Ultrawideband Frequency-Selective Absorber Designed with an Adjustable and Highly Selective Notch

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Keywords
tunable notch, frequency-selective absorber (FSA), RCS reduction, equivalent circuit model (ECM)

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Ultrawideband Frequency-Selective Absorber Designed with an Adjustable and Highly Selective Notch

Yuxuan Ding, Mengyao Li, Jianxun Su, Member, IEEE, Qingxin Guo, Senior Member, IEEE, Hongcheng Yin, Zengrui Li, Member, IEEE, and Jiming Song, Fellow, IEEE

Abstract—In this paper, the working mechanism of a wideband absorber designed with an adjustable and highly selective notch band is studied, in which the narrow notch band is independently controlled by the lower lossless layer of the absorber, while the upper lossy layer loaded with lumped resistors realizes absorption. We present two instances with geometrically controlled and electrically controlled notch bands, respectively. Without decreasing absorption performance, the notch position can be flexibly adjusted throughout the entire frequency band by simply modifying the dimension of the lossless frequency-selective surface (FSS) or changing the capacitance of the varactor, i.e., using geometric control or electrical control. The narrow notch band allows two wide absorption bands to be retained on both sides; therefore, good stealth performance is still guaranteed. Equivalent circuit models (ECM) are proposed to further explain the principle. The frequency-domain simulation, ECM, time-domain simulation, and experimental results are in good agreement and validate the adjustability and high selectivity of the notched absorbers. At the end of this paper, an FSA-backed monopole antenna is simulated and measured, which clearly illustrates that these FSAs can serve as the ground plane for antennas and realize out-of-band RCS reduction.

Index Terms—tunable notch, frequency-selective absorber (FSA), RCS reduction, equivalent circuit model (ECM)

I. INTRODUCTION

ABSORBERS are widely used in stealth technology, RCS reduction, radomes, electromagnetic shielding, and many other applications that may reduce or selectively reduce reflection or transmission of electromagnetic waves. Research on absorbers began in 1952 when the first absorber was proposed by Salisbury [1] with a quarter-wavelength thickness, which utilizes the λ/2 path difference between the incident wave and the return wave to achieve mutual cancellation. A Salisbury absorber is characterized by its simple principle, whereas it suffers from limited bandwidth. Multilayered Salisbury screen (Jaumann absorber [2]) is one solution to improve bandwidth; however, stacked layers end with a large thickness. The wedge-tapered absorber [3] proposed in 1971 showed the best absorption while also having a cumbersome structure.

Circuit analog absorber [4], which was proposed around the turn of this century, achieved a wider frequency response while maintaining a lightweight. Instead of homogeneous resistive sheets, band-stop FSSs were applied to absorbers, which were modeled by series RLC components. FSSs can be divided into conductive FSSs (lossless FSSs) and resistive FSSs (lossy FSSs). When applied to absorbers, lossy FSSs are either made using resistive sheets [5] or loading lumped resistors [6]. Employing multiple resonances, single-layer wideband absorbers were implemented with a rather thin structure. Recently, there have also been some novel absorber designs, such as adopting the combination of plasma and resistive FSS [7], fractal FSS [8], and absorbers on the base of a magnetic substrate and FSS [9]. As we can see, however, no matter how innovative the designs, they are most often combined with FSSs.

At present, the demand for absorbers mainly lies in slimmer and lighter structures, broader bands, and better absorption effects. At the same time, for different application scenarios, such as radomes, in addition to the absorption performance, there are also needs for allowing electromagnetic waves to transmit through the radomes in the operation band without distorting the radiation performance of the antennas. These are the so-called frequency-selective absorbers (FSA) [10] that generate a transmission band [11], [12] on the basis of a wideband absorber. Additionally, notched absorbers [13], [14] that can be used as antennas’ ground plane, serving as an FSS reflector, are designed to realize low-RCS antennas, which are another type of FSA, or more specifically, absorptive frequency-selective reflector (AFSR).

The design of a reflection band, either narrow or wideband, between two absorptive bands is not challenging work, if both the lossy and lossless FSSs are tuned simultaneously. However, realizing a reconfigurable and narrow reflective band with low insertion loss by merely tuning the lossless FSS is a considerable challenge.

In this paper, we first derived a theoretical formula based on transmission line theory to indicate that the notch can be flexibly tuned by only adjusting the lossless layer. The absorption and reflection mechanism of the proposed FSS...
absorbers is shown in Fig. 1. Our research showed that the absorption band \((f_{L1} \sim f_{H2})\) and the notch \(f_N\) can be controlled independently by the lossy layer and lossless layer, respectively. The independent design of the lossy layer and the lossless layer greatly simplifies the design process of the FSA with a dynamically tunable and highly selective notch. High selectivity (narrow reflection band) can guarantee two wide absorptive bands \((f_{L1} \sim f_{H1} \text{ and } f_{L2} \sim f_{H2})\), which can ensure good Stealth performance. In most previous publications, the bandwidth of two absorption bands is limited. The dynamically tunable notch can better meet wideband antenna application. Both cases for electrically and geometrically tunable notches are provided for different application scenarios.

