inhomogeneous broadening and a peak in the nuclear spin-lattice relaxation rate versus temperature of ^{17}O NMR confirm the presence of an antiferromagnetic phase transition at 78 K in a powder sample. The crystals we studied have $T_N=69$ K. ^{51}V NMR in the ordered state of crystals reveals the presence of two antiferromagnetic substructures at 4.2 K, each of which is collinear and which form an angle of $19(1)^\circ$ between them with the average direction approximately parallel

to the b axis. The origin and location in the lattice of the different spin substructures remain unknown. However, we speculate that the two magnetic substructures are associated with the two inequivalent V^{3+} $S=1$ zigzag spin chains in the orthorhombic crystal structure, respectively. Magnetic neutron diffraction studies are required to further characterize the magnetic structure below T_N . The temperature dependence of the zero-field resonance frequency at low temperatures suggests the presence of magnetic anisotropy and an energy gap in the spin wave excitation spectrum. The energy gap is estimated from spin wave theory to be between 64 and 98 K.

ACKNOWLEDGMENTS

We acknowledge F. Borsa, B. Lake, and A. Kreyssig for useful discussions. Work at the Ames Laboratory was supported by the Department of Energy-Basic Energy Sciences under Contract No. DE-AC02-07CH11358.

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