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TWO-PHASE SAMPLING EXPERIMENT FOR PROPENSITY SCORE ESTIMATION IN SELF-SELECTED SAMPLES

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Self-selected samples are frequently obtained due to different levels of survey participation propensity of the survey individuals. When the survey participation is related to the survey topic of interest, propensity score weighting adjustment using auxiliary information may lead to biased estimation. In this paper, we consider a parametric model for the response probability that includes the study variable itself in the covariates of the model and proposes a novel application of two-phase sampling to estimate the parameters of the propensity model. The proposed method includes an experiment in which data are collected again from a subset of the original self-selected sample. With this two-phase sampling experiment, we can estimate the parameters in a propensity score model consistently. Then the propensity score adjustment can be applied to the self-selected sample to estimate the population parameters. Sensitivity of the selection model assumption is investigated from two limited simulation studies. The proposed method is applied to the 2012 Iowa Caucus Survey.

1. Introduction. Nonresponse has become a major problem in sample surveys as participation rates have declined in many surveys. When survey units are chosen by surveyors, but these units elect not to participate, self-selection occurs. If many units elect not to participate, the representativeness of the observed sample can be called into question. In this self-selected sample, the participation probabilities are unknown and valid analysis of the self-selected sample is extremely difficult when survey participation is related to survey items [Baker et al. (2013)]. There exist sociological theories, such as the leverage-saliency theory [Groves, Eleanor and Amy (2000)], that try to identify psychological factors influencing survey participation, but it is not clear how to use those theories to analyze observed data.

To reduce the bias of the estimator from self-selected samples, the propensity score weighting method is commonly used. Rosenbaum and Rubin (1983) as well as Rosenbaum (1987) proposed using propensity scores to estimate treatment effects in observational studies. Fuller, Loughin and Baker (1994) and Lundstöm

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and Särndal (1999) proposed nonresponse adjustment methods using regression weighting techniques. Folsom and Singh (2000) also considered a nonlinear calibration procedure to control nonresponse bias. Duncan and Stasny (2001) used the propensity score method to control coverage bias in telephone surveys. Lee (2006) applied the propensity score method to a volunteer panel web survey. Durrant and Skinner (2006) used the method to address measurement error. Lee and Valliant (2009) and Valliant and Dever (2011) considered the propensity score method for a web-based voluntary sample. Kim and Riddles (2012) provided some theory for the propensity score weighting estimators. All of these studies assumed an ignorable selection mechanism. That is, it was assumed that the sample inclusion probability depends on one or more auxiliary variables with known or estimated marginal distributions. In other words, the selection mechanism was assumed to be missing at random in the sense of Rubin (1976). If that is the case, propensity scores can be consistently estimated and the resulting analysis is valid under the assumed propensity score model.

In self-selected samples, the ignorable selection mechanism assumption is not always realistic because survey participation may be related to the survey topic of interest [Groves, Presser and Dipko (2004)]. In this case, the propensity model using only demographic auxiliary variables may lead to biased estimation. In this paper, we consider the nonignorable selection mechanism in the propensity model for survey participation. To estimate the parameters of the propensity model consistently, we propose a novel application of the two-phase sampling experiment in a voluntary survey with voluntary respondents contacted twice. Because the second-phase sample is selected from those who already responded in the first phase, the model parameters in the second-phase sampling mechanism are easy to estimate. Furthermore, the estimated propensity for the second-phase sampling can also provide useful information for the first-phase sampling mechanism if the second contact is very similar to the original first contact.

Our paper is motivated by a telephone survey for the 2012 Iowa Caucus. In this survey the individuals obtained from a probability sampling procedure were asked about their intention to vote in the 2012 Iowa Caucus. Low participation rate (15%) may distort the representativeness of the sample of respondents. In the beginning of the telephone survey, the telephone interviewers identified the purpose of the study and asked for participation in the survey. Thus, survey respondents who chose to participate in this political survey may be systematically different from those who refused to participate. Thus, it is reasonable to assume that selection probability depends on the study variables (intention to vote for given candidates). In November 2011, the first-phase self-selected sample was obtained and then the second self-selected sample was obtained from the first-phase sample in the next month. Due to the similarity of the survey questions for both surveys, we treated the two selection mechanisms identically, up to overall response rates. Then the model parameters were estimated from the two-phase sample and the final estimates for voting intention were computed using the estimated propensity. Further details are presented in Section 6.

2. Basic setup. We introduce the basic setup which is very close to the 2012 Iowa Caucus Survey (ICS). As presented in Figure 2 in Section 6, the sampling structure is a three-phase sampling, where the first-phase sample is a probability sample but the second and the third samples are voluntary samples.

Let U be a finite population of known size N , A be a probability-based sample with known first and second-order inclusion probabilities, denoted by π_i and π_{ij} , and $A_1 (\subset A)$ be a respondent sample obtained from A . In sample A , we observe x_i , where x_i is the vector of auxiliary variables which often consist of demographic information. In sample A_1 , we observe (x'_i, y_{1i}) , and y_{1i} is the realized value of the study variable of interest at the time of observing elements in A_1 . According to the leverage-saliency theory, the selection probability for A_1 can be modeled as a function of x_i and z_i , where z_i is the unobservable variable that conceptually quantifies one's interest on the survey topics. Such an assumption is reasonable if the survey topic is informed to the survey interviewees in the very beginning of the survey, which is the case with the 2012 Iowa Caucus Survey. Thus, we may assume that

$$(2.1) \quad \text{pr}(\delta_{1i} = 1 | x_i, y_{1i}, z_i) = \frac{\exp(\beta_0 + \beta'_1 x_i + \beta_2 z_i)}{1 + \exp(\beta_0 + \beta'_1 x_i + \beta_2 z_i)}$$

for some coefficient $(\beta_0, \beta_1, \beta_2)$, where δ_{1i} is the indicator function for element i to be in sample A_1 .

Now, as z_i is not observable, we consider an alternative model using an observed surrogate variable for z . Because we observe y_1 instead of z , a natural alternative model is

$$(2.2) \quad \pi_{1i}(\phi) = \text{pr}(\delta_{1i} = 1 | x_i, y_{1i}) = \frac{\exp(\phi_0 + \phi'_1 x_i + \phi_2 y_{1i})}{1 + \exp(\phi_0 + \phi'_1 x_i + \phi_2 y_{1i})},$$

for some (ϕ_0, ϕ_1, ϕ_2) . More generally, we can write $\pi_{1i}(\phi) = \pi(x_i, y_{1i}; \phi)$ for known function $\pi(\cdot)$ with unknown parameter $\phi = (\phi_0, \phi_1, \phi_2)$.

To estimate the parameters in (2.2), we subject the respondents of the first-phase sampling to similar survey questions and obtain a second respondent sample A_2 from A_1 . That is, we perform a two-phase sampling under the same response mechanism. The response model for A_2 is

$$(2.3) \quad \pi_{2i}(\phi^*) = \text{pr}(\delta_{2i} = 1 | x_i, y_{2i}, \delta_{1i} = 1) = \frac{\exp(\phi^*_0 + \phi'_1 x_i + \phi_2 y_{2i})}{1 + \exp(\phi^*_0 + \phi'_1 x_i + \phi_2 y_{2i})},$$

where δ_{2i} is the indicator function for element i to be in sample A_2 , y_{2i} is the measurement of Y at the time of selecting A_2 , and (ϕ'_1, ϕ_2) is defined in (2.2). Here, we allow the study item Y to be time-dependent; in other words, the value of Y can change over time. Thus, we assume that the conditional odds for the first-respondent selection and for the second-respondent selection are the same. Obtaining the second-respondent sample A_2 from A_1 is an experiment that we perform to understand the response mechanism of A_1 from A by asking the same

questions to the same people whose y -values are available. We may perform the experiment in the random subsample of A_1 in order to reduce the cost, but the subsampling does not make any difference in the resulting analysis. From the two-respondent sample, we are interested in estimating $\theta_1 = E(Y_1)$ and $\theta_2 = E(Y_2)$.

We now discuss parameter estimation for the propensity models. Note that we observe (x'_i, y_{1i}, y_{2i}) in A_2 . Thus, we can construct the following estimating equation to estimate the parameters in (2.3):

$$(2.4) \quad \sum_{i \in A_1} \omega_i \left\{ \frac{\delta_{2i}}{\pi_{2i}(\phi^*)} - 1 \right\} h_{1i} = 0,$$

where $\omega_i = \pi_i^{-1}$, $h_{1i} = (1, x'_i, y_{1i})'$. Once $\hat{\phi}^* = (\hat{\phi}_0^*, \hat{\phi}'_1, \hat{\phi}_2)'$ is computed, we can use

$$\sum_{i \in A_1} \frac{\omega_i}{\pi_{1i}(\phi_0, \hat{\phi}_1, \hat{\phi}_2)} = N$$

to estimate ϕ_0 . Equation (2.4) is a calibration equation in the second-phase respondent sample using h_{1i} as the control variable. Use of calibration for propensity score adjustment has been considered by Fuller, Loughin and Baker (1994), Kott (2006) and Kott and Chang (2010).