The remainder of this paper is organized as follows. In Section II, the rationale for the independently regulated notch-band is analyzed. The modeling and performance of two absorbers with geometrically and electrically adjustable notches are detailed in Section III separately. In Section IV, taking the geometrically controlled notch absorber as an example, the numerical solution of impedance conditions for the metal-backed band-notched absorber is derived based on the general equivalent circuit model (ECM). Strict ECs are calculated in Section V. The fabricated and measured prototypes are described in Section VI, and one application scenario of our proposed FSA serving as a monopole’s ground plane is given with a time-domain simulation and actual measurement results. Section VII provides concluding remarks.

II. DERIVATION OF THE NOTCH-BAND CONTROL PRINCIPLE

As we know, an infinite periodic structure in free space can be seen as a space filter of electromagnetic waves, which is equivalent to a two-port network [15]. The free space and substrates are equivalent to transmission lines of corresponding electrical length with characteristic impedance \(Z_0 = 120\pi \ \Omega\) and \(Z_1 = Z_0/\sqrt{\varepsilon_r}\), respectively. The metal-backed substrate is equivalent to short-circuited transmission lines. The general ECM for a metal-backed notched absorber is shown in Fig. 2. Each FSS layer is equivalent to a shunt impedance in the circuit, where \(Z_R = R_R + jX_R\) and \(Z_F = jX_F\) denote the equivalent impedance of the lossy FSS and lossless FSS, respectively. The coupling effect between the lossless FSS and the metal ground is represented by \(C_T\).

To further analyze the reflection mechanism and the regulating principle of the notch band, we derive a simplified circuit of the notch absorber. For the sake of simplicity, the equivalent electrical length from Port 1 to the lossless FSS layer is approximately expressed as a total \(t_N \approx t_1\sqrt{\varepsilon_r} + t_5\), and the lossless FSS as well as the supporting substrate and the metal ground are considered together as a reactive load of \(Z_N = jX_N\) (see the red dotted boxes in Fig. 2). Therefore, the transfer matrix can be simplified as follows:

\[
\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 1/Z_R & 1 \end{bmatrix} \begin{bmatrix} \cos \delta_N & jZ_0 \sin \delta_N \\ jZ_0 \sin \delta_N & \cos \delta_N \end{bmatrix}
\]

\[
= \begin{bmatrix} \cos \delta_N & jZ_0 \sin \delta_N \\ \cos \delta_N + jZ_0 \sin \delta_N & \cos \delta_N + jZ_0 \sin \delta_N \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 1/Z_R & 1 \end{bmatrix} \begin{bmatrix} \cos \delta_N & jZ_0 \sin \delta_N \\ jZ_0 \sin \delta_N & \cos \delta_N \end{bmatrix},
\]

where \(\delta_N = \beta t_N = (2\pi t_N/c)f\) is the total phase path between lossy FSS and lossless FSS.

The reflection coefficient at the notch frequency is calculated as follows:

\[
|S_{11}| = \left| \frac{\Delta Z_N + B - C Z_N Z_F - D Z_F}{\Delta Z_N + B + C Z_N Z_F + D Z_F} \right| = 1.
\]

It should be mentioned that the absorption rate is calculated as \(1 - |S_{11}|^2\) with \(S_{21} = 0\) for the metal-backed absorbers throughout the whole discussion.

The complete expression of (2) is shown at the bottom of this page. The analytical solution to \(X_N\) is

\[
X_N = -Z_0 \tan \delta_N.
\]

Thus, the notch frequency \(f_N\) can be expressed by

\[
f_N = \frac{c}{2\pi N} \arctan \left( \frac{X_N}{Z_0} \right).
\]

That is, when the thickness of dielectric slabs is fixed, the notch frequency has a function relationship with the reactance \(X_N\) of the lossless layer and is independent of the lossy layer. We thereby prove that the notch frequency can be fully
controlled by adjusting the lossless layer while the absorption band remains stable. The independent design of the lossy layer and the lossless layer greatly simplifies the design process of an FSA with a dynamically tunable and highly selective notch.

III. MODELING AND PERFORMANCE OF TWO ABSORBERS

A. FSA with a Geometrically Controlled Notch-Band

For the first absorber designed with a geometrically controlled notch-band, a crossed dipole-shaped wideband absorber loaded with four lumped resistors is used as a baseline, which is composed of two perpendicular dipole-shaped [16], [17] patches in each unit and has a period of 10.2 mm. More than 10 dB RCS reduction for two polarizations is realized with a ratio bandwidth over 3.55 within the incident angle of 40°.

