

10-1999

# An Experimental and Theoretical Study of the Spin–Orbit Interaction for $\text{CO}^+(\text{A } 2\Pi_{3/2,1/2}, v^+=0-41)$ and $\text{O}^+2(\text{X } 2\Pi_{3/2,1/2g}, v^+=0-38)$

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## Abstract

Accurate spin–orbit splitting constants ( $A_{v^+}$ ) for the vibrational levels  $v^+=0-41$  of  $\text{CO}^+(\text{A } 2\Pi_{3/2,1/2})$  have been determined in a rotationally resolved pulsed field ionization photoelectron study. A change in slope is observed in the  $v^+$  dependence for  $A_{v^+}$  at  $v^+\approx 19-20$ . This observation is attributed to perturbation of the  $\text{CO}^+(\text{A } 2\Pi)$  potential by the  $\text{CO}^+(\text{B } 2\Sigma^+)$  state. Theoretical  $A_{v^+}$  values for  $\text{CO}^+(\text{A } 2\Pi_{3/2,1/2}, v^+=0-41)$  have also been obtained using a newly developed *ab initio* computational routine for spin–orbit coupling calculations. The theoretical  $A_{v^+}$  predictions computed using this routine are found to be in agreement with the experimental  $A_{v^+}$  values for  $\text{CO}^+(\text{A } 2\Pi_{3/2,1/2}, v^+=0-41)$ . Similar  $A_{v^+}$  calculations obtained for  $\text{O}^2(\text{X } 2\Pi_{3/2,1/2g}, v^+=0-38)$  are also in accord with the recent experimental  $A_{v^+}$  values reported by Song et al. [*J. Chem. Phys.* **111**, 1905 (1999)].

## Keywords

Ab initio calculations, Field desorption

## Disciplines

Chemistry

## Comments

The following article appeared in *Journal of Chemical Physics* 111 (1999): 6413, and may be found at doi:[10.1063/1.479941](https://doi.org/10.1063/1.479941).

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Citation: *The Journal of Chemical Physics* **111**, 6413 (1999); doi: 10.1063/1.479941

View online: <http://dx.doi.org/10.1063/1.479941>

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# An experimental and theoretical study of the spin-orbit interaction for $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0-41)$ and $\text{O}_2^+(\text{X}^2\Pi_{3/2,1/2g}, v^+ = 0-38)$

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(Received 10 June 1999; accepted 14 July 1999)

Accurate spin-orbit splitting constants ( $A_{v^+}$ ) for the vibrational levels  $v^+ = 0-41$  of  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2})$  have been determined in a rotationally resolved pulsed field ionization photoelectron study. A change in slope is observed in the  $v^+$  dependence for  $A_{v^+}$  at  $v^+ \approx 19-20$ . This observation is attributed to perturbation of the  $\text{CO}^+(\text{A}^2\Pi)$  potential by the  $\text{CO}^+(\text{B}^2\Sigma^+)$  state. Theoretical  $A_{v^+}$  values for  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0-41)$  have also been obtained using a newly developed *ab initio* computational routine for spin-orbit coupling calculations. The theoretical  $A_{v^+}$  predictions computed using this routine are found to be in agreement with the experimental  $A_{v^+}$  values for  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0-41)$ . Similar  $A_{v^+}$  calculations obtained for  $\text{O}_2^+(\text{X}^2\Pi_{3/2,1/2g}, v^+ = 0-38)$  are also in accord with the recent experimental  $A_{v^+}$  values reported by Song *et al.* [J. Chem. Phys. **111**, 1905 (1999)]. © 1999 American Institute of Physics. [S0021-9606(99)00938-1]

## I. INTRODUCTION

The spin-orbit constants ( $A_{v^+}$ ) for the  $v^+ = 0$  and 2 vibrational levels of  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2})$  have been determined to be 122.0 and 121.87  $\text{cm}^{-1}$ , respectively,<sup>1,2</sup> which are higher than the value of 117.5  $\text{cm}^{-1}$  cited in Huber and Herzberg<sup>3</sup> based on earlier measurements. To our knowledge, the  $A_{v^+}$  values for the high  $v^+$ -levels of  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+)$  have not been measured.

The most general experimental method for the determination of  $A_{v^+}$  values of cations for a wide range of  $v^+$  levels is the photoelectron spectroscopic technique. Due to autoionization mechanisms, photoelectron spectroscopic measurements often allow the observation of highly vibrationally excited states for the cation.<sup>4,5</sup> This is especially the case for threshold photoelectron (TPE) or pulsed field ionization photoelectron (PFI-PE) measurements using a tunable ionization source,<sup>5</sup> where highly vibrationally excited ionic states can be observed due to finite couplings to nearby resonance Rydberg states and/or repulsive states. In photoionization studies using a fixed energy light source, such as HeI, highly vibrationally excited ionic states with negligible Franck-Condon factors can also be observed.<sup>4</sup> When the HeI photon energy coincides with the excitation energy of a Rydberg level, the Rydberg level initially formed can decay to a lower vibronic state of the cation, concomitant with the ejection of an energetic electron. This two-step mechanism can thus give rise to a long progression of vibrational bands for the cation, which would not be observed via direct ionization. The HeI spectrum for CO obtained by Wannberg *et al.*<sup>4</sup> indeed reveals high vibrational bands up to  $v^+ = 18$  for  $\text{CO}^+(\text{A}^2\Pi)$ . However, the two spin-orbit states cannot be resolved in the latter experiment due to the relatively small spin-orbit splitting constant ( $A_{v^+}$ ) for  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2})$ . Kong and Hepburn<sup>6</sup>

have recently performed a high-resolution vacuum ultraviolet (VUV) laser PFI-PE study of  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0$  and 1). The observed rotationally resolved PFI-PE spectra for these vibrational bands are found to be consistent with  $A_{v^+} = 120 \text{ cm}^{-1}$  for  $v^+ = 0$  and 1, which is close to the value of 122  $\text{cm}^{-1}$  determined previously.<sup>1,2</sup>

Taking advantage of the high-resolution vacuum ultraviolet (VUV) facility of the chemical dynamics beamline established at the advanced light source (ALS),<sup>7,8</sup> we have recently developed a novel synchrotron based PFI-PE detection scheme,<sup>9,10</sup> achieving PFI-PE resolutions similar to that observed in VUV laser PFI-PE studies.<sup>10-12</sup> The ease of tunability over a wide energy range (6–30 eV) has made this synchrotron based PFI-PE method highly productive, particularly in measuring photoelectron bands of a long vibrational progression. In recent studies, we have reported rotationally resolved PFI-PE bands for long progressions of  $\text{O}_2^+(\text{X}^2\Pi_{3/2,1/2g}, v^+ = 0-38)$ ,<sup>13</sup>  $\text{NO}^+(\text{X}^1\Sigma^+, v^+ = 0-32)$ ,<sup>14</sup> and  $\text{CO}^+(\text{X}^2\Sigma^+, v^+ = 0-42)$ .<sup>15</sup> Using the same experimental method, we have obtained rotationally resolved PFI-PE spectra for  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0-41)$ . The intensities of PFI-PE bands for higher  $v^+$  ( $>10$ ) levels of  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2})$  are more than 100 fold lower than those observed for the  $v^+ = 0-2$  bands. Despite the low intensities for the high  $v^+$  bands, we have successfully recorded most of the PFI-PE bands for  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0-41)$  at the rotationally resolved level with good signal-to-noise ratios. Here, we present accurate  $A_{v^+}$  values for  $\text{CO}^+(\text{A}^2\Pi_{3/2,1/2}, v^+ = 0-41)$  derived from the analysis of the rotationally resolved PFI-PE spectrum of CO.