Once the parameters in (2.2) and (2.3) are estimated, we can use the following propensity-score-adjusted estimator:

$$(2.5) \quad \hat{\theta}_1 = \frac{1}{N} \sum_{i \in A_1} \omega_i \hat{\pi}_{1i}^{-1} y_{1i}$$

to estimate $\theta_1 = E(Y_1)$. Also, we can use

$$(2.6) \quad \hat{\theta}_2 = \frac{1}{N} \sum_{i \in A_2} \omega_i \hat{\pi}_{1i}^{-1} \hat{\pi}_{2i}^{-1} y_{2i}$$

to estimate $\theta_2 = E(Y_2)$. In addition, we may use the population-level information of x to improve the efficiency of the propensity-score-adjusted estimators, which will be presented in Section 4.

3. Main results. In this section we discuss some asymptotic properties of the proposed propensity-score-adjusted estimators. To discuss asymptotic properties of $\hat{\theta}_1$ in (2.5), we first define $\Phi = (\phi_0^*, \phi'_1, \phi_2, \phi_0)'$,

$$(3.1) \quad U_1(\Phi) \equiv \sum_{i \in A_1} \omega_i \left\{ \frac{\delta_{2i}}{\pi_{2i}(\phi_0^*, \phi_1, \phi_2)} - 1 \right\} (1, x'_i, y_{1i})' = (0, 0, 0)'$$

and

$$(3.2) \quad U_2(\Phi) \equiv \sum_{i \in A_1} \frac{\omega_i}{\pi_{1i}(\phi_0, \phi_1, \phi_2)} - N = 0.$$

Thus, equations (3.1) and (3.2) are a system of nonlinear equations that can be solved for Φ . We can write $U_c(\Phi)' = [U_1(\Phi)', U_2(\Phi)']$, and $(\hat{\theta}_1, \hat{\Phi})'$ can be ob-

tained as the solution to

$$U_p(\theta_1, \Phi) = 0, \quad U_c(\Phi) = 0,$$

where $U_p(\theta_1, \Phi) = N^{-1} \sum_{i \in A_1} \omega_i \{\pi_{1i}(\phi_0, \phi_1, \phi_2)\}^{-1} y_{1i} - \theta_1$. Because

$$E\{U_p(\theta_1^*, \Phi^*)\} = 0 \quad \text{and} \quad E\{U_c(\theta_1^*, \Phi^*)\} = 0,$$

where $(\theta_1^*, \Phi^*)'$ is the true parameter value, the solution $(\hat{\theta}_1, \hat{\Phi})'$ is consistent and has asymptotic variance

$$(3.3) \quad \text{var} \begin{pmatrix} \hat{\theta}_1 \\ \hat{\Phi} \end{pmatrix} \cong \begin{Bmatrix} -1 & E(\partial U_p / \partial \Phi) \\ 0 & E(\partial U_c / \partial \Phi) \end{Bmatrix}^{-1} \begin{Bmatrix} \text{var}(U_p) & \text{cov}(U_p, U_c) \\ \text{cov}(U_c, U_p) & \text{var}(U_c) \end{Bmatrix} \\ \times \left[\begin{Bmatrix} -1 & E(\partial U_p / \partial \Phi) \\ 0 & E(\partial U_c / \partial \Phi) \end{Bmatrix}' \right]^{-1}.$$

Using

$$\begin{bmatrix} -1 & E(\partial U_p / \partial \Phi) \\ 0 & E(\partial U_c / \partial \Phi) \end{bmatrix}^{-1} = \begin{bmatrix} -1 & E(\partial U_p / \partial \Phi) \{E(\partial U_c / \partial \Phi)\}^{-1} \\ 0 & \{E(\partial U_c / \partial \Phi)\}^{-1} \end{bmatrix},$$

then the asymptotic variance of $\hat{\theta}_1$ can be written, using the definition of U_p and U_c , as

$$\text{var}(\hat{\theta}_1) \cong \text{var} \left\{ U_p - E \left(\frac{\partial U_p}{\partial \Phi} \right) \left\{ E \left(\frac{\partial U_c}{\partial \Phi} \right) \right\}^{-1} U_c \right\} \\ = \text{var} \left\{ \hat{\theta}_1(\Phi) - E \left\{ \frac{\partial}{\partial \Phi} \hat{\theta}_1(\Phi) \right\} \begin{bmatrix} E\{\partial U_1(\Phi) / \partial \Phi\} \\ E\{\partial U_2(\Phi) / \partial \Phi\} \end{bmatrix}^{-1} U_c \right\},$$

where $\hat{\theta}_1(\Phi) = N^{-1} \sum_{i \in A_1} \omega_i y_{1i} \{1 + \exp(-\phi_0 - \phi'_1 x_i - \phi_2 y_{1i})\}$. Thus, the asymptotic variance can be written as

$$(3.4) \quad \text{var}(\hat{\theta}_1) \cong \frac{1}{N^2} V \left[\sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} y_{1i} - B_{1,y} \left\{ \sum_{i=1}^N \omega_i \delta_i \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} \right\} \right. \\ \left. - B_{2,y} \sum_{i=1}^N \left(\omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} - 1 \right) \right],$$

and

$$(B_{1,y}, B_{2,y}) = N \times E \left\{ \frac{\partial}{\partial \Phi} \hat{\theta}_1(\Phi) \right\} \begin{bmatrix} E\{\partial U_1(\Phi) / \partial \Phi\} \\ E\{\partial U_2(\Phi) / \partial \Phi\} \end{bmatrix}^{-1} \\ = \sum_{i=1}^N (1 - \pi_{1i}) y_{1i} (0, x'_i, y_{1i}, 1) \begin{pmatrix} \sum_{i=1}^N \pi_{1i} (1 - \pi_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i=1}^N (1 - \pi_{1i}) (0, x'_i, y_{1i}, 1) \end{pmatrix}^{-1},$$

where $h_{2i} = (1, x'_i, y_{2i})'$ and $0_{r \times 1}$ is the vector of zeros with dimension $r \times 1$, with $r = 2 + p$, and p is the dimension of x_i . Note that the variance (3.4) can be written as

$$(3.5) \quad \text{var}(\hat{\theta}_1) = \text{var} \left\{ \frac{1}{N} \sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} (y_{1i} - B_{2,y}) \right\} \\ + \text{var} \left\{ \frac{1}{N} \sum_{i=1}^N B_{1,y} \omega_i \delta_i \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} \right\}.$$

Roughly speaking, the first term in (3.5) is the asymptotic variance of the propensity-score-adjusted estimator when (ϕ'_1, ϕ_2) is known and the second term is the additional variance due to the fact that (ϕ'_1, ϕ_2) is estimated from the second-phase sample. Variance estimation is straightforward from (3.4), as we can replace the unknown parameters with their estimators.

We now discuss the asymptotic properties of $\hat{\theta}_2$ in (2.6), that is, the direct propensity-score-adjusted estimator of θ_2 . Using the argument similar to (3.4), we can obtain

$$(3.6) \quad \text{var}(\hat{\theta}_2) \cong \frac{1}{N^2} V \left[\sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i} \delta_{2i}}{\pi_{1i} \pi_{2i}} y_{2i} - D_{1,y} \left\{ \sum_{i=1}^N \omega_i \delta_i \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} \right\} \right. \\ \left. - D_{2,y} \sum_{i=1}^N \left(\omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} - 1 \right) \right],$$

where

$$(D_{1,y}, D_{2,y}) = N \times E \left\{ \frac{\partial}{\partial \Phi} \hat{\theta}_2(\Phi) \right\} \left[\begin{array}{c} E \{ \partial U_1(\Phi) / \partial \Phi \} \\ E \{ \partial U_2(\Phi) / \partial \Phi \} \end{array} \right]^{-1} \\ = \sum_{i=1}^N y_{2i} \{ (1 - \pi_{1i})(0, x'_i, y_{1i}, 1) + (1 - \pi_{2i})(1, x'_i, y_{2i}, 0) \} \\ \times \left(\begin{array}{c} \sum_{i=1}^N \pi_{1i} (1 - \pi_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i=1}^N (1 - \pi_{1i})(0, x'_i, y_{1i}, 1) \end{array} \right)^{-1}$$

and we used

$$\hat{\theta}_2(\Phi) = \frac{1}{N} \sum_{i \in A_2} \omega_i y_{2i} \{ 1 + \exp(-\phi_0 - \phi'_1 x_i - \phi_2 y_{1i}) \} \\ \times \{ 1 + \exp(-\phi_0^* - \phi'_1 x_i - \phi_2 y_{2i}) \}.$$

Writing

$$\frac{\delta_{1i}\delta_{2i}}{\pi_{1i}\pi_{2i}}y_{2i} = \frac{\delta_{1i}}{\pi_{1i}}y_{2i} + \frac{\delta_{1i}}{\pi_{1i}}\left(\frac{\delta_{2i}}{\pi_{2i}} - 1\right)y_{2i},$$

the asymptotic variance in (3.6) can be written as

$$\begin{aligned} \text{var}(\hat{\theta}_2) &\cong \frac{1}{N^2} \text{var} \left[\sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} (y_{2i} - D_{2,y}) \right] \\ (3.7) \quad &+ \frac{1}{N^2} \text{var} \left\{ \sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) (y_{2i} - D_{1,y} \pi_{1i} h_{1i}) \right\}. \end{aligned}$$

Thus, comparing (3.7) with (3.6), we note that $\hat{\theta}_2$ based on the A_2 sample does not necessarily have a larger variance than $\hat{\theta}_1$ that is computed from the first-phase sample A_1 . In fact, if y_{2i} is well approximated by h_{1i} , then the second term of the asymptotic variance in (3.7) is small and $\hat{\theta}_2$ is more efficient than $\hat{\theta}_1$.

