From NaZn4Sb3 to HT-Na1–xZn4–ySb3: Panoramic Hydride Synthesis, Structural Diversity, and Thermoelectric Properties

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Abstract
Two new sodium zinc antimonides NaZn4Sb3 and HT-Na1−xZn4−ySb3 were synthesized by using reactive sodium hydride, NaH, as a precursor. The hydride route provides uniform mixing and comprehensive control over the composition, facilitating fast reactions and high-purity samples, whereas traditional synthesis using sodium metal results in inhomogeneous samples with a significant fraction of the more stable NaZnSb compound. NaZn4Sb3 crystallizes in the hexagonal $P6_3/mmc$ space group (No. 194, $Z = 2$, $a = 4.43579(4)$ Å, $c = 23.41553(9)$ Å) and is stable upon heating in vacuum up to 736 K. The layered crystal structure of NaZn4Sb3 is related to the structure of the well-studied thermoelectric antimonides $AeZn2Sb2$ ($Ae = Ca, Sr, Eu$). Upon heating in vacuum, NaZn4Sb3 transforms to $HT-Na1−xZn4−ySb3$ ($x = 0.047(3)$, $y = 0.135(1)$) due to partial Na/Zn evaporation/elimination, as was determined from high-temperature in situ synchrotron powder X-ray diffraction. $HT-Na1−xZn4−ySb3$ has a complex monoclinic structure with considerable degrees of structural disorder ($P2_1/c$ (No. 14), $Z = 32$, $a = 19.5366(7)$ Å, $b = 14.7410(5)$ Å, $c = 20.7808(7)$ Å, $\beta = 90.317(2)^\circ$) and is stable exclusively in a narrow temperature range of 736–885 K. Further heating of $HT-Na1−xZn4−ySb3$ leads to a reversible transformation to NaZnSb above 883 K. Both compounds exhibit similarly low thermal conductivity at room temperature (0.9 W m$^{-1}$ K$^{-1}$) and positive Seebeck coefficients (38–52 $\mu$V/K) indicative of holes as the main charge carriers. However, resistivities of the two phases differ by 2 orders of magnitude.

Disciplines
Materials Chemistry

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From NaZn$_4$Sb$_3$ to \textit{HT}-Na$_{1-x}$Zn$_{4-y}$Sb$_3$: panoramic hydride synthesis, structural diversity, and thermoelectric properties

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Abstract

Two new sodium zinc antimonides NaZn$_4$Sb$_3$ and \textit{HT}-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ were synthesized by using reactive sodium hydride, NaH, as a precursor. The hydride route provides uniform mixing and comprehensive control over the composition, facilitating fast reactions and high-purity samples, whereas traditional synthesis using sodium metal results in inhomogeneous samples with a significant fraction of the more stable NaZnSb compound. NaZn$_4$Sb$_3$ crystallizes in the hexagonal $P6_3/mmc$ space group (No. 194, $Z = 2$, \(a = 4.43579(4)$ Å, \(c = 23.41553(9)$ Å), and is stable upon heating in vacuum up to 736 K. The layered crystal structure of NaZn$_4$Sb$_3$ is related to the structure of the well-studied thermoelectric antimonides \(AeZn_2Sb_2\) (\(Ae = \text{Ca, Sr, Eu}\)). Upon heating in vacuum NaZn$_4$Sb$_3$ transforms to \textit{HT}-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ (\(x = 0.047(3)$, \(y = 0.135(1)$) due to partial Na/Zn evaporation/elimination, as was determined from high-temperature \textit{in-situ} synchrotron powder X-ray diffraction. \textit{HT}-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ has a complex monoclinic structure with considerable degrees of structural disorder (\(P2_1/c\) (No. 14, \(Z = 32$), \(a = 19.5366(7)$ Å, \(b = 14.7410(5)$ Å, \(c = 20.7808(7)$ Å, \(\beta = 90.317(2)^\circ$) and is stable exclusively in a narrow temperature range of 736 – 885 K. Further heating of \textit{HT}-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ leads to a reversible transformation to NaZnSb above 883 K. Both compounds exhibit similarly low thermal conductivity at room temperature (0.9 W·m$^{-1}$·K$^{-1}$) and positive Seebeck coefficients (38–52 µV/K) indicative of holes as the main charge carriers. However, resistivities of the two phases differ by two orders of magnitude.
Introduction