In the theoretical front, reliable calculations on spin-orbit interactions have not been readily accessible due to the requirement of accurate electronic and vibrational wave functions. Many theoretical calculations<sup>16-19</sup> have been made

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on the potential-energy surfaces of  $\text{CO}^+$ . The recent multi-configuration self-consistent field configuration interaction (MCSCF-CI) calculations of Lavendy and Robbe<sup>16</sup> and Okada and Iwata<sup>17</sup> have obtained reliable predictions for the vibrational and rotational constants of  $\text{CO}^+(A^2\Pi_{3/2,1/2})$ . However, the  $A_{v^+}$  value of  $92\text{ cm}^{-1}$  for  $\text{CO}^+(A^2\Pi_{3/2,1/2})$  calculated by Lavendy and Robbe<sup>16</sup> is significantly smaller than the experimental measurements<sup>1,2</sup> of  $122\text{ cm}^{-1}$ .

In view of the lack of computational routines available for reliable calculations of spin-orbit coupling constants, we have recently developed a new *ab initio* computational code for this purpose. This code, to be included into the production version of the publicly available quantum chemistry package GAMESS,<sup>20</sup> has the capability of performing efficient spin-orbit coupling calculations for arbitrary spin multiplicities with any CI wave function types supported by GAMESS, for both one and two electron spin-orbit coupling operators. As a test of this computational code, we have calculated the  $A_{v^+}$  values for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$  for comparison with the experimental measurements.

Highly accurate spin-orbit coupling constants for  $\text{O}_2^+(X^2\Pi_{1/2,3/2g}, v^+\leq 11)$  have been determined previously<sup>21</sup> in a comprehensive analysis of the  $\text{O}_2^+(A^2\Pi_u) \rightarrow \text{O}_2^+(X^2\Pi_g)$  emission system. The VUV laser PFI-PE study of Kong and Hepburn has extended the measurement to  $\text{O}_2^+(X^2\Pi_{1/2,3/2g}, v^+=24)$ .<sup>22</sup> We note that the  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{1/2,3/2g}, v^+=-0-45)$  has also been reported recently in a synchrotron based TPE study.<sup>23</sup> However, the latter  $A_{v^+}$  values are derived only from vibrationally resolved data. By employing the synchrotron based PFI-PE detection method, Song *et al.* have made a comprehensive spectroscopic study on  $\text{O}_2^+(X^2\Pi_{1/2,3/2g}, v^+=-0-38)$  at the rotational-resolved level,<sup>13</sup> which provides accurate  $A_{v^+}$  values for these states. Thus, the experimental  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{1/2,3/2g})$  can be considered well established. For this reason, we have also obtained theoretical  $A_{v^+}$  values for this system. The comparison of the theoretical values with experimental  $A_{v^+}$  data for the  $\text{O}_2^+(X^2\Pi_{1/2,3/2g})$  system serves as a second test case for the new computational code.

## II. EXPERIMENTAL AND THEORETICAL METHODS

### A. High-resolution PFI-PE measurements

The design and performance of the chemical dynamics beamline at the ALS has been described previously.<sup>7-11</sup> Briefly, the major components for the high-resolution VUV photoionization facility at this beamline include a 10 cm period undulator (*U10*), a gas harmonic filter,<sup>24</sup> a 6.65 m off-plane Eagle mounted monochromator,<sup>8</sup> and a photoelectron-photoion apparatus.<sup>9-11</sup>

In the present experiment, helium was used in the gas harmonic filter, where higher undulator harmonics with photon energies greater than 24.59 eV were suppressed. The fundamental light from the undulator was then directed into the 6.65 m monochromator and dispersed by a 4800 l/mm grating (dispersion= $0.32\text{ \AA}/\text{mm}$ ) before entering the experimental apparatus. The ALS storage ring is capable of filling 328 electron buckets in a period of 656 ns. Each electron bucket emits a light pulse of 50 ps with a time separation of

2 ns between successive bunches. In each storage ring period, a dark gap (80 ns) consisting of 40 consecutive unfilled buckets exists for the ejection of cations from the orbit. Thus, the present experiment was performed in the multi-bunch mode with 288 bunches in the synchrotron orbit, corresponding to a repetition rate of 439 MHz.

The multipurpose photoelectron-photoion apparatus associated with the chemical dynamics beamline was used for the present study.<sup>9-11</sup> A continuous effusive CO beam was produced by a metal orifice (diameter=0.5 mm) at 298 K and a distance of 0.5 cm from the photoionization-photoexcitation (PI/PEX) region. Thus, the rotational temperature of the CO sample is expected to be  $\approx 298\text{ K}$ . We estimate that the CO density at the PI/PEX region is  $\approx 10^{-3}\text{ Torr}$ . The photoionization chamber and photoelectron chamber were evacuated by turbomolecular pumps with pumping speeds of 1200 and 3400 L/s, respectively. The respective pressures maintained in the photoionization chamber and the photoelectron chamber were  $\approx 1 \times 10^{-5}$  and  $\approx 1 \times 10^{-7}\text{ Torr}$  during the experiment.

The PFI-PE detection scheme using the high-resolution monochromatized undulator synchrotron radiation facility at the ALS has been described previously.<sup>9-11</sup> Briefly, a pulsed electric field (height=1.1 V/cm, width=40 ns, delayed by 20 ns with respect to the beginning of the 80 ns synchrotron dark gap) was applied to the repeller at the PI/PEX region. This pulsed electric field was used to field ionize high-*n* Rydberg species and extract photoelectrons toward the detector and was applied every synchrotron ring period (0.656  $\mu\text{s}$ ). An electron spectrometer, which consists of a steradiancy analyzer and a hemispherical energy analyzer arranged in tandem, was used to filter prompt electrons. We have previously shown that PFI-PEs can be detected with little background from prompt electrons after only an 8 ns delay with respect to the beginning of the dark gap.

The achievable PFI-PE resolution depends on the resolution of the excitation VUV light source and the magnitude of the applied pulsed electric field.<sup>10</sup> The PFI-PE spectra for CO presented in this experiment were measured using monochromator slits ranging from 30–200  $\mu\text{m}$ . The PFI-PE resolution achieved was 4–7  $\text{cm}^{-1}$  [full width at half maximum (FWHM)]. The photon energy step size and counting time used at each photon energy varied between 0.1–0.3 meV and 3–30 s, respectively.