The lumped resistors are used to realize wideband impedance matching between the structured absorber and free space. The absorption performance is mainly attributed to the lumped resistors due to the low dielectric loss. The absorption characteristic of the proposed wideband absorber (without a notch) is simulated and analyzed by the frequency domain solver of CST, as shown in Fig. 3.

To generate a notch within the absorption band, a lossless FSS and a substrate supporting it are added to the wideband absorber. The complete model of the notched absorber is shown in Fig. 4. A deformation exists at the end of dipoles to increase terminal capacitance. The sensitivity to incident angles and polarization has been decreased due to its rotationally symmetric and compact structure.

It is well-known that the free space wave impedance at oblique incidence varies with polarization, and the reflection coefficient varies accordingly. Any polarization can be decomposed into TE and TM waves, while \( Z_{0}^{\text{TE}} = Z_{0} \cos \theta \) and \( Z_{0}^{\text{TM}} = Z_{0} \cos \theta \). The impedance variation trends with incident angle are opposite for the two polarizations, which means it is impossible to achieve perfect impedance matching for two polarizations simultaneously under oblique incidences; there must be compromises between these two polarizations. As shown in Fig. 5, the absorption bands are well-maintained when the incident angle is less than 40° for TE polarization or is less than 30° for TM polarization. With an increasing incident angle, the lowest frequency of the grating lobes decreases [4], i.e., more grating lobes appear in the operating frequency band, leading to deterioration of angular stability. In addition to the grating lobes, for TM only, we can see spikes at 12.35 GHz under oblique incidences, which are the so-called Fano resonance [18]. These polarization-dependent Fano peaks result from the asymmetry of the lossless layer at oblique incidences. As we know, for TE polarization, the incident electric field is always in the y-direction. But for TM polarization, when the FSS is incident with an angle \( \theta \), there is a pitch angle between the incident electric field and the FSS plane, thus the symmetry of the system is destroyed, and as a result, Fano resonance is enhanced.

One advantage of our design is that the position of the sharp notch is completely controlled by the lossless FSS whose shape

---

Fig. 3. Reflection coefficient of a crossed dipole-shaped wideband absorber under different incident angles.

Fig. 4. Unit cell of the first absorber with a geometrically controlled notch band. The four chip resistors with a resistance value \( R = 125 \Omega \) are indicated in red. (a) Perspective view. (b) Upper lossy layer. (c) Lower lossless layer. (d) Side view. \( t_{L} = 1.2 \text{ mm}, w_{R} = 1.25 \text{ mm}, r = 1.4 \text{ mm}, l_{C} = 2.9 \text{ mm}, l_{T} = 1 \text{ mm}, r_{1} = 0.25 \text{ mm}, r_{2} = 3.8 \text{ mm}, t_{1} = 1 \text{ mm}, r_{2} = 1.4 \text{ mm}, w_{2} = 1.25 \text{ mm}, l_{C2} = 3.25 \text{ mm} \) and \( p = 10.2 \text{ mm} \).

Fig. 5. Reflection coefficient of a geometrically controlled notched absorber under different incident angles. (a) TE polarization. (b) TM polarization.
is determined by three parameters. By adjusting these three parameters, the center frequency of the notch-band can be adjusted across the whole band. The frequency-domain simulation results are shown in Fig. 6.

In fact, with the other two parameters fixed, simply changing \( r_2 \) can adjust the notch position throughout the entire frequency band, as shown in Fig. 6(a). As \( r_2 \) increases, the center of the notch moves to the lower frequencies.

With \( r_2 \) and \( w_2 \) fixed, changing \( l_2 \) can adjust the notch position over a relatively narrow band, as shown in Fig. 6(b). As \( l_2 \) increases, the center of the notch moves to lower frequencies. When \( l_2 \) increases from 0.4 to 0.5 mm, there is a hop in the position of the notch and a loss in bandwidth; therefore, the value of \( l_2 \) should not be too large.

With \( r_2 \) and \( l_2 \) fixed, changing \( w_2 \) can fine-tune the notch position, which is shown in Fig. 6(c). As \( w_2 \) increases, the center of the notch moves to higher frequencies. Meanwhile, \( w_2 \) affects the width of the notch-band. As \( w_2 \) increases, the notch becomes wider, resulting in poor selectivity; therefore, the value of \( w_2 \) should not be too large.

**B. FSA with an Electrically Controlled Notch-Band**

The second notched absorber has a similar structure to the first but has different FSS patterns. This absorber is designed based on an octagonal ring-shaped wideband absorber (see inset in Fig. 7). The lossy FSS of this absorber is composed of an octagonal ring and four lumped resistors in each unit and is rotationally symmetric. Good absorption performance is achieved within the incident angle of 30° for both TE and TM polarizations, as displayed in Fig. 7. The operating frequency band ranges from 4.63 GHz to 19.82 GHz for normal incidence.