Preparation of the compounds, especially new phases, is oftentimes a bottleneck in the material discovery process. Computational predictions regarding stability, structures and properties of novel compounds are proposed to guide experimentalists, but in order to accelerate materials discovery they should be verified by the targeted synthesis of new compounds [1-7]. The vast number of synthesis parameters (e.g. temperature, pressure, composition, annealing time, cooling/heating rates), as well as kinetic limitations make unguided solid-state synthesis serendipitous. In addition to the compositional space, the synthesis temperature is a decisive factor in the stabilization of a particular compound. In recent years, the advances in in-situ X-ray and neutron diffraction and in-situ TEM methods for reaction monitoring, allow a better understanding of the mechanisms in solid-state reactions [3, 8-17]. For instance, high-temperature X-ray diffraction data of the Cs/Sn/P/Se systems gave a “panoramic” view of the compositional phase space and allowed for the discovery of multiple new phases [3]. Unprecedented photon density and high resolution of synchrotron experiments have yielded high-quality data in a short timeframe, which allows for precise study of relationships among phases upon heating or cooling within a very narrow temperature gradient. Using such methods, “blind” synthetic pathway become clear and high-temperature intermediates detected from high-temperature X-ray diffraction can be further prepared ex-situ.

Hydride synthetic route, which uses mixable salt-like hydride precursors (e.g. alkali metal hydrides AH, A = Li, Na, K), instead of ductile alkali metals was successfully utilized for the synthesis of binary and ternary borides [7, 18-19], antimonides [20-21], arsenides [22-23], silicides [24-27], and germanides [24, 28]. This method is particularly applicable for the compositional screening in the discovery of new ternary alkali zinc antimonides, providing composition control and high purity samples [20]. Traditional solid state synthesis using alkali metal precursors is hampered by their ductility, high reactivity and vapor pressure at elevated temperatures, as well as side reactions with crucible materials. Ductility of alkali metals prevents the intimate mixing of precursors, which oftentimes results in the inhomogeneous samples and impedes compositional control.

Interest in ternary Zintl phase antimonides [29-33] stems primarily from the promising thermoelectric properties of some of the members of this vast family of the compounds, such as $AeZn_2Sb_2$ ($Ae = Ca, Sr, Ba, Eu, or Yb$) [34-35] and $Yb_{14}MnSb_{11}$ [35-37]. Structural and compositional diversity of ternary antimonides containing transition or post-transition metals together with electropositive cations suggests that there are a number of undiscovered related phases with potentially enhanced properties. The hydride synthesis route allows for fast screening of compositional space for different systems at a chosen synthetic temperature. On the other hand, metastable intermediates or phases, which are stable only in narrow temperature range, could be hidden.
Here, we have explored the ternary Na–Zn–Sb system and discovered two new compositionally similar, but structurally different ternary antimonides, both are featuring new structure types. Using the fast hydride route coupled with \textit{in-situ} high-temperature powder X-ray diffraction experiments, compositional and temperature screening allowed for synthesis of two new ternary phases: NaZn₄Sb₃ phase and what at first appeared to be its polymorph, but in fact it is a different compound with slightly Na/Zn depleted composition \textit{HT}-Na₁₋ₓZn₄₋ₓSb₃, stable in narrow temperature range. The hydride route yields single phase samples of both antimonides, allowing for the experimental access to their transport properties. The crystal structures, synthesis, structural transformations, and transport properties of the NaZn₄Sb₃ and \textit{HT}-Na₁₋ₓZn₄₋ₓSb₃ are discussed herein.
Experimental

**Synthesis.** Starting materials for synthesis were used as received: sodium hydride (Sigma-Aldrich, 95%), sodium metal (Alfa Aesar, 99.95%), zinc powder (Alfa Aesar, 99.996%), and antimony lump (Alfa Aesar, 99.9999%). All manipulations of reagents and samples were carried out under an inert argon atmosphere ($p$(O$_2$) < 1 ppm, $p$(H$_2$O) < 1 ppm) in a glove box (LC-Technology).