Instead of using the direct estimator $\hat{\theta}_2$ in (2.6), we can use a two-phase regression estimator to improve efficiency. The estimator is efficient in that it incorporates auxiliary information obtained from the first-phase sampling. See [Hidiroglou and Särndal \(1998\)](#), [Legg and Fuller \(2009\)](#) and [Kim and Yu \(2011\)](#) for more details about two-phase regression estimators. In our setup, the data vector $h_{1i} = (1, x'_i, y_{1i})'$ is available for both A_1 and A_2 . Thus, the two natural estimators for the population mean $\bar{h}_{1N} = N^{-1} \sum_{i=1}^N h_{1i}$, $\hat{h}_{1,1} = N^{-1} \sum_{i \in A_1} \omega_i \hat{\pi}_{1i}^{-1} h_{1i}$ and $\hat{h}_{2,1} = N^{-1} \sum_{i \in A_2} \omega_i \hat{\pi}_{1i}^{-1} \hat{\pi}_{2i}^{-1} h_{1i}$ can be computed from A_1 and A_2 , respectively, and they are both approximately unbiased for \bar{h}_{1N} . Using $\hat{h}_{1,1}$ and $\hat{h}_{2,1}$, the two-phase regression estimator can be constructed by

$$(3.8) \quad \hat{\theta}_{2,\text{Reg}} = \hat{\theta}_2 - \hat{C}_{h_1} (\hat{h}_{2,1} - \hat{h}_{1,1}),$$

where

$$(3.9) \quad \hat{C}_{h_1} = \sum_{i \in A_2} \omega_i \hat{\pi}_{1i}^{-1} \hat{\pi}_{2i}^{-1} y_{2i} h'_{1i} \left\{ \sum_{i \in A_2} \omega_i \hat{\pi}_{1i}^{-1} \hat{\pi}_{2i}^{-1} h_{1i} h'_{1i} \right\}^{-1}.$$

Because $E(\hat{h}_{2,1} - \hat{h}_{1,1}) \cong 0$, the regression estimator in (3.8) is approximately unbiased, regardless of the choice of \hat{C}_{h_1} . By applying the linearization method to each term of (3.8), we can get

$$\begin{aligned} \hat{\theta}_{2,\text{Reg}} &\cong \frac{1}{N} \sum_{i=1}^N \left\{ \omega_i \delta_i \frac{\delta_{1i}\delta_{2i}}{\pi_{1i}\pi_{2i}} y_{2i} - D_{1i,\text{Reg}} \omega_i \delta_i \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} \right. \\ &\quad \left. - D_{2,\text{Reg}} \left(\omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} - 1 \right) \right\}, \end{aligned}$$

where $D_{1i,Reg} = D_{1,y} + C_{h_1}^* \pi_{1i}^{-1} - C_{h_1}^* (D_{1,h_1} - B_{1,h_1})$ and $D_{2,Reg} = D_{2,y} - C_{h_1}^* (D_{2,h_1} - B_{2,h_1})$ with

$$(B_{1,h_1}, B_{2,h_1}) = \sum_{i=1}^N (1 - \pi_{1i}) h_{1i}(0, x'_i, y_{1i}, 1) \times \left(\begin{matrix} \sum_{i=1}^N \pi_{1i} (1 - \pi_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i=1}^N (1 - \pi_{1i}) (0, x'_i, y_{1i}, 1) \end{matrix} \right)^{-1},$$

$$C_{h_1}^* = p \lim \widehat{C}_{h_1},$$

$$(D_{1,h_1}, D_{2,h_1}) = \sum_{i=1}^N h_{1i} \{ (1 - \pi_{1i}) (0, x'_i, y_{1i}, 1) + (1 - \pi_{2i}) (1, x'_i, y_{2i}, 0) \} \times \left(\begin{matrix} \sum_{i=1}^N \pi_{1i} (1 - \pi_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i=1}^N (1 - \pi_{1i}) (0, x'_i, y_{1i}, 1) \end{matrix} \right)^{-1}.$$

Thus, the asymptotic variance is

$$\begin{aligned} \text{var}(\widehat{\theta}_{2,Reg}) &\cong \frac{1}{N^2} \text{var} \left[\sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i} \delta_{2i}}{\pi_{1i} \pi_{2i}} y_{2i} - \left\{ \sum_{i=1}^N \omega_i \delta_i D_{1i,Reg} \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} \right\} \right. \\ &\quad \left. - D_{2,Reg} \sum_{i=1}^N \left(\omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} - 1 \right) \right] \\ &= \frac{1}{N^2} \text{var} \left[\sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} (y_{2i} - D_{2,Reg}) \right] \\ &\quad + \frac{1}{N^2} \text{var} \left[\sum_{i=1}^N \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) (y_{2i} - D_{1i,Reg} \pi_{1i} h_{1i}) \right]. \end{aligned}$$

REMARK 3.1. Instead of \widehat{C}_{h_1} in (3.9), the optimal choice of \widehat{C}_{h_1} that minimizes the variance among the class of regression estimators with a form specified by (3.8) is

$$(3.10) \quad \widehat{C}_{h_1,opt} = \widehat{\text{cov}}(\widehat{\theta}_2, \widehat{h}_{2,1} - \widehat{h}_{1,1}) \{ \widehat{\text{var}}(\widehat{h}_{2,1} - \widehat{h}_{1,1}) \}^{-1},$$

where

$$\begin{aligned} \widehat{\text{cov}}(\hat{\theta}_2, \hat{h}_{2,1} - \hat{h}_{1,1}) &\cong \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{2i}}{\hat{\pi}_{2i}^2} \left(\frac{y_{2i}}{\hat{\pi}_{1i}} - \widehat{D}_{1,y} h_{1i} \right) \hat{\eta}'_i \\ &\quad - \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}^2} \left(\frac{y_{2i}}{\hat{\pi}_{2i}} - \widehat{D}_{2,y} \right) \hat{\tau}' \\ &\quad + \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{3i}}{\pi_i} \frac{\hat{z}'_{4j}}{\pi_j}, \\ \widehat{\text{var}}(\hat{h}_{2,1} - \hat{h}_{1,1}) &\cong \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{2i}}{\hat{\pi}_{2i}^2} \hat{\eta}_i^{\otimes 2} \\ &\quad + \frac{1}{N^2} \sum_{i \in A_1} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}^2} \hat{\tau}^{\otimes 2} \\ &\quad + \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{4i}}{\pi_i} \frac{\hat{z}'_{4j}}{\pi_j}, \end{aligned}$$

where $M^{\otimes 2} = MM'$,

$$\begin{aligned} \hat{z}_{3i} &= \frac{\delta_{1i}}{\hat{\pi}_{1i}} \left\{ \frac{\delta_{2i}}{\hat{\pi}_{2i}} y_{2i} - \left(\frac{\delta_{2i}}{\hat{\pi}_{2i}} - 1 \right) \hat{\pi}_{1i} \widehat{D}_{1,y} h_{1i} - \widehat{D}_{2,y} \right\}, \\ \hat{z}_{4i} &= \frac{\delta_{1i}}{\hat{\pi}_{1i}} \left\{ \left(\frac{\delta_{2i}}{\hat{\pi}_{2i}} - 1 \right) (\hat{\pi}_{1i}^{-1} - \widehat{D}_{1,h_1} + \widehat{B}_{1,h_1}) \hat{\pi}_{1i} h_{1i} - (\widehat{D}_{2,h_1} - \widehat{B}_{2,h_1}) \right\} \end{aligned}$$

and $\hat{\eta}_i = h'_{1i} \hat{\pi}_{1i}^{-1} - (\widehat{D}_{1,h_1} - \widehat{B}_{1,h_1}) h'_{1i}$, $\hat{\tau} = \widehat{D}_{2,h_1} - \widehat{B}_{2,h_1}$ with