The PFI-PE spectra for CO were calibrated using the PFI-PE spectra of the  $\text{Ar}^+(^2P_{3/2})$  and  $\text{Ne}^+(^2P_{3/2})$  bands obtained at the same experimental conditions. This calibration scheme assumes that the Stark shifts for the IEs of CO and the rare gases are identical. The calibration for the CO PFI-PE spectrum was made before and after the experiment. Our previous experience with energy calibrations of the PFI-PE spectra of other molecular systems indicates that the accuracy of the present energy calibration is within  $\pm 0.5\text{ meV}$ .<sup>25</sup> Since the spin-orbit PFI-PE components for individual  $v^+$ -levels were recorded in a single scan, the error due to energy calibration does not apply to the uncertainties assigned for the  $A_{v^+}$  values. Most of the  $A_{v^+}$  values reported here are based on rotationally resolved data and have uncertainties well within  $\pm 2\text{ cm}^{-1}$ .

TABLE I. Parameters<sup>a</sup> for the Morse potential [Eq. (2)] for CO<sup>+</sup>(A<sup>2</sup>Π) and O<sub>2</sub><sup>+</sup>(X<sup>2</sup>Π) obtained by fitting the *ab initio* potential energies and experimental vibrational energies for CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2</sub>).

Morse potential	$R_e$ (Å)	$A$ (Å <sup>-1</sup> )	$D_e$ (cm <sup>-1</sup> )	$\omega_e^+$ (cm <sup>-1</sup> )	$\omega_e^+ \chi_e^+$ (cm <sup>-1</sup> )
Expt CO <sup>+</sup> (A <sup>2</sup> Π <sub>3/2</sub> ) <sup>b</sup>	1.2444	2.3531	45 147	1567.5	13.61
Expt CO <sup>+</sup> (A <sup>2</sup> Π <sub>1/2</sub> ) <sup>b</sup>	1.2444	2.3579	45 006	1568.3	13.66
Expt CO <sup>+</sup> (A <sup>2</sup> Π) <sup>c</sup>	1.2436	2.345	45 115	1562.1	13.52
Theo CO(A <sup>2</sup> Π) <sup>d</sup>	1.2510	2.2585	45 542	1511.1	12.53
Expt O <sub>2</sub> <sup>+</sup> (X <sup>2</sup> Π) <sup>e</sup>	1.1200	2.8343	54 392	1919.1	16.93
Expt O <sub>2</sub> <sup>+</sup> (X <sup>2</sup> Π) <sup>c</sup>	1.1227	2.8008	53 250	1876.4	16.53
Theo O <sub>2</sub> <sup>+</sup> (X <sup>2</sup> Π) <sup>d</sup>	1.1249	2.7915	55 541	1910.0	16.42

<sup>a</sup> $R_e$  is the equilibrium bond distance for CO<sup>+</sup>(A<sup>2</sup>Π,  $v^+=0$ ) and  $D_e$ =well depth,  $\omega_e^+$ =vibrational frequency, and  $\omega_e^+ \chi_e^+$ =anharmonicity for the Morse potential.

<sup>b</sup>Morse potential based on experimental vibrational energies for work.

<sup>c</sup>Morse potential based on vibrational constants cited in Ref. 3.

<sup>d</sup>Morse potential based on *ab initio* potential energies calculated in this work.

<sup>e</sup>Morse potential based on experimental vibrational energies of Ref. 13.

## B. Spin-orbit coupling calculations

*Ab initio* spin-orbit coupling calculations have been made possible by generalization of the existing spin-orbit coupling code built into the quantum chemistry package GAMESS.<sup>20</sup> In order to accurately reproduce experimental results, a large basis set (AVTZ, built into MOLPRO)<sup>26-30</sup> and an extensive CI wave function have been used. The orbitals are optimized with complete active space self-consistent field (CASSCF) method, the active space including electrons in 8 orbitals (2s and 2p on C and O).<sup>31</sup> Energy values are further refined with single and double excitations from the CASSCF active space into the virtual space using MOLPRO. We have examined the effect of adding single and double excitations from the core 1s orbitals into virtual space: The CO<sup>+</sup> results do not include such excitations and the O<sub>2</sub><sup>+</sup> results do. Spin-orbit coupling calculations are performed with the CASSCF wave function and Pauli-Breit Hamiltonian,<sup>32</sup> including rigorous one and two-electron terms and using the modified version of GAMESS soon to be released for distribution. The effect of including neighboring states into spin-orbit coupling diagonalization has been studied. CO<sup>+</sup> calculations include the 6 lowest CI roots and O<sub>2</sub><sup>+</sup> calculations include two roots (i.e., only the <sup>2</sup>Π<sub>u</sub> state).

The potential energy of CO<sup>+</sup>(A<sup>2</sup>Π) has been calculated for a series of internuclear C-O distances ( $R$ ) of interest and a geometry optimization has been performed (at the CASSCF level) to locate the potential minimum. Experimentally, the splitting between the CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2</sub>) and CO<sup>+</sup>(A<sup>2</sup>Π<sub>1/2</sub>) spin-orbit states is found as a function of vibrational quantum number up to  $v^+=41$ . The rotational constants ( $B_v^+$ ) for CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>,  $v^+=0-41$ ) have also been determined. In the first approach, the corresponding average  $R$  value  $\langle r_{v^+} \rangle$  for individual  $v^+$ -levels of CO<sup>+</sup>(A<sup>2</sup>Π) is estimated using the approximation

$$\langle r_{v^+} \rangle = \frac{\hbar}{\sqrt{2\mu B_{v^+}}}, \quad (1)$$

where  $B_v$  is the rotational constant given by the experiment and  $\mu$  is the reduced mass of CO<sup>+</sup>. At each  $\langle r_{v^+} \rangle$  value, the spin-orbit coupling constant is computed (the single-point approach). As shown in the discussion below, the  $A_{v^+}$  con-

stants for CO<sup>+</sup>(<sup>2</sup>Π<sub>3/2</sub>) and CO<sup>+</sup>(<sup>2</sup>Π<sub>1/2</sub>) calculated at these  $\langle r_{v^+} \rangle$  distances deviate significantly from the experimental values, especially for high  $v^+$  levels.

A more sophisticated approach involves the least-square fit of the calculated *ab initio* potential energies at a series of  $R$  values to a Morse potential

$$U(R) = D_e \{1 - \exp[-a(R - R_e)]\}^2, \quad (2)$$

where  $D_e$  is the well-depth and  $R_e$  is the internuclear distance at the potential minimum. The best fitted parameters  $D_e$  and  $a$  obtained for the Morse potential are listed in Table I. The corresponding vibrational frequency ( $\omega_e$ ) and anharmonicity constant ( $\omega_e \chi_e$ ) for the Morse potential, together with the *ab initio*  $R_e$  value for CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>,  $v^+=0$ ), are also included in Table I. We note that for a Morse potential only two out of the four parameters ( $D_e$ ,  $a$ ,  $\omega_e$ ,  $\omega_e \chi_e$ ) are independent. Since accurate vibrational energies for the CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>,  $v^+=0-41$ ) states have also been determined based on the simulation of their PFI-PE bands, we have also constructed a Morse potential to provide the best fit for the experiment vibrational energies of CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>). The best fitted parameters for the experimental CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2</sub>) and CO<sup>+</sup>(A<sup>2</sup>Π<sub>1/2</sub>) Morse potentials are also given in Table I. We find that these Morse potentials obtained based on the experimental vibrational energies for CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>) are in reasonable agreement with the CO<sup>+</sup>(A<sup>2</sup>Π) Morse potential based on the *ab initio* calculation. We note that the  $R_e$  value and the width of the theoretical CO<sup>+</sup>(A<sup>2</sup>Π) Morse potential are greater than the experimental CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>) Morse potentials. As a result, the outer turning point of the theoretical Morse potential is greater than that of the experimental Morse potential at the same energy. We also list the Morse potential parameters for CO<sup>+</sup>(A<sup>2</sup>Π) constructed based on the vibrational constants cited in Huber and Herzberg.<sup>3</sup> These parameters are in accord with those deduced from the present experiment.