**Hydride route.** Fine antimony powders were prepared beforehand by ball-milling antimony lumps for 12 min in ambient atmosphere using a standard grinding set with tungsten carbide inserts and high-energy ball-mill SPEX 8000M MIXER/MILL. Afterwards, powders of the sodium hydride, zinc, and antimony were weighted in a 1.03:4:3 molar ratio ($m$ = 0.7 g) and loaded into a polycarbonate grinding set with a methacrylate grinding ball. The vial was further sealed into two plastic bags under argon atmosphere, and removed from the glove box for ball-milling. Samples were ball-milled for 12 min to achieve sufficient mixing, while longer ball-milling caused partial decomposition of NaH. Inside the glovebox, freshly prepared fine powders were loaded into tantalum containers, which were sealed shut by arc-welding. The sealed tantalum ampoules were removed from the glove box and placed into silica reactors equipped with Swagelok safety check valves to prevent over-pressurizing of the reactors due to hydrogen gas release during the heat treatment. The silica reactors were evacuated to $4 \times 10^{-5}$ Bar and placed into a resistance furnace (Thermo Scientific Thermolyne Type FD1500M) equipped with a temperature controller (Eurotherm 3216). Samples were slowly (1.4 K/min) heated from room temperature to 723 K, held at that temperature for 8 h, and cooled to room temperature naturally by switching off the furnace. Phase-pure NaZn$_4$Sb$_3$ compound can be prepared with high purity by following the synthetic method described above. Quenching samples with a Na:Zn:Sb molar ratio of 1.03:4:3 in tantalum containers from higher temperatures (800 K) did not allow the stabilization of $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$. For synthesis of $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase, powders of NaZn$_4$Sb$_3$ phase were loaded into graphitized silica tubes (5 mm diameter, 7 cm length), evacuated to $4 \times 10^{-5}$ bar, flame-sealed, and rapidly heated from room temperature to 800 K (8.4 K/min), held there for 30 min (allowing for partial Na/Zn elimination), and quenched into cold water. Alternatively, $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase can be prepared using the hydride route in tantalum containers, with a Na and Zn depleted (~10%) composition, *i.e.* a NaH:Zn:Sb molar ratio of 0.93:3.61:3. Samples were slowly (1.7 K/min) heated from room temperature to 800 K, held at that temperature for 8 h, and quenched into cold water. Both compounds are air- and moisture-stable but were stored in glovebox for further manipulations.

**Synthesis from elements: single crystals growth.** To obtain crystals suitable for single crystal X-ray diffraction, direct synthesis from elements and heating profile with a slow cooling step was employed. A molar ratio of Na:Zn:Sb = 1.7:4.7:3 with a considerable excess of both Na and Zn was utilized, since samples
with compositions closer to stoichiometric 1:4:3 molar ratio always contained considerable amount of NaZnSb and binary zinc antimonides as impurities. For single crystal growth of the NaZn₄Sb₃ compound, elemental Na, Zn, and Sb were loaded into a graphitized silica tube, flame-sealed under vacuum, and heated from room temperature to 923 K (2.1 K/min), held at that temperature for 24 h, cooled to 473 K at a rate of 0.04 K/min, and cooled to room temperature by switching the furnace off. The same molar ratio 1.7:4.7:3 was utilized for single crystal growth of the $HT$ phase. The mixture was heated from room temperature to 873 K (2.4 K/min), held at that temperature for 12 h, cooled to 800 K at a rate of 0.015 K/min, and rapidly quenched in cold water. Single crystals of the NaZn₄Sb₃ or $HT$-Na$_{1-x}$Zn$_{4-y}$Sb₃ compounds were mechanically separated from the powders of NaZnSb, additionally traces of binary zinc antimonides were present as impurities within the samples.

Characterization.

Laboratory Powder X-ray Diffraction (PXRD). The purity of polycrystalline samples was checked by means of Rigaku MiniFlex600 powder diffractometer with Cu $K\alpha$ radiation ($\lambda = 1.540593$ Å) and Ni-$K\beta$ filter. Data were collected on a zero-background plate holder in air at room temperature. Phase analysis was performed using the PDF-2 database incorporated into PDXL program software [38].