$$\begin{aligned} (\widehat{B}_{1,h_1}, \widehat{B}_{2,h_1}) &= \sum_{i \in A_1} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}} h_{1i} (0, x'_i, y_{1i}, 1) \\ &\quad \times \left(\frac{\sum_{i \in A_2} \omega_i \hat{\pi}_{2i}^{-1} (1 - \hat{\pi}_{2i}) h_{1i} h'_{2i}, 0_{r \times 1}}{\sum_{i \in A_1} \omega_i \hat{\pi}_{1i}^{-1} (1 - \hat{\pi}_{1i}) (0, x'_i, y_{1i}, 1)} \right)^{-1}, \\ (\widehat{D}_{1,h_1}, \widehat{D}_{2,h_1}) &= \sum_{i \in A_2} \omega_i \frac{h_{1i}}{\hat{\pi}_{1i} \hat{\pi}_{2i}} \{ (1 - \hat{\pi}_{1i}) (0, x'_i, y_{1i}, 1) + (1 - \hat{\pi}_{2i}) (1, x'_i, y_{2i}, 0) \} \\ &\quad \times \left(\frac{\sum_{i \in A_2} \omega_i \hat{\pi}_{2i}^{-1} (1 - \hat{\pi}_{2i}) h_{1i} h'_{2i}, 0_{r \times 1}}{\sum_{i \in A_1} \omega_i \hat{\pi}_{1i}^{-1} (1 - \hat{\pi}_{1i}) (0, x'_i, y_{1i}, 1)} \right)^{-1} \end{aligned}$$

and

$$\begin{aligned}
 (\widehat{D}_{1,y}, \widehat{D}_{2,y}) &= \sum_{i \in A_2} \omega_i \frac{y_{2i}}{\widehat{\pi}_{1i} \widehat{\pi}_{2i}} \{ (1 - \widehat{\pi}_{1i})(0, x'_i, y_{1i}, 1) + (1 - \widehat{\pi}_{2i})(1, x'_i, y_{2i}, 0) \} \\
 &\quad \times \left(\begin{array}{c} \sum_{i \in A_2} \omega_i \widehat{\pi}_{2i}^{-1} (1 - \widehat{\pi}_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i \in A_1} \omega_i \widehat{\pi}_{1i}^{-1} (1 - \widehat{\pi}_{1i})(0, x'_i, y_{1i}, 1) \end{array} \right)^{-1}.
 \end{aligned}$$

Such an estimator can be called a design-optimal regression estimator, as termed by Rao (1994).

REMARK 3.2. Model (2.1) can be viewed as a measurement error model in the sense that the true covariate z_i is not observed, but surrogate variables $y_{1i} = z_i + u_{1i}$ and $y_{2i} = z_i + u_{2i}$ are observed instead of z_i , where u_{1i} and u_{2i} are measurement errors associated with y_{1i} and y_{2i} , respectively. Assuming that the measurement errors follow a normal distribution, we can apply the propensity weighting method with error-prone covariates, using the recent approach of McCaffrey, Lockwood and Setodji (2013), to our two-phase sampling experiment.

Specifically, the measurement error model for obtaining the A_1 sample is given by (2.1) with $y_{1i} \sim N(z_i, \sigma_{u1}^2)$ and the measurement error model for obtaining the A_2 sample from A_1 sample is given by

$$\text{pr}(\delta_{2i} = 1 | x_i, y_{2i}, z_i, \delta_{1i} = 1) = \frac{\exp(\beta_0^* + \beta'_1 x_i + \beta_2 z_i)}{1 + \exp(\beta_0^* + \beta'_1 x_i + \beta_2 z_i)},$$

with $y_{2i} \sim N(z_i, \sigma_{u2}^2)$. It turns out that our proposed method is equivalent to the propensity weighting method under this measurement error model using the method of McCaffrey, Lockwood and Setodji (2013). More details can be found in Section B of the supplemental article [Chen and Kim (2014a, 2014b)].

4. Use of population auxiliary information. In this section we assume that population information $\bar{X}_N = \sum_{i \in U} x_i$ is available. In this case, we can apply the calibration techniques [Deville and Särndal (1992); Fuller (2002)] to provide external consistency of the resulting propensity-score-adjusted estimator to the known population mean \bar{X}_N . To incorporate both population and sample-level information, similar to Section 3, the regression estimator $\hat{\theta}_{1, \text{Reg}}$ of θ_1 can be written as

$$\begin{aligned}
 (4.1) \quad \hat{\theta}_{1, \text{Reg}} &= \hat{\theta}_1 - \widehat{B}_{\text{Reg}}(\hat{\theta}_{x,1} - \bar{X}_N) \\
 &\cong \hat{\theta}_1 - B_{\text{Reg}}(\hat{\theta}_{x,1} - \bar{X}_N),
 \end{aligned}$$

where $\hat{\theta}_1$ is defined in (2.5),

$$\hat{\theta}_{x,1} = N^{-1} \sum_{i \in A_1} \omega_i \widehat{\pi}_{1i}^{-1} x_i, \quad \widehat{B}_{\text{Reg}} = \sum_{i \in A_1} \omega_i \widehat{\pi}_{1i}^{-1} y_{1i} x'_i \left(\sum_{i \in A_1} \omega_i \widehat{\pi}_{1i}^{-1} x_i x'_i \right)^{-1}$$

and $B_{\text{Reg}} = p \lim \widehat{B}_{\text{Reg}}$. After ignoring the higher-order terms, it can be shown that

$$\hat{\theta}_{1,\text{Reg}} = \frac{1}{N} \sum_{i=1}^N \left\{ \omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} (y_{1i} - B_{\text{Reg}} x_i) - B_{1,\text{Reg}} \omega_i \delta_i \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} - B_{2,\text{Reg}} \left(\omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} - 1 \right) + B_{\text{Reg}} \bar{X}_N \right\},$$

where $B_{1,\text{Reg}} = B_{1,y} - B_{\text{Reg}} B_{1,x}$, $B_{2,\text{Reg}} = B_{2,y} - B_{\text{Reg}} B_{2,x}$,

$$(B_{1,x}, B_{2,x}) = \sum_{i=1}^N (1 - \pi_{1i}) x_i(0, x'_i, y_{1i}, 1) \left(\begin{array}{c} \sum_{i=1}^N \pi_{1i} (1 - \pi_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i=1}^N (1 - \pi_{1i}) (0, x'_i, y_{1i}, 1) \end{array} \right)^{-1}.$$

Therefore, the asymptotic variance can be estimated as follows:

$$\begin{aligned} \text{var}(\hat{\theta}_{1,\text{Reg}}) &= \frac{1}{N^2} \sum_{i \in A_1} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}^2} (y_{1i} - \widehat{B}_{\text{Reg}} x_i - \widehat{B}_{2,\text{Reg}})^2 \\ &+ \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{5i}}{\pi_i} \frac{\hat{z}_{5j}}{\pi_j} \\ &+ \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{2i}}{\hat{\pi}_{2i}^2} (\widehat{B}_{1,\text{Reg}} h_{1i})^2 \\ &+ \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{6i}}{\pi_i} \frac{\hat{z}_{6j}}{\pi_j}, \end{aligned} \tag{4.2}$$

where $\hat{z}_{5i} = \delta_{1i} \hat{\pi}_{1i}^{-1} (y_{1i} - \widehat{B}_{\text{Reg}} x_i - \widehat{B}_{2,\text{Reg}})$, $\hat{z}_{6i} = \delta_{1i} (\delta_{2i} \hat{\pi}_{2i}^{-1} - 1) \widehat{B}_{1,\text{Reg}} h_{1i}$, $\widehat{B}_{1,\text{Reg}} = \widehat{B}_{1,y} - \widehat{B}_{\text{Reg}} \widehat{B}_{1,x}$, $\widehat{B}_{2,\text{Reg}} = \widehat{B}_{2,y} - \widehat{B}_{\text{Reg}} \widehat{B}_{2,x}$,

$$\begin{aligned} (\widehat{B}_{1,x}, \widehat{B}_{2,x}) &= \sum_{i \in A_1} \omega_i \hat{\pi}_{1i}^{-1} (1 - \hat{\pi}_{1i}) x_i(0, x'_i, y_{1i}, 1) \\ &\times \left(\begin{array}{c} \sum_{i \in A_2} \omega_i \hat{\pi}_{2i}^{-1} (1 - \hat{\pi}_{2i}) h_{1i} h'_{2i}, 0_{r \times 1} \\ \sum_{i \in A_1} \omega_i \hat{\pi}_{1i}^{-1} (1 - \hat{\pi}_{1i}) (0, x'_i, y_{1i}, 1) \end{array} \right)^{-1}. \end{aligned}$$