The vibronic wave function used is

$$\Psi^v(r, R) = \Psi_N^v(R) \Psi_e(r, R), \quad (3)$$

where  $\Psi_N^v(R)$  is an eigenfunction of the theoretical Morse

potential,  $\Psi_e(r,R)$  is the electronic wave function, and  $r$  is the electron coordinate. The theoretical  $A_{v^+}$  value is calculated as,

$$\begin{aligned} A_{v^+} &= \int \int \Psi_N^v(R)^+ [\Psi_e(r,R)^+ \hat{H}_{PB} \Psi_e(r,R) \\ &\quad - \Psi_e'(r,R)^+ \hat{H}_{PB} \Psi_e'(r,R)] \Psi_N^v(R) dr dR \\ &= \int \Psi_N^v(R)^+ A(R) \Psi_N^v(R) dR, \end{aligned} \quad (4)$$

where  $\hat{H}_{PB}$  is the Pauli–Breit (PB) Hamiltonian<sup>31</sup> and  $\Psi_e(r,R)$  and  $\Psi_e'(r,R)$  are the eigenvectors of the  $H_{PB}$  matrix in the basis of CASSCF states. The unprimed and primed states correspond to the two levels between which the splitting is calculated (i.e., between  $J=\frac{1}{2}$  and  $J=\frac{3}{2}$  levels). *Ab initio* splitting constants as a function of  $R$ ,  $A(R)$ , are first calculated at discrete  $R$  values and then fitted to an appropriate analytical form for the convenience of performing numerical integration. For the  $\text{CO}^+(A^2\Pi_{3/2,1/2})$  system, the  $A(R)$  function is found to have the form  $A(R)=h(1-\tanh[(R-R_0)s])+A_0$  with the following least-square fit parameters:  $h=51.25$ ,  $A_0=13.5$ ,  $R_0=2.02$ ,  $s=3.75$ . Here,  $R$  and  $A(R)$  are in  $\text{\AA}$  and  $\text{cm}^{-1}$ , respectively.

The average vibrational energies for the  $\text{O}_2^+(X^2\Pi_{3/2,1/2,g})$  spin–orbit states have been determined recently in a similar PFI-PE experiment by Song *et al.*<sup>13</sup> The Morse potentials based on fitting to these experimental vibrational energies are given in Table I for comparison with the best fitted *ab initio* Morse potential for  $\text{O}_2^+(X^2\Pi)$ . As a reference, we also include in Table I the Morse potential for  $\text{O}_2^+(X^2\Pi)$  based on the vibrational constants cited in Huber and Herzberg.<sup>3</sup> Similar to the observation for the  $\text{CO}^+(A^2\Pi)$  system, the theoretical  $R_e$  value is larger than that determined in the experiment. As a result, the other wall of the theoretical Morse potential for  $\text{O}_2^+(X^2\Pi)$  is wider than that for the experimental Morse potential.

The  $A(R)$  function associated with Eq. (4) of the  $\text{O}_2^+(X^2\Pi)$  system has the functional form:  $A(R)=h \exp[-s(R-R_0)^2]+A_0$ . The least-square fit parameters are,  $h=138.219$ ,  $A_0=1.06641$ ,  $R_0=1.0115$ , and  $s=58.9876$ .

### III. RESULTS AND DISCUSSION

#### A. $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$

We have obtained rotationally resolved PFI-PE bands for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$ . The bulk of these data and their analysis, including important issues on spectroscopy and photoionization dynamics, will be presented in a future publication.<sup>33</sup> Here, we have selected to show in Figs. 1(a), 1(b), and 2(b) the respective experimental PFI-PE bands (solid circles) for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=2,15,38)$  to illustrate of the assignment for the spin–orbit components and the typical quality of the simulation. As with the rotational and vibrational constants, the  $A_{v^+}$  values for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$  are derived from the spectral simulation. The intensities shown for the spectra of Figs. 1(a), 1(b), and 2 reflect the actual relative intensities. As

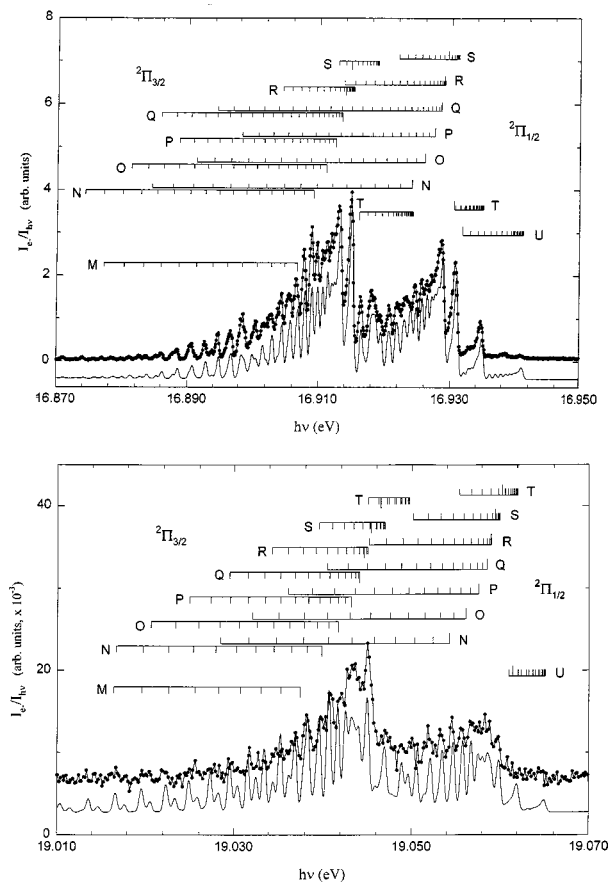


FIG. 1. Comparison of the experimental (solid circles) and BOS simulated (solid line) PFI-PE spectra for (a)  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=2)$  and (b)  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=15)$ . Positions for individual rotational are indicated using down pointing and up pointing stick marks for the  $2\Pi_{3/2}$  and  $2\Pi_{1/2}$  components, respectively. The rotational branches are labeled as  $M, N, O, P, Q, R, S, T,$  and  $U$  for  $\Delta N=-4, -3, -2, -1, 0, 1, 2, 3,$  and  $4$ , respectively. In each  $\Delta N$  case shown, the position of the first and second transitions are indicated by progressively shorter lines. The PFI-PE resolution achieved  $=4 \text{ cm}^{-1}$  (FWHM).