Single-Crystal X-ray Diffraction (SC-XRD). Single crystal data were collected by means of Bruker D8 VENTURE diffractometer (Photon CMOS detector, Mo-$\mu$S microsource and Oxford Cryosystem 800 low temperature device) at 100 K for crystals of NaZn₄Sb₃ and $HT$-Na$_{1-x}$Zn$_{4-y}$Sb₃. Data integration, absorption correction, and unit cell determination was performed by APEX 3 software [39]. The starting atomic parameters were obtained by direct methods with the SHELXS-2017 [38]. Subsequently, the structures were refined using SHELXL-2017 [39] (full-matrix least-squares on $F_o^2$).

NaZn₄Sb₃. Crystals of NaZn₄Sb₃ phase were found to be extensively twinned and/or weakly diffracting, hardly suitable for SC-XRD. Only basic crystallographic parameters, i.e. syngony, cell dimensions, and tentative structural model, though with reasonable interatomic distances, were extracted from experimental single crystal X-ray diffraction data. Due to weak intensity of reflections and insufficient crystal quality, the tentative structure solution was obtained first in triclinic syngony (space group $P\overline{1}$). The further symmetry analysis of atomic coordinates model using Platon software package (command ADDSYM) [41] indicates that the actual symmetry of the structure is hexagonal, space group $P6_3/mmc$ (No. 194, $Z = 2$), $a = 4.43579(4)$ Å, $c = 23.41553(9)$ Å, $V = 399.003(5)$ Å³. This structural model was further used for Rietveld refinement from high-resolution synchrotron powder X-ray diffraction data (Table S1, Figure S1, Table 2).
HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$. Crystals of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase were considerably larger and stronger diffracting than those of NaZn$_4$Sb$_3$. Analysis of the diffraction data revealed pseudo-orthorhombic symmetry, e.g. monoclinic Laue symmetry with the $\beta$ angle close to 90°, space group $P2_1/c$ (No. 14, $Z = 32$). The positions of antimony and zinc atoms were obtained from direct methods (SHELXS) [40]. Positions of sodium atoms were located from a combination of least-squares refinement and difference Fourier maps (SHELXL) [40]. While in the determined model the interatomic distances were found to be within the reasonable range, the refinement has $R_1 \sim 6.5\%$, large inexplicable electron density peaks at the difference Fourier map, and deviation of the $E$-value statistics from 0.97 and 0.74 for ideal centric and acentric distributions (indicative of possible twinning). The data set was analyzed by COSET [42] to determine the twin law, corresponding to the 2-fold rotation around $a$-axis. Further refinement using commands TWIN (1 0 0 0 −1 0 0 0 −1) and BASF in SHELXL allowed to further reduce $R_1$ values down to $\sim 4\%$, while twin fraction was refined to $\sim 7\%$. Further refinement revealed electron density peaks at the difference Fourier map located in a close proximity to the selected Zn or Sb atomic sites, thus the split site model was considered. In this model the sum of site occupancy factors (s.o.f.) for an atomic site and its split counterparts was constrained to 100\%, while the atomic displacement parameters (ADPs) were constrained to be the same: Sb(17)–Sb(25), Sb(21)–Sb(26), Sb(24)–Sb(27), Zn(16)–Zn(32), Zn(20)–Zn(33), Zn(27)–Zn(34), Zn(29)–Zn(35), Zn(30)–Zn(36), Zn(31)–Zn(37) (Table 3). The refined s.o.f. for split Sb and Zn sites did not exceed 13\% and 19\%, respectively. Further refinement indicated that atomic displacement parameters (ADPs) for Na(5) and Na(8) sites were unambiguously larger comparing to the six other Na sites, thus, s.o.f. for Na(5) and Na(8) sites was refined and found to have partial occupancy of 84\% and 75\% respectively. Additionally, Zn(17) and Zn(23) atoms were found to be partially occupied (96.6\% and 93.5\%). More detailed analysis indicates complex crystallographic disorder that was modeled with series of constrains. For instance, independently refined occupancies of Sb(17), Zn(20) and Zn(17) were found to be same within 3 e.s.d. (estimated standard deviation). Therefore, the final refinement of the occupancies was done with the following constrains: either Sb(17), Zn(20) and Zn(17) atoms (refined s.o.f. 95.5\%) or Sb(25) and Zn(33) atoms (refined s.o.f. of 4.5\%) are present. Similar constrains were used for occupancies of Sb(21) and Zn(23), and Sb(24) and Zn(30). In the same manner, occupancies of Na(5) and Zn(31), Na(8), Zn(16) and Zn(27) were constrained to be the same. Details of the data collection and refinement are summarized in Table 1, atomic coordinates, s.o.f. and ADPs are given in Table S2, interatomic distances are listed in Table S3.