Fig. 8 shows the unit cell structure of the second notched absorber. A major difference from the geometrically controlled absorber is the use of a varactor diode on its lossless layer, which makes it possible to shift the notch position electrically. Hence, one can implement a real-time adjustment of the notch-band by simply changing the bias voltage of the varactor. The lossless layer is based on an H-shaped pattern with a narrow slot on the edge, which permits a y-polarized notch, as seen in Fig. 9(a). When the incident electric field is perpendicular to the direction of the varactor diode, which means the varactor diode is inactive and the induced current on the lossless layer is very low; therefore, there will be no notch-band. The H-shaped structure also makes it easy to apply a bias voltage to the varactor diodes. To narrow the notch-band and achieve high

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Fig. 6. Reflection coefficient of the geometrically controlled notched absorber with different length values of (a) \( r_2 \), (b) \( l_2 \), and (c) \( w_2 \) (mm).

Fig. 7. Reflection coefficient of an octagonal ring-shaped wideband absorber under different incident angles.

Fig. 8. Unit cell of the second absorber with an electrically controlled notch. The four chip resistors with a resistance value \( R_s = 340 \Omega \) are indicated in red. (a) Perspective view. (b) Upper lossy layer. (c) Lower lossless layer. (d) Side view. \( l_{ES} = 1 \text{ mm}, \; w_{ES} = 0.8 \text{ mm}, \; l_E = 4.1 \text{ mm}, \; d = 8.2 \text{ mm}, \; t_s = 0.5 \text{ mm}, \; t_2 = 4.4 \text{ mm}, \; t_3 = 1 \text{ mm}, \; l_{CW} = 0.4 \text{ mm}, \; w_{CW} = 0.3 \text{ mm}, \; h_z = 5.5 \text{ mm}, \; h_2 = 2.9 \text{ mm}, \; w_{C2} = 2.1 \text{ mm}, \; h_{C3} = 1.3 \text{ mm}, \; w_{C3} = 0.6 \text{ mm}, \; \text{and} \; p = 10.2 \text{ mm} \)
selectivity, some deformation is adopted with no more tautology. The simulation results of oblique incidences are shown in Fig. 9.

The type of varactor diode we chose is a MA46H120 with low parasitic capacitance and high Q, and the varactor has a linear tuning range from 0.14 pF to 1.1 pF. As shown in Fig. 10, the notch frequency decreases with increasing capacitance C under y-polarization. For x-polarization, the absorber retains wideband absorption characteristics and will not be affected by the capacitance C of the varactor. Therefore, when applied to antennas, the antenna polarization should be consistent with the polarization of the notch, which can effectively ensure antenna gain and achieve good stealth performance for both polarizations.

IV. IMPEDANCE CONDITION FOR NOTCHED ABSORBERS

In this part, all numerical calculations are based on the geometrically controlled notched absorber. The electrically controlled design can be solved similarly. To simplify the calculation of the numerical solution, only the impedance values of FSSs are set as dependent variables.

First, we plug in the thickness values of the wideband absorber and calculate the values of $Z_R$ that meet the absorption conditions. The equation $|S_{11}| = 0$ is solved numerically at each frequency point with the help of MATLAB, enabling us to obtain $R_R$ and $X_R$ curves satisfying the perfect absorption condition (PAC). For a practical design, we usually choose $|S_{11}| < -10$ dB (with a linear value of 0.316) as a criterion to evaluate the absorption performance, which was referred to as a general absorption condition (GAC) [15]. We successively get the value ranges of $R_R$ and $X_R$ satisfying GAC when $X_R$ and $R_R$ are constrained to PAC respectively. When both the real part and the imaginary part of $Z_R$ come within the areas defined by GAC, less than $-10$ dB reflection can be realized. As shown in Fig. 11, the impedance values of the freestanding lossy FSS in our design lie in the absorption areas at the operating band.

Then comes the generation of the notch-band. From this point forward, we take into account $Z_R$, $C_T$, and $t_2$. As before, the thickness $t_2$ is set to a constant.

It should be noted that the coupling capacitance $C_T$ is considerable when calculating the notch frequency $f_{N}$, which can be confirmed by observing the distribution of the electric field. The value of $C_T$ directly depends on the dimensions of the lossless FSS, and because the dimensions of lossless FSS determine the notch frequency $f_N$, we can deduce that $C_T$ has a function relationship with $f_N$. Using simulation software Ansys Electronics Desktop, we can get impedance curves of the freestanding lossless FSS and the lossless FSS backed with a grounded substrate, namely $Z_R$ and $Z_s$ (see Fig. 2), respectively. With the help of the optimization tool of ADS, we determined the values of $C_T$ for different length values of $r_2$, then the relationship between $C_T$ and $f_N$ is obtained by curve fitting.

$$C_T = \frac{1}{0.0421 f_s^2 - 0.2142 f_s + 1.0366}$$

Plugging in the designed $Z_R$ of the upper lossy FSS, the reflection condition is calculated in an ideal world with $|S_{11}| = 1$ and in a practical situation with less than 0.5 dB insertion loss,
ic coupling is incident electric field. The notch frequency, we can deduce that, we can recognize that the magnetic field concentrates on the metallic units is stronger at lower frequencies, and mainly spreads over the terminal capacitance within a unit.