shown in these figures, the intensities for the  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=15$  and  $38)$  bands are more than two orders of magnitude lower than for the  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=2)$  band. We note that the PFI-PE band for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=38)$  has partial overlap with the  $\text{CO}^+(X^2\Sigma^+, v^+=37)$ . Thus, Fig. 2 is a composite figure with panel (a) showing the comparison of the experimental (solid circles) and simulated (solid line) spectra for  $\text{CO}^+(X^2\Sigma^+, v^+=37)$ . The analysis and simulation of the PFI-PE bands for  $\text{CO}^+(X^2\Sigma^+, v^+=0-42)$  has been reported previously and thus will not be substantiated here.<sup>13</sup>

The relative intensities for rotational structures resolved in a vibrational band were simulated using the Buckingham–Orr–Sichel (BOS) model,<sup>34</sup> which is described by the formula

$$\sigma(J^+ \leftarrow N^+) \propto \sum_{\lambda} Q(\lambda; J^+, N^+) C_{\lambda}. \quad (5)$$

This model was derived to predict rotational line strengths observed in the single-photon ionization of diatomic molecules. Since the BOS model does not take into account channel interactions, which are certain to occur in the

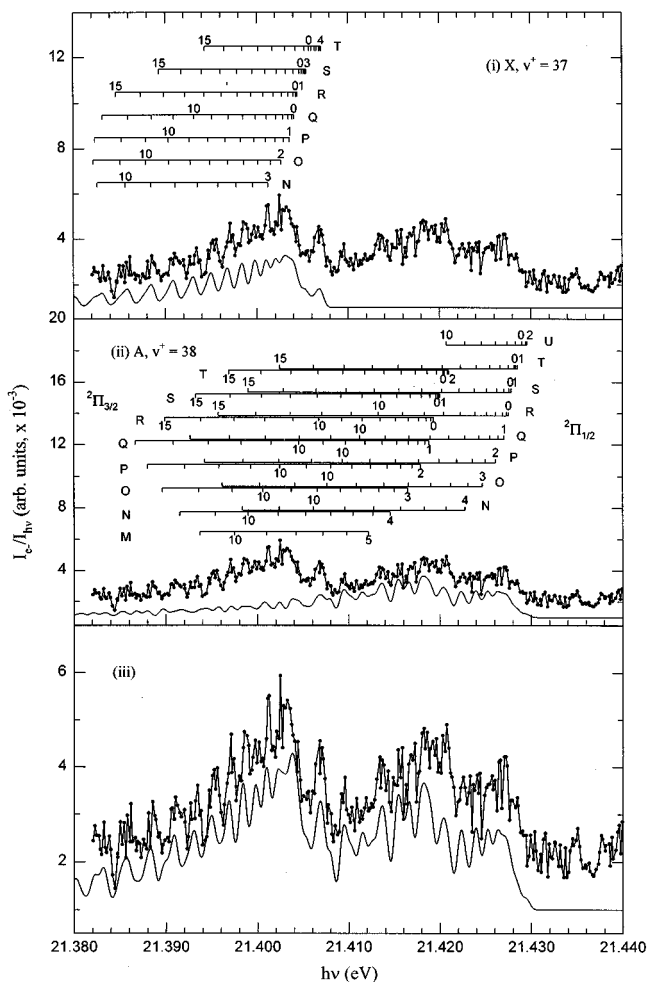


FIG. 2. Composite simulation spectra for CO<sup>+</sup>(X<sup>2</sup>Σ<sup>+</sup>, v<sup>+</sup>=37) and CO<sup>+</sup>(A<sup>2</sup>Π, v<sup>+</sup>=38). The figure is divided into three panels. Panel (i) [(ii)] compares the experimental PFI-PE spectrum (solid circles) and the deconvoluted (solid line) PFI-PE spectrum for CO<sup>+</sup>(X<sup>2</sup>Σ<sup>+</sup>, v<sup>+</sup>=37) [CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>, v<sup>+</sup>=38)]. Panel (iii) compares the experimental (solid circles) PFI-PE spectrum with the sum of the deconvoluted (solid line) spectra for CO<sup>+</sup>(X<sup>2</sup>Σ<sup>+</sup>, v<sup>+</sup>=37) and CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2,1/2</sub>, v<sup>+</sup>=38). In panel (i), positions for individual rotational transitions are indicated by down pointing stick marks. In panel (ii), positions for individual rotational transitions are indicated using down pointing and up pointing stick marks for the <sup>2</sup>Π<sub>3/2</sub> and <sup>2</sup>Π<sub>1/2</sub> components, respectively. The numbers in panels (i) and (ii) are N'' values. The rotational branches are labeled as M, N, O, P, Q, R, S, T, and U for ΔN = -4, -3, -2, -1, 0, 1, 2, 3, and 4, respectively. The PFI-PE resolution achieved=4 cm<sup>-1</sup> (FWHM).

PFI-PE spectra, we may consider the BOS simulation used here as semiempirical in nature. As in previous studies, the BOS simulation is valid in determining spectroscopic constants from the experimental PFI-PE spectra. The factor C<sub>λ</sub> is associated with the electronic transition moments, which is the linear combination of electron transition amplitudes for the possible angular momenta l of the ejected electron. The other factor Q is determined by the angular momentum coupling scheme. The parameter λ can be interpreted as the partial wave of the electron in the ground state of the neutral molecule. The more general interpretation of λ is that of the angular momentum transfer in the photoionization process. The angular momentum coupling factor Q for the photoion-

ization of the present CO system can be described by a Hund's case (b) to (a) transition. The Q factor is thus expressed as

$$Q(\lambda; J^+, N'') = \frac{2J^+ + 1}{2S^+ + 1} \sum_{\chi = |\lambda - 1/2|}^{\chi = \lambda + 1/2} (2\chi + 1) \times \left( \begin{matrix} \lambda & S^+ & \chi \\ \Delta\Lambda & \Sigma^+ & \Lambda'' - \Omega^+ \end{matrix} \right)^2 \times \left( \begin{matrix} J^+ & \chi & N'' \\ -\Omega^+ & \Omega^+ - \Lambda'' & \Lambda'' \end{matrix} \right)^2, \quad (6)$$

where ΔΛ = Λ<sup>+</sup> - Λ'' and Ω<sup>+</sup> = |Λ<sup>+</sup> ± Σ<sup>+</sup>|. Here, Λ<sup>+</sup> and Σ<sup>+</sup> are the projection of the electron orbital angular momentum and electron spin angular momentum on the axis of CO<sup>+</sup>, respectively, and Λ'' is the projection of the electron orbital angular momentum on the axis of CO. Given that ΔΛ = 1 for the transition CO<sup>+</sup>(A<sup>2</sup>Π<sub>Ω</sub>, v<sup>+</sup>) ← CO(X<sup>1</sup>Σ<sup>+</sup>, v''=0), the first 3-j symbol of Eq. (6) requires that λ ≥ 1. The contribution by each C<sub>λ</sub> was determined from the fit to the experimental data. Each spin-orbit state was simulated using a unique set of C<sub>λ</sub>'s. The rotational structure observed in the experiment was accounted for using the BOS coefficients (C<sub>1</sub>, C<sub>2</sub>, C<sub>3</sub>, and C<sub>4</sub>). Thus, the possible angular momentum states for the ejected photoelectron were l = 0, 1, 2, 3, 4, and 5. The possible change in total angular momentum for a Hund's case (b) to (a) ionization transition is given by<sup>12</sup>

$$\Delta J = J^+ - J'' = l + \frac{3}{2}, l + \frac{1}{2}, \dots, -l - \frac{3}{2}. \quad (7)$$

Rotational transitions (ΔN = N<sup>+</sup> - N'') of -4, -3, -2, -1, 0, 1, 2, 3, and 4 (designated as M, N, O, P, Q, R, S, T, and U branches, respectively) are clearly observed in the spectra, although transitions up to ΔN = ±6 are possible according to Eq. (7).