Further refinement indicates that atomic displacement parameters (ADPs) for Na(5) and Na(8) sites were unambiguously larger comparing to the six other Na sites, thus, s.o.f. for Na(5) and Na(8) sites was
refined and found to have partial occupancy of 81% in both cases. Details of the data collection and refinement are summarized in Table 1, atomic coordinates, s.o.f. and ADPs are given in Table S2, interatomic distances are listed in Table S3.

**Table 1.** Experimental details and crystallographic data for the $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ (single crystal X-ray diffraction data, 100 K).

<table>
<thead>
<tr>
<th>parameter</th>
<th>value</th>
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<td>refined composition</td>
<td>$Na_{0.953(3)}Zn_{3.865(1)}Sb_3$</td>
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<tr>
<td>space group, $Z$</td>
<td>$P2_1/c$, 24</td>
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<tr>
<td>cell parameters: $a$, Å</td>
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<tr>
<td>$b$, Å</td>
<td>14.708(3)</td>
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<tr>
<td>$c$, Å</td>
<td>20.736(4)</td>
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<tr>
<td>$\beta$, °</td>
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<tr>
<td>$V$, Å³</td>
<td>5950(1)</td>
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<td>density g/cm³</td>
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<tr>
<td>wavelength, Å</td>
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<tr>
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<tr>
<td>min/max transmission</td>
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<tr>
<td>crystal size, mm</td>
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<tr>
<td>measured reflections</td>
<td>104502</td>
</tr>
<tr>
<td>independent reflections</td>
<td>15401 ($R_{\text{int}} = 0.025$)</td>
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<tr>
<td>reflections with $F &gt; 2\sigma(F)$</td>
<td>13212 ($R_\sigma = 0.038$)</td>
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<tr>
<td>parameters</td>
<td>602</td>
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<tr>
<td>GOF for $F^2$</td>
<td>1.13</td>
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<tr>
<td>Final $R$-indices [$F &gt; 2\sigma(F)$]</td>
<td>$R_1 = 0.039$, $wR_2 = 0.086$</td>
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<tr>
<td>$R$-indices (all data)</td>
<td>$R_1 = 0.050$, $wR_2 = 0.091$</td>
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<tr>
<td>larg. diff. peak and hole, e/Å³</td>
<td>2.99 / -1.75</td>
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<td>structure solution</td>
<td>direct methods, SHELXS</td>
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<tr>
<td>structure refinement</td>
<td>least-squares, SHELXL</td>
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</table>
Further details of the crystal structure refinement can be obtained from the Fachinformationszentrum Karlsruhe, 76344 Eggenstein-Leopoldshafen, Germany (fax: (+49)7247-808-666; e-mail: crysdata@fiz-karlsruhe.de) on quoting the depository number CSD 1919785.

**Synchrotron Powder X-ray Diffraction.** High-resolution synchrotron powder diffraction data were collected at beamline 11-BM Advanced Photon Source (APS), Argonne National Laboratory (ANL) with an average wavelength $\lambda = 0.412804 \ \text{Å}$. Data were collected at room temperature and ambient pressure in a Kapton capillary.

High-temperature synchrotron powder X-ray diffraction data (HT-PXRD) was collected at beamline 17-BM (APS ANL) with an average wavelength $\lambda = 0.24130 \ \text{Å}$. Powdered samples of NaZn$_4$Sb$_3$ and HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ were filled in a 0.7 mm outer diameter thick-wall (0.1 mm) silica capillary and sealed under vacuum. The capillary was mounted into a secondary shield capillary (0.9 mm inner diameter, 1.1. mm outer diameter) located on a sample stage equipped with two resistive micro-heaters and a thermocouple set as close as possible to the measurement area. The further details of experimental setup can be found elsewhere [43]. Data were collected upon heating and cooling in the temperature range 298 K $\rightarrow$ 900 K $\rightarrow$ 298 K with a heating and cooling rate of 10 K·min$^{-1}$ and 15 K·min$^{-1}$ for NaZn$_4$Sb$_3$ and HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$, respectively.