The slight discrepancies should be attributed to the coupling effect between lossy FSS and lossless FSS, which is relatively weak and is not taken into consideration in the general ECM.

V. EQUIVALENT CIRCUIT EXTRACTION AND ANALYSIS

By observing the distribution of electric field and magnetic field, the distribution of equivalent capacitance and inductance can be roughly inferred (see Fig. 14). For the geometrically controlled notched absorber, we see that the magnetic field concentrates on the metal cross in the center. The coupling between units is primarily electric coupling, which exists between the ends of adjacent dipoles, and the coupling is stronger at lower frequencies. As frequency increases, the coupling between units weakens, and the electric coupling gradually distributed between the intersecting dipole ends within a unit. In general, we can deduce that the equivalent capacitance generated by the interaction between units is larger than that from within a unit, i.e., $C_{11}$ representing the equivalent capacitance between units is much larger than $C_{12}$ representing the terminal capacitance within a unit. The metal cross in the center contributes to the equivalent inductance $L_1$.

Similarly, for the octagonal ring-shaped lossy FSS of the electrically controlled notched absorber, it can be seen from the electric field distribution that the electric coupling between units is stronger at lower frequencies, and mainly spreads over the gaps in the direction of the incident electric field. Meanwhile, the magnetic field concentrates on the metallic stripes along the incident electric field. Two arms perpendicular to the incident electric field have almost no current flowing through. The equivalent capacitance in the direction of the incident electric field is much larger, that is, $C_{31}$.

Fig. 12. Impedance conditions of freestanding lossless FSS at notch frequencies compared with impedance values of our designed lossless FSSs. ($t_1 = 0.25$ mm, $t_2 = 3.8$ mm and $t_3 = 1$ mm)

i.e., $|S_{11}| \geq -0.5$ dB (linear value of 0.94). The result is shown in Fig. 12. Through comparison with the designed impedance values of the freestanding lossless FSS, the notch frequency can be recognized and corresponds to the simulation results of Ansys Electronics Desktop. Moreover, the light blue ($|S_{11}| \geq 0.94$) can be seen to widen, which means the selectivity of notch-band worsens as $f_n$ increases, and this trend is consistent with full-wave simulation result (see Fig. 6). The slight discrepancies should be attributed to the coupling effect between lossy FSS and lossless FSS, which is relatively weak and is not taken into consideration in the general ECM.

Fig. 13. Surface current distribution of lossless FSS layers at a lower absorption band of 7 GHz, notch frequency of 10 GHz, and higher absorption band of 17 GHz. (a)-(c) Geometrically controlled lossless layer, ($t_1 = 1.4$ mm) (d)-(f) Electrically controlled lossless layer under y-polarization. (C = 0.4 pF)

Fig. 14. Integrated ECM for (a) geometrically controlled notched absorber of two polarizations and (b) electrically controlled notched absorber of $y$- and $x$-polarization, respectively.
is much larger than $C_{32}$. In this context, the octagonal rings loaded with resistors are modeled as distributed RLC components.

The band-stop FSS in free space, which can be modeled by a series LC circuit, resonates to be zero impedance when it presents reflection characteristics, and it is inductive below the resonant frequency and capacitive above the resonant frequency. In addition to the rigorous calculations in Section IV, there is a simple method to estimate the resonance frequency of the band-stop lossless FSS in the geometrically controlled FSA.

The traditional cross-shaped FSS is composed of two orthogonal microstrip lines, which allow it to work with an electric field in either direction. In free space, the first resonance occurs at a frequency point where the length of the microstrip line equals half-wavelength [19]. In this instance, the lossless FSS is almost sandwiched by two F4B substrates, which makes the resonance frequency of the freestanding lossless FSS go down by about \( \sqrt{\varepsilon_r} \) [4, 20]; that is, the resonance frequency of the lossless FSS can be roughly estimated as \( c/(2L_c \times \sqrt{\varepsilon_r}) \), where \( L_c \) is the length of the microstrip line. However, while employing a traditional cross-shaped FSS to produce a notch, the adjustable range of notch-band is limited with a large insertion loss. To overcome these shortcomings, the crosswise dipole-shaped FSS with \( L_c \approx L_{c2} + 4r_2 \) is designed to increase terminal capacitance, and as a result, a sharp notch with an insertion loss less than 0.5 dB is obtained, which can be adjusted across the whole band.