We assume that the rotational population for CO was characterized by a Boltzmann distribution with a rotational temperature of 298 K. The simulation uses known spectroscopic constants for the molecular ground-state CO(X<sup>1</sup>Σ<sup>+</sup>, v<sup>+</sup>): ω<sub>e</sub>'' = 2169.813 58 cm<sup>-1</sup>, ω<sub>e</sub>χ<sub>e</sub>'' = 13.288 31 cm<sup>-1</sup>, B<sub>e</sub>'' = 1.931 28 cm<sup>-1</sup>, and α<sub>e</sub>'' = 0.0175 04 cm<sup>-1</sup>.<sup>3</sup> The spin-rotational splitting present in the ionic state has been ignored since it is much smaller than the experimental PFI-PE resolution.

In addition to the BOS C<sub>λ</sub> coefficients, the rotational constant B<sub>v</sub><sup>+</sup> and the spin-orbit coupling constant A<sub>v+</sub> were varied during the simulation of each vibration level. The simulated spectra (solid line, lower spectra) shown in Figs. 1(a), 1(b), and 2(b) were obtained using a Gaussian profile with a linewidth of 4, 4, and 7 cm<sup>-1</sup> (FWHM), respectively. The positions of the rotational transitions CO<sup>+</sup>(A<sup>2</sup>Π<sub>3/2</sub>, v<sup>+</sup>, N<sup>+</sup>) ← CO(X<sup>1</sup>Σ<sup>+</sup>, v''=0, N'') and CO<sup>+</sup>(A<sup>2</sup>Π<sub>1/2</sub>, v<sup>+</sup>, N<sup>+</sup>) ← CO(X<sup>1</sup>Σ<sup>+</sup>, v''=0, N'') are shown by, respectively, downward pointing and upward pointing stick marks in Figs. 1(a), 1(b), and 2(b). As shown in Figs. 1(a) and 1(b), the agreement between the BOS simulated spectra and the experiment PFI-PE spectra are excellent, yielding values of 120.2 ± 2.0 cm<sup>-1</sup> for A<sub>v+</sub>(v<sup>+</sup>=2), and 117.0 ± 2.0 cm<sup>-1</sup> for A<sub>v+</sub>(v<sup>+</sup>=15). The A<sub>v+</sub>(v<sup>+</sup>=2) value is in excellent accord



TABLE II. Comparison of the experimental and theoretical spin-orbit constants [ $A_{v^+}$  ( $\text{cm}^{-1}$ )] for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$  and  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=0-38)$ .

$v^+$	$A_{v^+}$ ( $\text{cm}^{-1}$ )			
	Expt[ $\text{CO}^+(A^2\Pi)$ ] <sup>a</sup>	Theo[ $\text{CO}^+(A^2\Pi)$ ] <sup>b</sup>	Expt[ $\text{O}_2^+(X^2\Pi)$ ] <sup>c</sup>	Theo[ $\text{O}_2^+(X^2\Pi)$ ] <sup>b</sup>
0	120.2	115.7(116.0)	200.2	195.0(195.1)
1	121.0	115.6(116.0)	199.5	194.4(194.8)
2	120.2	115.5(116.0)	199.0	193.7(194.5)
3	120.2	115.4(115.9)	198.5	193.0(194.2)
4	121.0	115.3(115.8)	197.6	192.2(193.9)
5	122.6	115.2(115.8)	198.0	191.4(193.7)
6	120.2	115.1(115.8)	196.6	190.6(193.2)
7	120.2	114.9(115.7)	195.0	189.7(192.8)
8	120.2	114.7(115.7)	193.1	188.8(192.4)
9	119.4	114.5(115.6)	192.5	187.8(192.0)
10	116.1	114.2(115.6)	192.2	186.8(191.6)
11	120.2	113.9(115.5)	191.0	185.8(191.4)
12	119.4	113.5(115.5)	190.0	184.7(190.7)
13	117.0	113.1(115.4)	189.4	183.5(190.3)
14	119.4	112.6(115.4)	188.0	182.3(189.8)
15	117.0	112.0(115.3)	187.0	181.0(189.3)
16	117.0	111.3(115.3)	185.0	179.8(188.7)
17	117.0	110.5(115.2)	183.5	178.4(188.2)
18	117.0	109.6(115.2)	183.0	177.0(187.6)
19	119.4	108.5(115.2)	179.3	175.5(187.0)
20	...	107.3	182.0	173.9(186.3)
21	...	105.8	177.0	172.3(185.3)
22	109.7	104.2(116.5)	174.0	170.6(185.3)
23	...	102.3	173.0	168.9(184.2)
24	103.2	100.3(130.4)	169.0	167.0(183.1)
25	101.6	98.0(111.0)	168.0	165.1(182.2)
26	99.2	95.5(111.4)	165.0	163.1(182.2)
27	96.0	92.8(111.4)	163.0	161.1(181.4)
28	94.4	90.0(111.2)	161.0	159.0(180.4)
29	91.1	86.9(110.9)	159.0	156.7(179.5)
30	88.7	83.8(110.6)	155.0	154.4(179.0)
31	85.5	80.6(108.9)	155.0	152.0(177.4)
32	83.1	77.4(108.7)	150.0	149.5(175.6)
33	81.5	74.2(107.6)	147.0	147.0(174.4)
34	77.4	71.0(106.7)	146.0	144.3(173.0)
35	74.2	67.9(105.9)	144.0	141.5(173.7)
36	70.2	64.9(105.0)	141.0	138.6(171.6)
37	67.8	61.9(103.7)	142.0	135.7(173.0)
38	66.1	59.1(102.2)	141.0	132.6(169.3)
39	...	56.4	...	...
40	59	53.7(96.0)	...	...
41	57	51.2(92.8)	...	...

<sup>a</sup>This work. Experimental  $A_{v^+}$  values for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$ .

<sup>b</sup>This work. Theoretical  $A_{v^+}$  values for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$  or  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=0-38)$  calculated using the *ab initio* Morse potential. Values in parentheses are obtained by the single-point approach based on the  $\langle r_e \rangle$  value calculated using Eq. (1).

<sup>c</sup>Reference 13. Experimental  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{3/2,1/2})$ .

with the literature value of  $121.87 \text{ cm}^{-1}$ .<sup>2</sup> The comparison of the BOS simulated (solid line) and experimental (solid circles) PFI-PE band for  $\text{CO}^+(A^2\Pi_{1/2}, v^+=38)$  is shown in Fig. 2(b). The sum of the simulated spectra for  $\text{CO}^+(X^2\Sigma^+, v^+=37)$  shown in Fig. 2(a) and  $\text{CO}^+(A^2\Pi_{1/2}, v^+=38)$  gives the overall simulated spectrum (solid line) in Fig. 2(c), which is again in excellent accord with the experimental PFI-PE spectrum (solid circles). The  $A_{v^+}$  value for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=38)$  is determined to be  $66.1 \pm 3.0 \text{ cm}^{-1}$ .