In addition, we can consider a design-optimal regression estimator, as discussed in Remark 3.1, that incorporates all information in an optimal way. Specifically, the optimal regression estimator of θ_1 can be written as

$$\hat{\theta}_{1,\text{opt}} = \hat{\theta}_1 - \widehat{B}_{\text{opt}}(\hat{\theta}_{x,1} - \bar{X}_N), \tag{4.3}$$

where $\widehat{B}_{opt} = \widehat{cov}(\hat{\theta}_1, \hat{\theta}_{x,1}) \widehat{var}^{-1}(\hat{\theta}_{x,1})$, with

$$\begin{aligned} \widehat{cov}(\hat{\theta}_1, \hat{\theta}_{x,1}) &= \frac{1}{N^2} \sum_{i \in A_1} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}^2} \hat{\eta}_i^* + \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{2i}}{\hat{\pi}_{2i}^2} \widehat{B}_{1,y} h_{1i} (\widehat{B}_{1,x} h_{1i})' \\ &\quad + \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{7i}}{\pi_i} \frac{\hat{z}'_{8j}}{\pi_j}, \\ \widehat{var}(\hat{\theta}_{x,1}) &= \frac{1}{N^2} \sum_{i \in A_1} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}^2} (x_i - \widehat{B}_{2,x})^{\otimes 2} \\ &\quad + \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{2i}}{\hat{\pi}_{2i}^2} (\widehat{B}_{1,x} h_{1i})^{\otimes 2} \\ &\quad + \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{8i}}{\pi_i} \frac{\hat{z}'_{8j}}{\pi_j}, \end{aligned}$$

and

$$\begin{aligned} \hat{z}_{7i} &= \delta_{1i} \hat{\pi}_{1i}^{-1} \{y_{1i} - (\delta_{2i} \hat{\pi}_{2i}^{-1} - 1) \hat{\pi}_{1i} \widehat{B}_{1,y} h_{1i} - \widehat{B}_{2,y}\}, \\ \hat{z}_{8i} &= \delta_{1i} \hat{\pi}_{1i}^{-1} \{x_i - (\delta_{2i} \hat{\pi}_{2i}^{-1} - 1) \hat{\pi}_{1i} \widehat{B}_{1,x} h_{1i} - \widehat{B}_{2,x}\}, \end{aligned}$$

$\hat{\eta}_i^* = x_i' y_{1i} - y_{1i} \widehat{B}'_{2,x} - \widehat{B}_{2,y} x_i' + \widehat{B}_{2,y} \widehat{B}'_{2,x}$. $\widehat{B}_{1,x}$, $\widehat{B}_{1,y}$, $\widehat{B}_{2,x}$ and $\widehat{B}_{2,y}$ are defined in Section 3.

Now, the regression estimator of θ_2 can be written as

$$\begin{aligned} \hat{\theta}_{2,Reg} &= \hat{\theta}_2 - \widehat{B}_{1,Reg}^* (\hat{h}_{2,1} - \hat{h}_{1,1}) - \widehat{B}_{2,Reg}^* (\hat{\theta}_{x,2} - \bar{X}_N) \\ &= \hat{\theta}_2 - B_{1,Reg}^* (\hat{h}_{2,1} - \hat{h}_{1,1}) - B_{2,Reg}^* (\hat{\theta}_{x,2} - \bar{X}_N), \end{aligned}$$

where $\hat{\theta}_{x,2} = N^{-1} \sum_{i \in A_2} \omega_i \hat{\pi}_{1i}^{-1} \hat{\pi}_{2i}^{-1} x_i$. $(\widehat{B}_{1,Reg}^*, \widehat{B}_{2,Reg}^*)$ is the regression coefficient. It can be shown that

$$\begin{aligned} \hat{\theta}_{2,Reg} &= \frac{1}{N} \sum_{i=1}^N \left\{ \omega_i \delta_i \frac{\delta_{1i} \delta_{2i}}{\pi_{1i} \pi_{2i}} (y_{2i} - B_{2,Reg}^* x_i) - D_{1i,Reg}^* \omega_i \delta_i \delta_{1i} \left(\frac{\delta_{2i}}{\pi_{2i}} - 1 \right) h_{1i} \right. \\ (4.4) \quad &\quad \left. - D_{2,Reg}^* \left(\omega_i \delta_i \frac{\delta_{1i}}{\pi_{1i}} - 1 \right) + B_{2,Reg}^* \bar{X}_N \right\}, \end{aligned}$$

where

$$\begin{aligned} D_{1i,Reg}^* &= \{D_{1,y} + B_{1,Reg}^* (\pi_{1i}^{-1} - D_{1,h_1} + B_{1,h_1}) - B_{2,Reg}^* D_{1,x}\}, \\ D_{2,Reg}^* &= \{D_{2,y} - B_{1,Reg}^* (D_{2,h_1} - B_{2,h_1}) - B_{2,Reg}^* D_{2,x}\}, \end{aligned}$$

and

$$\begin{aligned}
 (D_{1,x}, D_{2,x}) &= \sum_{i=1}^N x_i \{ (1 - \pi_{1i})(0, x'_i, y_{1i}, 1) + (1 - \pi_{2i})(1, x'_i, y_{2i}, 0) \} \\
 &\quad \times \left(\begin{array}{c} N \\ \sum_{i=1} \pi_{1i}(1 - \pi_{2i})h_{1i}h'_{2i}, 0_{r \times 1} \\ N \\ \sum_{i=1} (1 - \pi_{1i})(0, x'_i, y_{1i}, 1) \end{array} \right)^{-1}.
 \end{aligned}$$

Also, similarly to (4.3), the optimal regression estimator of θ_2 can be written as

$$(4.5) \quad \hat{\theta}_{2,\text{opt}} = \hat{\theta}_2 - \hat{B}_{1,\text{opt}}^* (\hat{h}_{2,1} - \hat{h}_{1,1}) - \hat{B}_{2,\text{opt}}^* (\hat{\theta}_{x,2} - \bar{X}_N),$$

where

$$(\hat{B}_{1,\text{opt}}^*, \hat{B}_{2,\text{opt}}^*) = \widehat{\text{cov}}\{\hat{\theta}_2, (\hat{h}_{2,1} - \hat{h}_{1,1}, \hat{\theta}_{x,2})\} [\widehat{\text{var}}\{(\hat{h}_{2,1} - \hat{h}_{1,1}, \hat{\theta}_{x,2})\}]^{-1}.$$

$\widehat{\text{cov}}(\hat{\theta}_2, \hat{h}_{2,1} - \hat{h}_{1,1}), \widehat{\text{var}}(\hat{h}_{2,1} - \hat{h}_{1,1})$ are defined in (3.10),

$$\begin{aligned}
 \widehat{\text{cov}}(\hat{h}_{2,1} - \hat{h}_{1,1}, \hat{\theta}_{x,2}) &\cong \frac{1}{N^2} \sum_{i \in A_2} \omega_i \frac{1 - \hat{\pi}_{2i}}{\hat{\pi}_{2i}^2} \left(\frac{x_i}{\hat{\pi}_{1i}} - \hat{D}_{1,x} h_{1i} \right) \hat{\eta}'_i \\
 &\quad - \frac{1}{N^2} \sum_{i \in A_1} \omega_i \frac{1 - \hat{\pi}_{1i}}{\hat{\pi}_{1i}^2} (x_{2i} - \hat{D}_{2,x}) \hat{\tau}' \\
 &\quad + \frac{1}{N^2} \sum_{i \in A} \sum_{j \in A} \tilde{\Delta}_{ij} \frac{\hat{z}_{9i}}{\pi_i} \frac{\hat{z}'_{4j}}{\pi_j},
 \end{aligned}$$

where

$$\hat{z}_{9i} = \frac{\delta_{1i}}{\hat{\pi}_{1i}} \left\{ \frac{\delta_{2i}}{\hat{\pi}_{2i}} x_i - \left(\frac{\delta_{2i}}{\hat{\pi}_{2i}} - 1 \right) \hat{\pi}_{1i} \hat{D}_{1,x} h_{1i} - \hat{D}_{2,x} \right\},$$

$\widehat{\text{cov}}(\hat{\theta}_2, \hat{\theta}_{x,2})$ and $\widehat{\text{var}}(\hat{\theta}_{x,2})$ can be derived similarly.

5. Simulation study.

5.1. *Simulation one.* In simulation one, we performed a limited simulation study to test the performance of our proposed estimator and to perform a sensitivity analysis of the model assumptions. In the simulation study, we generated a finite population of size $N = 10,000$. In the population, we generated $(x_{1i}, x_{2i}, y_{1i}, y_{2i}, z_i)$, where

$$\begin{aligned}
 Z_i &= 0.5 + 0.5X_{1i} + 0.5X_{2i} + e_i, \\
 Y_{1i} &= Z_i + U_{1i}, \quad Y_{2i} = Z_i + U_{2i},
 \end{aligned}$$

$X_{1i}, X_{2i}, U_{1i}, U_{2i}$ and e_i are independently and identically distributed with $N(1, 1)$, $N(0, 1)$, $N(0, \sigma_1^2)$, $N(0, \sigma_2^2)$ with $\sigma_1 = \sigma_2 = 0.59$ and $\exp(1) - 1$, respectively. From the finite population, we repeatedly generated two-phase samples with approximate sample sizes $n_1 = 500$ and $n_2 = 300$ for the phase one and phase two samples, respectively. We consider the following response mechanisms for the first phase and second phase sampling indicators δ_{1i} and δ_{2i} :

(M1) *Linear Ignorable*

$$\pi_{1i} = \frac{\exp(\phi_0 + \phi_1 X_i)}{1 + \exp(\phi_0 + \phi_1 X_i)}, \quad \pi_{2i} = \frac{\exp(\phi_0^* + \phi_1 X_i)}{1 + \exp(\phi_0^* + \phi_1 X_i)},$$

where $(\phi_0, \phi_1, \phi_0^*) = (-3.2, 0.3, 0.2)$.