To further validate the circuit model, the surface current distribution of the lower band-stop FSS is shown in Fig. 13. Strong surface current is excited only at the notch frequency, very low surface current is induced on the lossless FSS, which means that the tangential electric field is very weak, and consequently, the band-stop FSS is transparent to EM waves and the FSA works as a wideband absorber.

The lossless FSS of the electrically controlled absorber, which is loaded with a varactor, is designed with several gaps to increase the distributed capacitance. After the simulation, it can be seen that the electric field concentrates on the meandering edges of the shape. Strong surface current is induced around the varactor at notch frequency, and a notch-band can only be generated under \( \gamma \)-polarized wave (see Fig. 13(e)) when the incident electric field is parallel to the varactor. For \( x \)-polarization, because the incident electric field is perpendicular to the varactor, very low surface current is induced on the lossless layer, and as a result, there will be no notch-band. Moreover, changing \( C \) cannot influence \( Z_r \); thus, the \( S_{11} \) curve is not affected by the varactor and remains unchanged under \( x \)-polarization.

A general ECM for metal-backed notched absorbers has been discussed in Section II, as is shown in Fig. 2, where variables are functions of both frequency and dimension. For the variables in ECM to be independent of frequency, the upper lossy FSS is modeled by an RLC network [15], and the lower band-stop FSS is modeled by a series LC circuit. To accurately model the absorber under specific dimensions and values, \( C_{11} \) is introduced to ECM, which represents the coupling effect between lossy FSS and lossless FSS and is much smaller than \( C_{32} \). The final circuit schematics of our proposed FSAs are presented in Fig. 14. The first FSA is rotationally symmetric, so its ECM is the same for two polarizations under normal incidence.

As shown in Fig. 14(a), chip resistors in each unit are in parallel, so we have modified the formula in [21] and the total equivalent resistance can be estimated as

\[
R_e \approx \frac{R_s}{N} \frac{S}{S_R},
\]

where \( S \) is the patch area corresponding to the resistance branch, \( S_R \) is the surface area of a chip resistor, \( R_S = R \times w_R/l_R \) is the surface resistance of chip resistors and \( N \) is the number of branches in parallel.

The above estimated \( R_e \) from observations is not accurate, so the optimization tool of Ansys Electronics Desktop is used to approximate the \( S_{11} \) results of the full-wave simulation when impedance values of the freestanding FSSs have been taken as a reference primarily. The optimized parametric values of equivalent circuits are listed in Table I. The \( S_{11} \) result of our proposed ECM is consistent with the \( S_{11} \) curve simulated by CST (see Fig. 15). In the ECM, the dielectric loss is not taken

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<td>0.03</td>
</tr>
</tbody>
</table>

Fig. 15. Reflection coefficients obtained via full-wave simulation and equivalent circuit calculation. (a) Geometrically controlled notched absorber with \( r_1 = 1.4 \) mm. (b) Electrically controlled notched absorber with \( C = 0.4 \) pF.
into account, and only major distributed components are introduced, which are the main causes of deviation from the simulation results.

VI. EXPERIMENTAL VERIFICATION

In this section, samples of the proposed FSAs with geometrically controlled and electrically controlled notch-band have been manufactured and tested.

A. Measurement of a Geometrically Controlled FSA

For the geometrically controlled FSA, which is composed of 19 × 19 unit cells and is 200 × 200 mm² in size, we fabricated one lossy layer and one lossless layer and assembled them successively with nylon screws. As explained before, for the geometrically controlled FSA, we can obtain different notch frequencies by replacing lossless layers of different dimensions. In this experiment, we choose two instances with the only difference of \( r_2 \), which has a length of 1.4 mm and 0.9 mm respectively, and their time-domain simulation results from CST are provided to validate the adjustability of the notch-band.

As shown in Fig. 16, the metallic patterns were printed on F4B substrates using printed circuit board (PCB) technology, and four chip resistors (0805, 120 Ω) were soldered on the copper strips of each resistive element and four chip resistors (0805, 120 Ω) were soldered on the upper substrate and lower substrate to keep them parallel.

The absorbing/reflecting performance of the geometrically controlled FSA was measured by the compact antenna test range system at the Science and Technology on Electromagnetic Scattering Laboratory in Beijing, China [22], [23]. To improve measurement precision, five pairs of standard linearly polarized horn antennas working at 4-6 GHz, 6-8 GHz, 8-12 GHz, 12-18 GHz, and 18-24 GHz were used for transmitting and receiving electromagnetic waves. The RCS is measured using a Keysight N5234A vector network analyzer. To eliminate the interferences from multiple reflections and the coupling effect between two horns, the time-domain gating function of the network analyzer was used to accurately measure the reflected wave. The RCS reduction results of the prototype were obtained after calibrating with a metal ground plane test.