Diffraction patterns were analyzed by the Rietveld refinement method using the GSAS II software package [43]. The profile parameters, background parameters, zero correction, and cell parameters were refined first. The background was fitted using a shifted 14 order Chebyshev polynomial function (NaZn$_4$Sb$_3$) and 24-point linear interpolation (HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$), a pseudo-Voigt function was applied to generate the profile shape, the preferential orientation of crystallites was taken into account. Due to the complexity of the structure of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase and presence of light elements (Na, Zn) together with heavy element (Sb), the refinement of all atomic parameters cannot be reliably performed from powder X-ray diffraction data (data/parameters), but full profile fitting using the model determined from the single crystal X-ray diffraction results in low $R_B = 12 \%$, indicating its validity (Tables S1, Figure S2).

**Spark-Plasma Sintering.** Samples of NaZn$_4$Sb$_3$ and HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ prepared via hydride route were further consolidated into dense pellets using Spark Plasma Sintering (SPS). In the argon-filled glovebox, the powdered samples were loaded into a small graphite die (inner diameter 5 mm) between several circles of graphite foil and enclosed with tungsten carbide plungers. The smaller die was assembled, inserted into larger outer graphite die with graphite plungers (inner diameter 20 mm) and further transported to SPS-machine Dr. Sinter Lab Jr. SPS-211Lx (Sumitomo Coal Mining Co., Ltd.) keeping the assembly under inert atmosphere. The samples were sintered by slow heating to 448 K over a period of 10 min under a uniaxial pressure of 90 MPa and dwelling for 5 min. Afterwards, the pressure was released, and sintered pellets were
allowed to cool to room temperature without application of pressure. The pellets were removed from the graphite dies and polished to remove traces of the graphite foil. The geometrical densities of the pellets were ~ 85 % and 81 % for NaZn₄Sb₃ and HT-Na₁₋ₓZn₄₋ₙSb₃ phases, respectively, compared to the theoretical X-ray densities. Binary ZnSb was detected as impurity (7 wt. %) in sintered pellet of NaZn₄Sb₃ phase.

**Elemental Analysis.** Elemental analysis was performed by means of EI Quanta-250 field emission scanning electron microscope (SEM) equipped with an Oxford X-Max 80 detector and an Oxford Aztec energy-dispersive X-ray analysis system. Inside glove box small pieces of the pellets sintered by SPS were mounted onto an aluminum holder designed for air-sensitive samples using double-sided carbon tape, oriented with a flat face perpendicular to the beam and analyzed using a 15 kV accelerating voltage and an accumulation time of 60 s.

**Thermoelectric Properties Measurement.** Transport properties of pellets prepared by SPS were measured in the temperature range of 10–300 K using the commercial multipurpose Physical Properties Measurement System Evercool II (PPMS, Quantum Design). The Seebeck thermopower and thermal conductivity were measured using the Thermal Transport Option (TTO) in a two-probe configuration. Electrical resistivity was measured using the Alternating Current Transport (ACT) option and a four-probe geometry using 50 μm platinum wires attached with silver paste.

**Differential Scanning Calorimetry-Thermal Gravimetry Analysis (DSC-TGA).** To evaluate the thermal stability of the phases, a differential scanning calorimetry (DSC) measurement was performed using a Netzsch 404 F3 Pegasus Differential Scanning Calorimeter. Powdered samples of NaZn₄Sb₃ and HT-Na₁₋ₓZn₄₋ₙSb₃ (m ≅ 50 mg) were sealed inside an evacuated silica ampoule, heated to 873 K, and cooled to room temperature with a rate of 10 K/min rate. In a separate run, the thermal stability of a powdered samples of NaZn₄Sb₃ (m = 12.14 mg) and HT-Na₁₋ₓZn₄₋ₙSb₃ (m = 11.05 mg) were checked by DSC/TGA measurement in an alumina Al₂O₃ pan-type crucible with a lid using a Netzsch STA449 F1 Jupiter. Samples were heated to 900 K and cooled to room temperature with a 10 K/min rate under a flow of argon.