(M2) *Linear Nonignorable Nonmeasurement error*

$$\pi_{1i} = \frac{\exp(\phi_0 + \phi_1 X_i + \phi_2 Y_{1i})}{1 + \exp(\phi_0 + \phi_1 X_i + \phi_2 Y_{1i})},$$

$$\pi_{2i} = \frac{\exp(\phi_0^* + \phi_1 X_i + \phi_2 Y_{2i})}{1 + \exp(\phi_0^* + \phi_1 X_i + \phi_2 Y_{2i})},$$

where $(\phi_0, \phi_1, \phi_2, \phi_0^*) = (-3.4, 0.3, 0.1, 0.5)$.

(M3) *Complementary log-log Nonignorable Nonmeasurement error*

$$\pi_{1i} = 1 - \exp\{-\exp(\phi_0 + \phi_1 X_i + \phi_2 Y_{1i})\},$$

$$\pi_{2i} = 1 - \exp\{-\exp(\phi_0^* + \phi_1 X_i + \phi_2 Y_{2i})\},$$

where $(\phi_0, \phi_1, \phi_2, \phi_0^*) = (-3, 0.1, -0.1, -0.1)$.

(M4) *Probit Nonignorable Nonmeasurement error*

$$\pi_{1i} = \Phi(\phi_0 + \phi_1 X_i + \phi_2 Y_{1i}), \quad \pi_{2i} = \Phi(\phi_0^* + \phi_1 X_i + \phi_2 Y_{2i}),$$

where $(\phi_0, \phi_1, \phi_2, \phi_0^*) = (-2, 0.2, 0.2, 0.1)$.

(M5) *Linear Nonignorable Measurement error*

$$\pi_{1i} = \frac{\exp(\phi_0 + \phi_1 X_i + \phi_2 Z_i)}{1 + \exp(\phi_0 + \phi_1 X_i + \phi_2 Z_i)},$$

$$\pi_{2i} = \frac{\exp(\phi_0^* + \phi_1 X_i + \phi_2 Z_i)}{1 + \exp(\phi_0^* + \phi_1 X_i + \phi_2 Z_i)},$$

where $(\phi_0, \phi_1, \phi_2, \phi_0^*) = (-3.4, 0.3, 0.1, 0.5)$.

(M6) *Complementary log-log Nonignorable Measurement error*

$$\pi_{1i} = 1 - \exp\{-\exp(\phi_0 + \phi_1 X_i + \phi_2 Z_i)\},$$

$$\pi_{2i} = 1 - \exp\{-\exp(\phi_0^* + \phi_1 X_i + \phi_2 Z_i)\},$$

where $(\phi_0, \phi_1, \phi_2, \phi_0^*) = (-3, 0.1, -0.1, -0.1)$.

(M7) *Probit Nonignorable Measurement error*

$$\pi_{1i} = \Phi(\phi_0 + \phi_1 X_i + \phi_2 Z_i), \quad \pi_{2i} = \Phi(\phi_0^* + \phi_1 X_i + \phi_2 Z_i),$$

where $(\phi_0, \phi_1, \phi_2, \phi_0^*) = (-2, 0.2, 0.2, 0.1)$.

We used $B = 2000$ Monte Carlo sample size. The “working” model for the propensity score estimation is the Linear Nonignorable model (M2). From each sample, we computed the following four estimators for $\theta_1 = E(Y_1)$:

- (1) Naive: Calibration estimator which assumes ignorable missing mechanism;
- (2) PS: Proposed propensity score estimator, as defined in (2.5);
- (3) REG: Proposed regression estimator, as defined in (4.1); and
- (4) OPT: Proposed optimal estimator, as defined in (4.3).

We also computed the following five estimators for $\theta_2 = E(Y_2)$:

- (1) Naive: Calibration estimator which assumes ignorable missing mechanism;
- (2) PS: Proposed propensity score estimator, as defined in (2.6);
- (3) REG: Proposed regression estimator by incorporating first-phase sample information, as defined in (3.8);
- (4) OPT1: Proposed optimal estimator by incorporating first-phase sample information, as defined in Remark 3.1; and
- (5) OPT2: Proposed optimal estimator by incorporating both first-phase sample and population information, as defined in (4.5).

The simulation results for point and variance estimations are given in Tables 1 for models (M1)–(M4) and 2 for models (M5)–(M7). Specifically, we calculated the Biases, Standard Errors (SE), Root Mean Squared Errors (RMSE) of the point estimators and Relative Bias (RB) of the proposed variance estimators. Under models (M1) and (M2), the proposed estimators show negligible biases, which confirms our theory. Furthermore, the proposed estimators show modest biases even under models (M3)–(M7) where the assumed response model is not equal to the true response model. To investigate the effect of using incorrect response models, we made plots of $1/\hat{\pi}_i$ on $1/\pi_i$ under four different response models (M1)–(M4), where $\hat{\pi}_i$ are the fitted values of the response probabilities under the working model and π_i are the true response probabilities. In Figure 1, the plot under model (M3) shows that most of the sample observations are located above the line of $y = x$, which suggests that many observations are assigned to bigger propensity weights ($1/\hat{\pi}_i$) than necessary. Thus, the resulting PS estimator can be positively biased, as confirmed in Table 1. On the other hand, the plot under model (M4) shows the opposite phenomenon and the resulting estimator is negatively biased. According to the plots, we find that the fitted values are highly correlated with the true values even under the wrong models. Thus, the bias of the PS estimators is also modest under (M3)–(M4). Similar results have been found for (M5)–(M7). The regression estimator and the optimal estimator are more efficient

TABLE 1
Simulation results of the point estimators and variance estimators under models (M1)–(M4) for simulation one

Model	Parameter	Method	Bias	SE	RMSE	RB
(M1)	θ_1	Naive	-0.0029	0.0751	0.0751	N/A
		PS	0.0071	0.1647	0.1648	0.0363
		REG	0.0108	0.1622	0.1625	0.0160
		OPT	0.0077	0.1556	0.1557	0.0543
	θ_2	Naive	-0.0034	0.0907	0.0908	N/A
		PS	0.0069	0.1559	0.1560	0.0342
		REG	0.0072	0.1584	0.1586	0.0123
		OPT1	0.0074	0.1582	0.1584	-0.0153
		OPT2	0.0082	0.1496	0.1498	-0.0182
(M2)	θ_1	Naive	0.1662	0.0838	0.1861	N/A
		PS	-0.0026	0.1786	0.1786	-0.0093
		REG	-0.0013	0.1708	0.1709	0.0034
		OPT	-0.0001	0.1670	0.1670	0.0118
	θ_2	Naive	0.1857	0.0954	0.2088	N/A
		PS	0.0007	0.1645	0.1644	-0.0217
		REG	0.0002	0.1656	0.1656	-0.0160
		OPT1	0.0022	0.1633	0.1633	-0.0294
		OPT2	0.0030	0.1524	0.1524	-0.0238
(M3)	θ_1	Naive	-0.1578	0.0721	0.1735	N/A
		PS	0.0712	0.1957	0.2083	-0.0077
		REG	0.0910	0.1963	0.2164	-0.0316
		OPT	0.0777	0.1846	0.2003	0.0283
	θ_2	Naive	-0.2137	0.0843	0.2297	N/A
		PS	0.0490	0.1795	0.1860	0.0215
		REG	0.0546	0.1889	0.1966	-0.0849
		OPT1	0.0420	0.1833	0.1880	-0.0506
		OPT2	0.0523	0.1759	0.1835	-0.0506
(M4)	θ_1	Naive	-0.2593	0.0671	0.2678	N/A
		PS	-0.0325	0.1822	0.1850	0.0036
		REG	-0.0830	0.1714	0.1904	0.0833
		OPT	-0.0707	0.1701	0.1842	0.0266
	θ_2	Naive	-0.2689	0.0765	0.2795	N/A
		PS	-0.0244	0.1544	0.1563	0.0823
		REG	-0.0180	0.1678	0.1688	-0.0914
		OPT1	-0.0242	0.1630	0.1648	-0.0549
		OPT2	-0.0607	0.1583	0.1695	-0.0945

than the PS estimator, and the optimal estimator has the smallest variance, which is consistent with the theory. The PS estimator of θ_2 is more efficient than that of θ_1 since y_{2i} is well approximated by y_{1i} , which is a part of h_{1i} when computing