Fig. 17 shows a comparison of the measured and simulated RCS reduction results of the geometrically controlled FSA with \( r_2 = 1.4 \) mm. The measured data are largely in keeping with the time-domain simulation results. Except for the fabrication error and resistor value tolerances, the slight discrepancy between time-domain simulation and measurement results should be attributed to the unevenness of the handmade air layer and the parasitic effect of lumped resistors, which was not taken into account in the full-wave simulation. Compared with the frequency-domain simulation results for infinite periodic structures, the higher insertion losses result from the edge effects of finite arrays. The time-domain simulation result of \( r_2 = 0.9 \) mm is also provided. Compared with the result for \( r_2 = 1.4 \) mm, the notch frequency shifts from 10.0 GHz to 14.5 GHz. The adjustability of the notch is proven in this way.

To reflect the applicability of the geometrically controlled FSA with bistatic scenarios, the time-domain simulation results of bistatic scattering RCS in the E-plane are shown in Fig. 18.
At the absorption frequencies of 7 GHz and 17 GHz, the bistatic RCS of the FSA in the entire space is much lower than that of the equal-sized PEC ground surface. The bistatic stealth performance is better than diffuse scattering based on the phase cancellation method, whose sidelobe level will increase according to the law of conservation of energy [24]-[26]. Moreover, the FSA serves as a PEC surface where almost all incident energy is reflected at notch frequencies of 10 GHz and 14.5 GHz for $r_1 = 1.4$ mm and $r_2 = 0.9$ mm, respectively.

**B. Measurement of an Electrically Controlled FSA**

For the electrically controlled FSA, we fabricated a prototype with $14 \times 14$ unit cells, which is shown in Fig. 19. The upper lossy layer is mounted with four chip resistors (0603, 340 $\Omega$) in each unit, and the lower lossless layer is welded with one varactor diode (MA46H120) in each unit. The size of the F4B substrates is $147$ mm $\times$ $143$ mm due to the addition of bias lines printed on two sides to feed the varactor diodes. For subsequent antenna-loaded tests, one unit cell has been removed. The upper lossy layer is held up with 10 nylon screws and gaskets to keep a 4.4 mm distance from the lower lossless layer.

The measurement setup is shown in the insets of Fig. 20. The electrically-controlled FSA was measured in an anechoic chamber using Keysight E5071A with time-domain gating, which was used to reduce multipath interferences during the measurement of the reflection coefficient. The aperture of the horn antenna for testing is $75$ mm $\times$ $75$ mm, and the horn antenna is 1 m away from the FSA. The FSA was surrounded with absorbent foam to reduce the effect of edge diffraction. Limited by this measurement setup, the far-field conditions were hard to meet for the entire frequency range.

In testing of the electrically controlled FSA, the notch frequency is regulated by changing the bias voltage of the varactor diodes. With an increasing bias voltage, the capacitance of the varactors decreases, thereby the notch moves to higher frequencies. As shown in Fig. 20, the variation trend of the notch-band is consistent with previous conclusions.

To illustrate the application scenario of these band-notched FSAs, we conducted experiments of a monopole antenna backed with the electrically controlled FSA. As shown in Fig. 19, we fabricated a monopole antenna, and then made the upper lossy layer of the FSA. (d) Lower lossless layer of the FSA.

![Fig. 19. Photos of the electrically controlled FSA and an FSA-backed monopole. (a) Photo of the fabricated monopole antenna. (b) Ground plane of the monopole. (c) Top lossy layer of the FSA. (d) Lower lossless layer of the FSA.](image)

![Fig. 20. Measured reflection of the electrically controlled FSA with different bias voltages.](image)

![Fig. 21. Simulated RCS of an FSA-backed monopole under $y$-polarized and $x$-polarized normal incidences compared with a PEC-backed monopole.](image)

![Fig. 22. Simulated and measured reflection of an FSA-backed monopole compared with a PEC-backed monopole. The insets are photos of the PEC-backed monopole.](image)

![Fig. 23. Gain of an FSA-backed monopole compared with a PEC-backed monopole at notch frequency of 11.8 GHz.](image)
monopole perpendicular to the surface of the FSA. The length of the monopole is 18 mm. The monopole is fixed to an F4B substrate, which is 20 mm × 20 mm in size. A metal ground patch with a side length of 10 mm is printed on the back, as shown in Fig. 19(b).

It is learned that a well-structured FSA with more unit cells produces a better ground plane for the antenna, but there is a trade-off between efficiency and RCS. FSA-backed antennas suffer from low-efficiency, which is a compromise to low-RCS. From Fig. 21, we can see that modification to the central unit of FSA has little impact on the performance of RCS reduction; the FSA serving as a ground plane of the monopole effectively lowers the out-of-band RCS level of the monopole.