The  $A_{v^+}$  values for  $\text{CO}^+(A^2\Pi_{1/2}, v^+=0-41)$  obtained in the BOS simulation are listed in Table II. The plot of the

experimental  $A_{v^+}$  value versus  $v^+$  is shown in Fig. 3. It is interesting to note that the  $A_{v^+}$  value seems to remain nearly constant until  $v^+ \approx 19$ , which has an IE value of 19.6 eV. Then it decreases nearly linearly toward higher  $v^+$ . Although the  $A_{v^+}$  values for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=20, 21,$  and  $23)$  were not determined in the present experiment due to serious overlap with the  $\text{CO}^+(B^2\Sigma^+, v^+=0-2)$  bands, the plot of Fig. 3 seems to reveal a break or a change in slope at  $v^+ \approx 19$  to 20. This may be indicative of perturbation by other states.

Figure 4 depicts the PFI-PE spectrum for CO in the region of 18.5–20.7 eV. The positions of  $v^+$  levels for

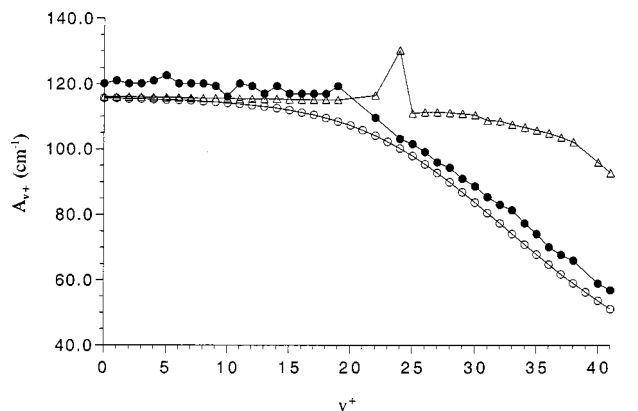


FIG. 3. Plot of the experimental and theoretical spin-orbit splitting constants ( $A_{v^+}$ ) for  $\text{CO}^+(A^2\Pi_{3/2,1/2})$  versus  $v^+$  in the range of  $v^+=0-41$ . Experimental values are in solid circles. The theoretical values obtained using the *ab initio* Morse potential and by the single-point approach are shown as open circles and triangles, respectively.

$\text{CO}^+(X^2\Sigma^+, A^2\Pi_{3/2,1/2}, B^2\Sigma^+)$  are marked in the figure. We note the overlap of the weak  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=19$  and  $20)$  PFI-PE bands with the overwhelmingly strong vibrational band for  $\text{CO}^+(B^2\Sigma^+, v^+=0)$  at 19.80 eV. This observation suggests that the break observed for the  $v^+$  dependence of  $A_{v^+}$  may arise from high-order interactions between the  $\text{CO}^+(A^2\Pi, v^+=19$  and  $20)$  and  $\text{CO}^+(B^2\Sigma^+, v^+=0)$  states. By symmetry, the  $\text{CO}^+(A^2\Pi)$  and  $\text{CO}^+(B^2\Sigma^+)$  can mix by spin-orbit interaction.

Included in Table II are the theoretical  $A_{v^+}$  values obtained based on the theoretical Morse potential and the single-point approach. We have also plotted in Fig. 3 these theoretical  $A_{v^+}$  values. As shown in Fig. 3, for  $v^+ \leq 19$  the single-point theoretical predictions and the experimental results are in slightly better accord than those obtained based on the theoretical Morse potential. However, the predictions for  $v^+ > 19$  obtained by the single-point approach deviate significantly lower from the experimental values. This discrepancy observed at high  $v^+$  is expected and can be attributed to the increasing anharmonicity of the  $\text{CO}^+(A^2\Pi)$  po-

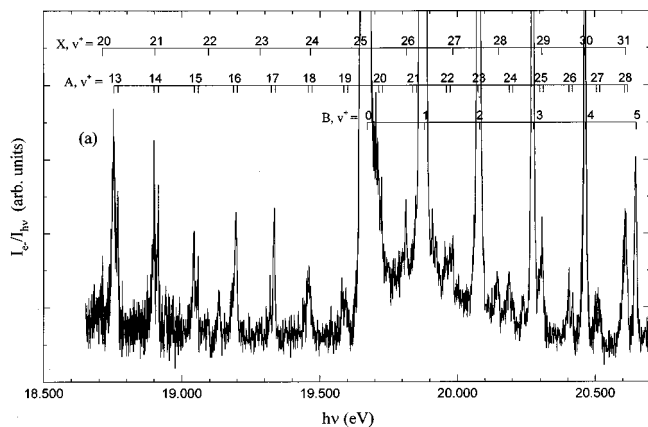


FIG. 4. PFI-PE spectrum for CO in the energy region of 18.5–20.7 eV. The positions of  $v^+$  levels for  $\text{CO}^+(X^2\Sigma^+, A^2\Pi_{3/2,1/2}, B^2\Sigma^+)$  are marked in the figure. Note that the overlap of the weak  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=19$  and  $20)$  PFI-PE bands with the overwhelmingly strong vibrational band for  $\text{CO}^+(B^2\Sigma^+)$  at 19.80 eV.

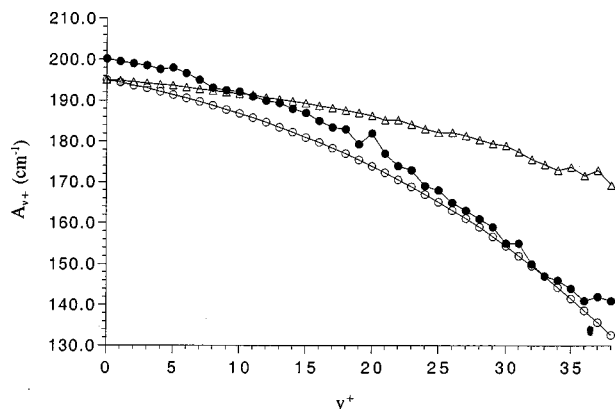


FIG. 5. Plot of the experimental and theoretical spin-orbit splitting constants ( $A_{v^+}$ ) for  $\text{O}_2^+(A^2\Pi_{3/2,1/2})$  versus  $v^+$  in the range of  $v^+=0-38$ . Experimental values are in solid circles. The theoretical values obtained using the *ab initio* Morse potential and by the single-point approach are shown as open circles and triangles, respectively.

tential at high  $v^+$ . That is, the  $\langle r_e \rangle$  values calculated using the approximation of Eq. (1) are not valid at high  $v^+$  levels, yielding significantly smaller values than the actual equilibrium bond distances for high  $v^+$  levels. The theoretical predictions obtained using the theoretical Morse potential show the correct overall  $v^+$  dependence for  $A_{v^+}$ . The theoretical  $A_{v^+}$  value varies smoothly over the whole  $v^+$  range. Contrary to the experimental observation, the  $v^+$  dependence for the theoretical  $A_{v^+}$  values shows no break at  $v^+ \approx 19$  to  $20$ .