TABLE 2
Simulation results of the point estimators and variance estimators under models (M5)–(M7) for simulation one

Model	Parameter	Method	Bias	SE	RMSE	RB
(M5)	θ_1	Naive	0.1242	0.0794	0.1474	N/A
		PS	-0.0312	0.1788	0.1814	-0.0147
		REG	-0.0278	0.1707	0.1729	-0.0236
		OPT	-0.0270	0.1668	0.1690	-0.0055
	θ_2	Naive	0.1649	0.0911	0.1884	N/A
		PS	-0.0037	0.1620	0.1620	0.0001
		REG	-0.0049	0.1648	0.1648	-0.0150
		OPT1	-0.0014	0.1632	0.1632	-0.0364
		OPT2	0.0007	0.1525	0.1525	-0.0412
(M6)	θ_1	Naive	-0.1269	0.0725	0.1462	N/A
		PS	0.1129	0.1993	0.2290	0.0032
		REG	0.1309	0.2006	0.2396	-0.0517
		OPT	0.1196	0.1914	0.2256	-0.0006
	θ_2	Naive	-0.1926	0.0838	0.2100	N/A
		PS	0.0787	0.1863	0.2023	0.0008
		REG	0.0831	0.1918	0.2090	-0.0624
		OPT1	0.0757	0.1875	0.2023	-0.0437
		OPT2	0.0843	0.1797	0.1985	-0.0464
(M7)	θ_1	Naive	-0.1922	0.0660	0.2032	N/A
		PS	0.0356	0.1705	0.1742	0.0287
		REG	-0.0174	0.1635	0.1644	0.0847
		OPT	-0.0002	0.1664	0.1664	0.0006
	θ_2	Naive	-0.2526	0.0771	0.2641	N/A
		PS	0.0005	0.1626	0.1626	0.0240
		REG	0.0017	0.1626	0.1626	0.0128
		OPT1	-0.0017	0.1630	0.1630	-0.0138
		OPT2	-0.0375	0.1579	0.1623	-0.0399

the model parameters. Variance estimators show negligible relative biases in most cases. The simulation study suggests that the proposed estimator is robust against the failure of the assumed response models.

5.2. *Simulation two.* In this simulation study, we consider only model (M5) Linear Nonignorable Measurement error. In order to test the sensitivity of model misspecification of equal coefficients for two-phase response mechanisms, we perform simulation studies by using the following response mechanisms:

$$\pi_{1i} = \frac{\exp(\phi_0 + \phi_1 x_{1i} + \phi_2 z_i)}{1 + \exp(\phi_0 + \phi_1 x_{1i} + \phi_2 z_i)}, \quad \pi_{2i} = \frac{\exp(\phi_0^* + \phi_1 x_{1i} + \phi_2^* z_i)}{1 + \exp(\phi_0^* + \phi_1 x_{1i} + \phi_2^* z_i)},$$

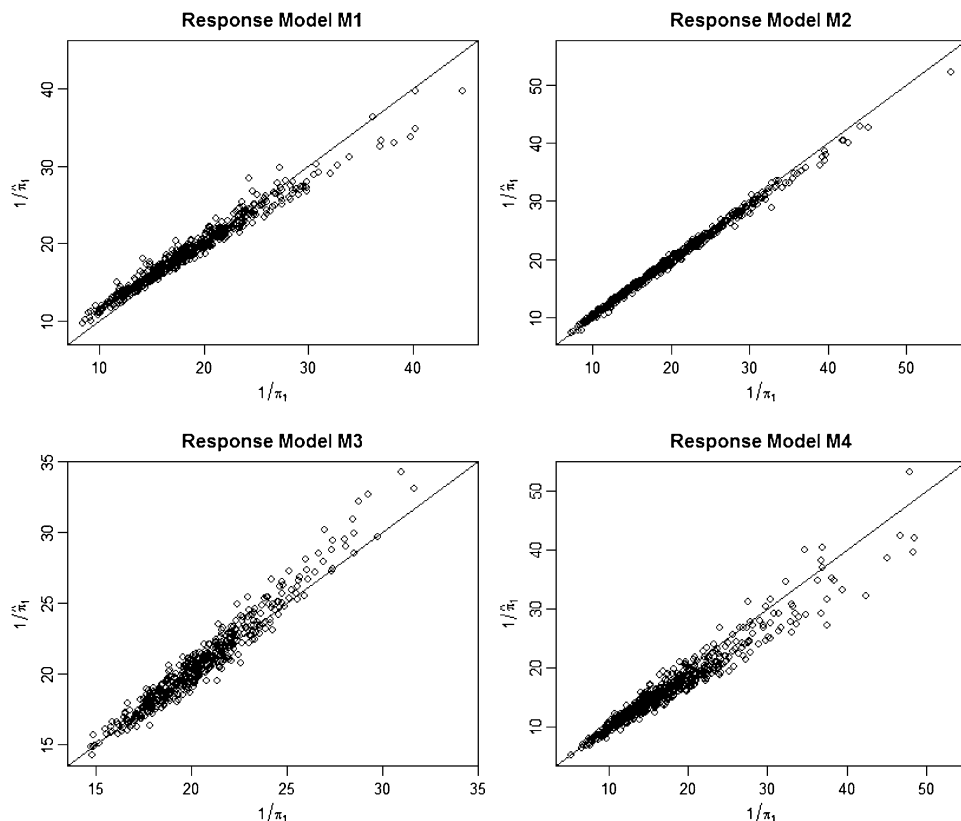


FIG. 1. Plots of the fitted values on the true value of the inverse response probability under models (M1)–(M4).

where $(\phi_0, \phi_1, \phi_2, \phi_0^*, \phi_2^*) = (-3.4, 0.3, 0.1 + d, 0.5, 0.1)$. Specifically, we consider the following three cases:

- (C1) Small Difference: $d = 0.01$.
- (C2) Medium Difference: $d = 0.05$.
- (C3) Big Difference: $d = 0.1$.

Other setups of simulation two are the same as that for simulation one. The results are presented in Table 3. According to Table 3, the biases for all the proposed estimators increase when the discrepancy parameter d increases, but the biases are still very modest. The variance estimators show very small relative biases, which confirms the stability of the variance estimators. Other patterns of the results are similar to that for simulation one.

6. Empirical study. The proposed two-phase propensity score estimator is applied to the data obtained from the 2012 Iowa Caucus Survey (ICS). The Iowa

TABLE 3

Simulation results of the point estimators and variance estimators under model (M5) for simulation two

Model	Parameter	Method	Bias	SE	RMSE	RB
(C1)	θ_1	Naive	0.1426	0.0837	0.1653	N/A
		PS	-0.0199	0.1731	0.1742	0.0228
		REG	-0.0213	0.1627	0.1641	0.0279
		OPT	-0.0194	0.1607	0.1618	0.0281
	θ_2	Naive	0.1852	0.0929	0.2071	N/A
		PS	0.0066	0.1607	0.1608	0.0080
		REG	0.0059	0.1627	0.1628	0.0026
		OPT1	0.0076	0.1605	0.1607	-0.0099
		OPT2	0.0064	0.1486	0.1487	-0.0071
(C2)	θ_1	Naive	0.2043	0.0802	0.2194	N/A
		PS	0.0384	0.1726	0.1768	-0.0213
		REG	0.0239	0.1609	0.1626	0.0157
		OPT	0.0295	0.1601	0.1628	-0.0048
	θ_2	Naive	0.2457	0.0892	0.2614	N/A
		PS	0.0610	0.1597	0.1709	-0.0182
		REG	0.0599	0.1611	0.1718	-0.0168
		OPT1	0.0628	0.1602	0.1720	-0.0427
		OPT2	0.0529	0.1480	0.1572	-0.0273
(C3)	θ_1	Naive	0.2992	0.0797	0.3096	N/A
		PS	0.1093	0.1678	0.2002	-0.0221
		REG	0.0763	0.1605	0.1777	-0.0131
		OPT	0.0887	0.1597	0.1826	-0.0446
	θ_2	Naive	0.3533	0.0931	0.3654	N/A
		PS	0.1357	0.1566	0.2072	-0.0078
		REG	0.1353	0.1587	0.2085	-0.0115
		OPT1	0.1374	0.1573	0.2089	-0.0355
		OPT2	0.1158	0.1498	0.1893	-0.0644

political party caucuses are a significant component of the presidential candidate selection process. In 2011, two caucus polls were conducted to be implemented prior to the January 2012 Iowa Republican Caucus. In the first poll, approximately 1200 registered Republicans and Independents (no party) were interviewed in November 2011. The second poll was a follow-up conducted in December 2011 with the November 2011 respondents to identify changes in their voting preferences.