For comparison, we also measured a PEC-backed monopole antenna. The ground plane of the single PEC-backed monopole is 50 mm in diameter printed on the underside of a perforated F4B substrate, as shown in the insets of Fig. 22. The substrate for the monopole is 1 mm in thickness. According to Fig. 22, the center frequency of the FSA-backed monopole shifts slightly toward higher frequencies, and the bandwidth narrows, which is a consequence of near-field coupling. In Fig. 23, the scattering and radiation performance of the single PEC-backed monopole is also provided as a reference. From Fig. 22 and Fig. 23, it is clear that our designed band-notched FSA allows the monopole antenna to work properly at the notch-band and maintains its radiation pattern, while at other frequencies, the FSA still works as an absorber, thereby reducing the RCS of the antenna.

For an electrically controlled FSA loaded with varactors, in actual use, we recommend using an analog-digital converter (DAC) to control the bias voltage of the varactor diodes and a microcontroller to control the DAC [27]. In this way, the notch frequency of the FSA can be instantly manipulated by a computer via communication with the microcontroller. The operating frequency of the antenna is correlated with the notch frequency; thus, the RCS of a frequency-sweep antenna can be reduced in real time.

Table II provides a comparison of our two designs with two other reported band-notched FSAs. Only our designs have adjustable and highly selective notches. The tunable range of the electrically controlled FSA is limited by the capacitance range of the varactor diode (MA46H120).

### VII. Conclusion

In this paper, we presented two ultrawideband FSA designs with a flexibly adjustable and highly selective notch. By cascading a band-stop FSS layer after the resistive layer, a notch is inserted to the wide absorption band, and the notch frequency is fully controlled by the lossless layer, which can be shifted across the entire absorption band by simply adjusting the lossless layer. Less than 0.5 dB insertion loss is realized at notch frequencies. It is expected that the notched absorber can be combined with an antenna or an antenna array and serve as a ground plane or FSS reflector to realize out-of-band RCS reduction.

The notch frequency of the first design is geometrically controlled, which means the notch is adjusted by replacing the lossless layer and can be applied to narrowband antennas. Thanks to the smaller cell size compared to FSS and the rotationally symmetric structure, this absorber has good angular stability, and is equally effective for both y- and x-polarization within the incident angle of 30°.

Loading a varactor in the lossless FSS, the notch frequency of the second design is electrically controllable under y-polarization, which is better for real-time control of notch frequency, thereby realizing efficient and cost-effective regulation by simply changing the applied voltage of the varactor. Thanks to its real-time control of the notch band, this band-notched absorber can be used not only in narrowband antennas, but also in wideband antennas to create low RCS antennas. A ratio bandwidth \( f_{notch} / f_{T₁} \) of 4:1 is realized for this FSA. Under x-polarization, the FSA retains wideband absorption characteristics.

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Notch Band</th>
<th>Absorption Band</th>
<th>Other Attributes</th>
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<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>Polarization</td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>[16]</td>
<td>No</td>
<td>8.2-9.8</td>
<td>4.8-8</td>
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<tr>
<td></td>
<td>(7.9 GHz)</td>
<td>&amp; 10.2-16</td>
<td>86.5%</td>
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<td></td>
<td>No</td>
<td>4.15-4.56</td>
<td>2.05-4.02</td>
</tr>
<tr>
<td></td>
<td>(3.54 GHz)</td>
<td>&amp; 4.78-7.24</td>
<td>95.4%</td>
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<tr>
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<td>5.35-19.9</td>
<td>5.35-9.46</td>
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<td>&amp; 10.63-19.9</td>
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<tr>
<td>Our work</td>
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<td>8-14</td>
<td>4.77-10.86</td>
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<tr>
<td></td>
<td>(Electrical)</td>
<td>&amp; 11.96-19.08</td>
<td>110.8%</td>
</tr>
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\( λ₁ = \) free space wavelength at the lowest operating frequency \( f_{T₁} \) (see Fig. 1)

\( a \) Relative Absorption Bandwidth: The ratio of the absorption bandwidth relative to the center frequency, which is calculated as (see Fig. 1)

\[
2(f_{T₁} - f_{T₂})/f_{T₁} + f_{T₂}
\]

Table II PERFORMANCE COMPARISON OF BAND-NOTCHED FSAs

<table>
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<th>Absorption Band</th>
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<td></td>
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<td>&amp; 11.96-19.08</td>
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</tbody>
</table>
In the final stages of this work, prototypes of the notched absorbers were fabricated and measured. The theoretical analysis, full-wave simulation, ECM, and experimental results were found to be in reasonable agreement, demonstrating the validity of the proposed design strategies. Moreover, an FSA-backed monopole is measured and vividly shows that the two FSAs can serve as antenna’s ground plane and reduce RCS of the antenna.

REFERENCES

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