We find that all theoretical  $A_{v^+}$  values obtained based on the theoretical Morse potential are slightly lower than the corresponding experimental values. Upon comparing the theoretical and experimental Morse potentials, we find that the *ab initio*  $R_e$  value is larger than the experiment  $R_e$  value. Furthermore, the outer wall of the *ab initio* Morse potential is softer than that of the experimental Morse potential. That is, at the same energy, the outer turning point for the *ab initio* Morse potential lies at a larger  $R$  than that for the experimental Morse potential. As a result, the theoretical Morse potential predicts a larger value for the average equilibrium distance for a given  $v^+$  than that of the experimental Morse potential. This analysis indicates that the lower theoretical predictions compared to the experimental results can be partly ascribed to finite inaccuracy of the *ab initio* Morse potential.

### B. $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=0-38)$

The theoretical  $A_{v^+}$  predictions obtained here based on the single-point approach and the *ab initio* Morse potential are listed in Table I and plotted in Fig. 5 for comparison with the experimental  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=0-38)$ . The latter values have been reported recently by Song *et al.*<sup>13</sup> Similar to the comparison of the  $\text{CO}^+(A^2\Pi)$  system, the single-point predictions are slightly closer to the experimental results at low  $v^+$  ( $< 19$ ). However, contrary to the experimental observation, the slope for the single-point  $A_{v^+}$  prediction versus  $v^+$  plot remains nearly constant over the entire range of  $v^+=0-38$ . That is, the single-point predictions are significantly higher than the corresponding ex-

perimental values at higher  $v^+ (>21)$  levels. This observation can also be attributed to the inaccuracy of using Eq. (1) for the prediction of  $\langle r_e \rangle$  values at high  $v^+$ -levels.

The trend of the  $v^+$  dependence for the theoretical  $A_{v^+}$  value obtained using the *ab initio* Morse potential is consistent with the experimental data. Although the theoretical predictions based on the *ab initio* Morse potential and experimental  $A_{v^+}$  values are in general agreement, all theoretical predictions are slightly lower than the corresponding experimental results. The comparison of the *ab initio* and experimental Morse potentials are similar to the situation of the  $\text{CO}^+(A^2\Pi)$  system. That is, the outer wall of the theoretical Morse potential is shifted to the longer range compared to that of the experimental Morse potential. Thus, this partly contributes to the lower calculated  $A_{v^+}$  values.

The  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=20)$  determined in both the synchrotron based PFI-PE<sup>13</sup> and VUV laser<sup>22</sup> PFI-PE studies are higher than the  $A_{v^+}$  values for the adjacent  $v^+=19$  and 20 states. Thus, the variation of  $A_{v^+}$  versus  $v^+$  is most likely not a smooth function (see Fig. 5). We note that this kink observed at  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=20)$  with an IE  $\approx 15.96$  eV is also close to the beginning of the vibrational progression of the  $\text{O}_2^+(a^4\Pi_u)$  state beginning at  $\approx 16.10$  eV. The latter PFI-PE band is nearly in total overlap with the  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=21)$  state. The  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=37$  and 38), which have the IEs  $\approx 17.9$ –18.0 eV, also seem to deviate from the general trend of the  $A_{v^+}$  versus  $v^+$  curve. This observation may be correlated to the appearance of the vibrational progression for the  $\text{O}_2^+(b^4\Sigma_g^-)$  state at 18.1 eV. On the basis of this observation, we tentatively attribute this kink at  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=20)$  and  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=37$  to 38) as due to perturbation by the  $\text{O}_2^+(a^4\Pi_u)$  and  $\text{O}_2^+(b^4\Sigma_g^-)$  states, respectively. This speculation requires theoretical confirmations in the future.

The effect of core excitations is noticeable mostly at large distances near the dissociation limit where the core excitation become essential to obtain a good energy curve. The Morse potential parameters are noticeably better for  $\text{O}_2^+$  where the excitations have been included. The inclusion of other low lying states of  $\text{CO}^+$ , most noticeably,  $X^2\Sigma^+$ , gives an opportunity to theoretically verify the experimentally seen features in spin-orbit splitting. Since the Morse potential approach is based upon the single state results it displays a smooth dependence without any jumps. The single point approach, on the other hand, allows to study the effect of other states. The calculated jump in spin-orbit splitting at  $v^+=24$  is due to interaction with the  $X^2\Sigma^+$  state. However here the *ab initio* method experiences difficulties associated with having to obtain accurate wave function for both  $X^2\Sigma^+$  and  $A^2\Pi$  states. Two possible solutions exist: State-averaging between the two states of interest or using a feature of our code to do spin-orbit coupling with nonorthogonal separate sets of orbitals. To be consistent with the rest of calculations we choose to optimize orbitals only for the  $A^2\Pi$  state and use these orbitals to obtain the wave function for the other state. This causes a somewhat overestimated jump in the splitting.

## IV. CONCLUSIONS

We have obtained accurate  $A_{v^+}$  constants for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$  in a rotationally resolved PFI-PE experiment. A break at  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+ \approx 19$  to 20) was observed in the plot of  $A_{v^+}$  versus  $v^+$ . Such a feature is tentatively interpreted as due to perturbation of the  $\text{CO}^+(B^2\Sigma^+)$  state. We have also identified similar features in the  $v^+$  dependence of  $A_{v^+}$  values for  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=0-38)$ , suggesting perturbation from the  $\text{O}_2^+(A^2\Pi_u)$  and  $\text{O}_2^+(b^4\Sigma_g^-)$  states.

We have also developed a new *ab initio* computational code for reliable spin-orbit coupling calculations. The  $A_{v^+}$  predictions for  $\text{CO}^+(A^2\Pi_{3/2,1/2}, v^+=0-41)$  and  $\text{O}_2^+(X^2\Pi_{3/2,1/2g}, v^+=0-38)$  obtained using this computation routine are found to be in agreement with experimental measurements.<sup>13</sup>

The systematic underestimation of the theoretical values for the splitting relative to the experimental values is attributed to two factors of the same order of importance: The first-order perturbative treatment of spin-orbit coupling and the complete omission of the spin-spin coupling. To assert the effect of a larger CI expansion upon the spin-orbit coupling we have performed spin-orbit coupling calculations with single excitations from the CAS into the virtual space at equilibrium, near the dissociation limit and at a middle point. The splitting decreased by about  $4 \text{ cm}^{-1}$  except for the dissociation limit where the change was  $8 \text{ cm}^{-1}$ . Thus, the agreement with experiment is found to be worse with the inclusion of the single excitations. Single and double excitations are several million in number and are not possible computationally unless some kind of contraction scheme is employed.

## ACKNOWLEDGMENTS

This work was supported by the Director, Office of Energy Research, Office of Basic Energy Sciences, Chemical Science Division of the U.S. Department of Energy under Contract No. W-7405-Eng-82 for the Ames Laboratory, and Contract No. DE-AC03-76SF00098 for the Lawrence Berkeley National Laboratory. Y.S. is the recipient of the 1999 Wall Fellowship at Iowa State University.

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