The sampling frame for the November 2011 poll was constructed from the Iowa voter registry provided by the Iowa Secretary of State. The telephone numbers on the list were reported by voters at the time of their registration and therefore included both landlines and cell phone numbers. A stratified systematic sampling

design was used to select the initial sample. Five variables were used to create strata or sorting variables to ensure spread across the range of variation in age, voter activity, geography, gender and party affiliation. One indicator variable was created to differentiate voters 35 years or above from younger voters, and a second indicator variable defined whether a voter had attended one or more of the previous five primaries. Three additional variables used in designing the sample were congressional district, registered party and gender.

Strata were defined by party affiliation, congressional district, the age indicator and the prior primary attendance indicator. Within parties, sample size allocation incorporated an oversampling of primary attendees to maximize the chances of reaching likely caucus attendees. Sample allocation across the remaining strata was defined in proportion to the number of voters in each stratum. The stratified design was implemented using a systematic probability proportional to size selection scheme. The size measure was based on the relative proportion of voters in each stratum. For each party list, the systematic selection scheme was applied to a list of voters sorted by congressional district, age indicator, previous primary attendance indicator and gender.

A sample of 9000 voters was selected for the November 2011 poll, consisting of 6000 Republicans and 3000 Independents. Telephone numbers were unavailable for 836 of the sampled voters. The remaining 8164 sample households were contacted. Excluding 190 noneligible numbers, 1256 registered voters were finally interviewed from the November poll, which resulted in a 15.8 percent response rate. The November survey of registered Republicans and Independents contained questions related to anticipated caucus attendance, candidates of choice and opinions on candidate characteristics, as well as demographic and background items. In the December 2011 poll, 1256 respondents from the November poll were contacted again for a follow-up survey and 940 interviews were completed, leading to a 74.9 percent response rate. Figure 2 summarizes the two-phase sampling structure of the 2012 Iowa Caucus Survey.

To apply our proposed method to the ICS data, let Y be the reported value of the “First Choice” candidate. After preliminary analysis, we decided to use $X = (\text{Party}, \text{Age})$ as the auxiliary variable in the propensity model. The auxiliary variable has a known total at the population level and is also related to the survey participation rate. The population size is $N = 1,315,981$. Denote DY_1 and DY_2 as

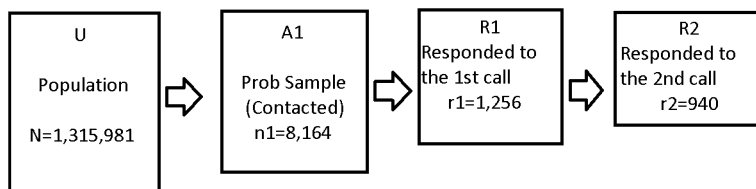


FIG. 2. Sample structure of 2012 Iowa Caucus Survey.

the dummy variables of “First Choice” based on the first sample A_1 and the second sample A_2 , and let DX be the dummy variable based on X . Then the parameters of interest are

$$\theta_1 = \frac{\sum_{i \in U} Z_i DY_{1i}}{\sum_{i \in U} Z_i}$$

and

$$\theta_2 = \frac{\sum_{i \in U} Z_i DY_{2i}}{\sum_{i \in U} Z_i},$$

where Z_i is the indicator of “Caucus Attendance” for unit i . That is, $Z_i = 1$ if “Caucus Attendance = Definitely attend” or “Caucus Attendance = Likely to attend.” The outcome of the Iowa Caucus on January 3, 2012 is

$$(6.1) \quad \theta_0 = (24.5\%, 10.3\%, 21.4\%, 43.7\%)$$

for “First Choice” candidate: Romney, Perry, Paul, Others. Note that our parameters θ_1 and θ_2 are not necessarily equal to θ_0 , although they may be close for certain candidates.

The propensity model used for the proposed estimator is

$$(6.2) \quad \pi_{1i}(\phi) = \frac{\exp(\phi_0 + \phi'_1 DX_i + \phi'_2 DY_{1i})}{1 + \exp(\phi_0 + \phi'_1 DX_i + \phi'_2 DY_{1i})}$$

and

$$(6.3) \quad \pi_{2i}(\phi^*) = \frac{\exp(\phi_0^* + \phi'_1 DX_i + \phi'_2 DY_{2i})}{1 + \exp(\phi_0^* + \phi'_1 DX_i + \phi'_2 DY_{2i})},$$

where $DX_i = (DX_{1i}, DX_{2i})'$, $DY_{1i} = (DY_{11i}, DY_{12i}, DY_{13i}, DY_{14i}, DY_{15i})'$ and $DY_{2i} = (DY_{21i}, DY_{22i}, DY_{23i}, DY_{24i}, DY_{25i})'$. Using the proposed methods in Section 3, we obtain parameter estimates for the selection model. The estimated parameters are given in Table 4. Table 4 shows that variables DX_1 , DX_2 and DY_{11} have significant effects on the selection mechanisms, which supports our model for nonignorable sample selection.

We consider three estimators for estimating θ_t for $t = 1, 2$: (i) the naive estimator (Naive) based on the respondents, computed by $\hat{\theta}_{tN} = \sum_{i \in A_t} Z_i DY_{ti} /$

TABLE 4
Estimated coefficients in the propensity model

Coefficient	Age	Party	Romney	Perry	Paul	Others
Est	0.588	0.782	0.991	0.454	0.866	1.307
SE	0.266	0.251	0.454	0.663	0.841	0.985
<i>t</i> -value	2.211	3.116	2.183	0.685	1.030	1.327

TABLE 5
Estimated parameters (s.e.) for 2012 Iowa Caucus Survey results

Survey	Method	Romney	Perry	Paul	Others
November	Naive	0.340	0.108	0.130	0.422
	Ignorable	0.316	0.103	0.146	0.435
	Proposed	0.303 (0.062)	0.106 (0.039)	0.093 (0.107)	0.499 (0.046)
December	Naive	0.281	0.140	0.131	0.448
	Ignorable	0.270	0.144	0.148	0.437
	Proposed	0.244 (0.043)	0.134 (0.026)	0.112 (0.046)	0.509 (0.036)

Standard errors are in parentheses.

$(\sum_{i \in A_t} Z_i)$; (ii) the ignorable-response estimator (Ignorable), computed by $\hat{\theta}_{iIE} = \sum_{i \in A_t} \omega_{ti} Z_i DY_{ti} / (\sum_{i \in A_t} \omega_{ti} Z_i)$, where ω_{ti} is the propensity score obtained by assuming the ignorable adjustment weight which is obtained by setting $\phi_2 = 0$ in the sample selection model; and (iii) the proposed propensity score estimator using nonignorable sample selection models in (6.2) and (6.3). The proposed propensity score estimators are computed by (2.5) and (2.6).

The results for point estimation are given in Table 5. The proposed estimates are closer to the Iowa Caucus results in (6.1) than the other estimates for Romney and Perry. Furthermore, the proposed method enables us to compute the estimated standard errors of the point estimates using the theory discussed in Section 3. The estimated standard errors in the December 2011 survey estimates are smaller than those in the November 2011 survey estimates, which is consistent with our findings in Section 5. However, the estimates for Paul and Others are further away from the reported true values compared to other estimators, which are not that encouraging. It may be due to the uncontrolled time effect.

7. Concluding remarks. Estimators from self-selected samples can suffer from selection bias. Propensity score weighting using demographic variables can reduce selection bias, but the bias may remain important if survey participation depends on the study variable itself. We make assumptions about the selection mechanism that explicitly include the study variable in the selection model. To estimate the model parameters, we propose obtaining a second survey from the original self-selected sample. If the second survey has questions similar to the first one, we may assume that the regression coefficients for the explanatory variables in the propensity model are the same as for the original sample. The propensity model is then identified and the model parameters can be estimated using a generalized method of moments. The proposed method also permits estimation of the standard errors of the estimated parameters.

As mentioned in Remark 3.2, our proposed approach is equivalent to the measurement error model approach of McCaffrey, Lockwood and Setodji (2013) for propensity score weighting. Also, two limited simulation studies in Section 5 suggest that the proposed method is robust against the failure of the assumed response models and individual-level heterogeneity in the propensity to respond that persists over time. The proposed estimators have modest biases even when the equality of coefficients for the two response mechanisms violate in a certain range.

The proposed method provides a useful tool for analyzing voluntary samples as well as nonignorable nonresponse problems for survey data and, in particular, web-based panel surveys. In a panel survey, the same sample can be contacted several times and the proposed two-phase estimation approach can be extended to multiphase estimation. This is a topic of future study.

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SUPPLEMENTARY MATERIAL

Supplement Derivations: Supplement Derivations for Sections 3 and 4 (DOI: [10.1214/14-AOAS746SUPPA](https://doi.org/10.1214/14-AOAS746SUPPA); .pdf). Details of derivations for variances and variance estimators in Sections 3 and 4.

Supplement Justifications: Supplement Justifications for Remark 3.2 (DOI: [10.1214/14-AOAS746SUPPB](https://doi.org/10.1214/14-AOAS746SUPPB); .pdf). Details of justifications for Remark 3.2.

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