**Computational details.** First-principles calculations were carried out based on density functional theory (DFT) using VASP code [44-46]. The projected augmented-wave (PAW) method [47] was used to describe the electron-ion interaction, and the generalized gradient approximation (GGA) in the Predew-Burke-Ernzerhof (PBE) form [48] was employed for the exchange-correlation energy functional. A plane-wave basis with a kinetic energy cutoff of 520 eV was used. Only the Γ-point was used to perform the Brillouin zone integration for the large unit cell with the composition Na₃Zn₁₂₄Sb₉₆ containing 252 atoms. All atoms in the calculation cell were allowed to relax until the forces on each atom is smaller than 0.01 eV/Å.
Results and discussion.

In the ternary system Na–Zn–Sb, only NaZnSb (PbClF or Cu₂Sb structure type, \(P4/nmm\)) has been previously reported [49-50]. Recently, we have successfully utilized hydride route for preparation of complex solids, including antimonides [19-20], which are hardly accessible by traditional methods of synthesis. The hydride route utilizes brittle salt-like alkali metal hydride precursors (LiH, NaH, KH) instead of ductile and soft alkali metals. This method facilitates thorough mixing of the reactants, allowing for comprehensive control over the alkali metal concentration, thus providing an exceptional purity of products and fast reaction kinetics. Furthermore, it can be used for fast screening of multicomponent systems allowing identification of new compounds with specific chemical composition. For example, in the K–Zn–Sb system, in which only KZnSb has been previously reported [49-50], we recently obtained new compound \(K_{8-x}Zn_{18+y}Sb_{16}\) with high purity using the hydride method [19], while synthesis from elements resulted in inhomogeneous samples with considerable fraction of thermodynamically stable KZnSb.

When the same hydride synthesis is applied in the Na–Zn–Sb system, we identified NaZn₄Sb₃, which subsequently led to the discovery of the \(HT\)-Na\(_{1-x}\)Zn\(_{4-y}\)Sb\(_3\) phase. The composition NaZn\(_4\)Sb\(_3\) is located directly on the line connecting Na and binary Zn\(_4\)Sb\(_3\) or \(Zn_{13-\delta}Sb_{10}\) in the ternary phase diagram. Interestingly, Zn\(_4\)Sb\(_3\) or \(Zn_{13-\delta}Sb_{10}\) exhibits complex temperature-driven phase transitions \(\alpha' \rightarrow \alpha \rightarrow \beta \rightarrow \gamma\) followed by melting at 841 K [51-55]. From the structural point of view, the phase transitions in Zn\(_4\)Sb\(_3\) occur because of the ordering of Zn interstitial atoms and vacancies and is accompanied by the slight variation in Zn composition [51-55]. Structural polymorphism is retained, when Na is introduced to the Zn\(_4\)Sb\(_3\) structure, as two polymorphic-like compounds can be stabilized: NaZn\(_4\)Sb\(_3\) and another phase (referred to as \(HT\)-Na\(_{1-x}\)Zn\(_{4-y}\)Sb\(_3\)). The latter shows a deviation from the 1:4:3 composition and is stable in a narrow temperature range, thus can only be prepared by quenching from high temperatures.

**Crystal structure of NaZn\(_4\)Sb\(_3\).** Synthesis from Na, Zn, and Sb elements in a 1.03:4:3 molar ratio resulted in inhomogeneous samples, where NaZnSb was a major product. On the contrary, the single-phase sample of NaZn\(_4\)Sb\(_3\) can be prepared using NaH, Zn, and Sb mixed in a 1.03:4:3 molar ratio. Synthesis from elements always resulted in inhomogeneous multiphase samples, thus the compositions utilized for single crystal growth deviate from 1:4:3. Single crystals of targeted NaZn\(_4\)Sb\(_3\) phase were selected from the multiphase sample with nominal molar ratio of Na:Zn:Sb = 1.7:4.7:3; samples with composition closer to stoichiometric 1:4:3 molar ratio (e.g. 1.3:4.3:3) contained substantial amounts of NaZnSb and binary zinc antimonides as impurities making harvesting of crystals challenging (Figure S3). The tentative crystal structure model was first obtained from single crystal X-ray diffraction, but the crystals were of poor quality. The obtained model was further refined using synchrotron powder X-ray diffraction data (Table 1 and S1).
NaZn₄Sb₃ has a layered crystal structure \((P6_3/mmc, hP16, a = 4.43579(4) \, \text{Å}, c = 23.41553(9) \, \text{Å}, Z = 2)\) (Figure 1). Search by Pearson symbol, unit cell metric, and Wyckoff sequence \((f\, da)\) of the Inorganic Structure database (ICSD) indicates that this is a new structure type, although its crystal structure is closely related to other ternary zinc antimonides [56], as discussed below. In the structure of NaZn₄Sb₃, Zn atoms occupy two 4\(f\) sites, Sb atoms on one 4\(f\) and one 2\(d\) sites, while a single Na 2\(a\) site is present (Table 2). The layered structure of NaZn₄Sb₃ can be viewed as anionic [Zn₄Sb₃]⁻ slabs sandwiched between a single layer of Na⁺ cations. Within the anionic [Zn₄Sb₃]⁻ slab there are two types of Zn atoms: Zn(2) with a distorted tetrahedral coordination by four Sb atoms at a distances of 2.57 Å and 2.86 Å (×3) and Zn(1) with a trigonal pyramidal coordination by three Sb atoms at a distance of 2.65 Å. A fourth Sb atom is present for Zn(1), but is located at a considerably longer distance, ~3.18 Å. The two antimony atoms have considerably different environments as well: Sb(1) (4\(f\) site) is in an “inverted tetrahedron” or “umbrella-like” coordination capping the surface of the slab by four Zn atoms at a distance of 2.65 Å (×3) and 2.57 Å, and additionally, it has 3 Na atoms at a distance of 3.26 Å. Sb(2) (2\(d\) site) is in a trigonal prismatic coordination at the center of the slab by six Zn atoms at a distance of 2.86 Å. These distances are within the range for typical Zn–Sb distances in other ternary alkali metal zinc antimonides [52], such as NaZnSb (2.76 Å) [20, 50], KZnSb (2.62 Å) [50], K₈₋ₓZn₁₈₊₃ₓSb₁₆ (2.63–2.95 Å) [19], hex-LiZnSb (2.67–2.76 Å) [57], Rb₂Zn₅Sb₄ (2.64–2.90 Å at 200 K) [58], as well as in binary zinc antimonides, such as ZnSb (2.64–2.90 Å) [59], Zn₄Sb₃ (2.55–2.98 Å) [51], and β-Zn₈Sb₇ (2.63-3.15 Å) [60].

The structure of NaZn₄Sb₃ is related to the well-studied \(AeZn₂Sb₂\) \((Ae = Ca, Sr, Eu, Yb)\) family [33-34] with Ce₂SO₂ structure type \((P\bar{3}m, hP5, \text{for } Ae = Ca a = 4.441 \, \text{Å}; c = 7.464 \, \text{Å})\) as well as to the ACd₄P₃ and AZn₄P₃ phases \((A = Na, K, Rb, Cs; P₃ = As, P)\) with NaZn₄As₃ structure type \((R\bar{3}m; hR8, \text{for } NaZn₄As₃; a = 4.1694 \, \text{Å}; c = 32.86 \, \text{Å})\) [61]. Disregarding the trigonal pyramidal coordination of Zn(1) atom, the anionic [Zn₄Sb₃]⁻ slab in the structure of NaZn₄Sb₃ can be viewed as a layer of edge-sharing ZnSb₄ tetrahedra in the \(ab\)-plane, similar to that in \(AeZn₂Sb₂\). Unlike the \(AeZn₂Sb₂\) structure, the [Zn₂Sb₂] layers are further linked by sharing common Sb atoms into [Zn₄Sb₃] slabs. In fact, the structure of NaZn₄Sb₃ can be derived from the CaZn₂Sb₂ structure (Figure 1 and 2a), where every other Ca layer is removed and the adjacent [Zn₂Sb₂] layers are shifted and condensed into a single slab accompanied with removal of one Sb layer (Figure 2a). The resultant [Zn₄Sb₃] slab in NaZn₄Sb₃ is comparable to that of [Zn₄As₃] in NaZn₄As₃ (Figure 1 left) [61]. Unlike NaZn₄Sb₃, the two Zn atoms in adjacent tetrahedral ZnAs₄ units are not aligned, leading to different central Sb atom coordination: trigonal prismatic in the case of NaZn₄Sb₃ and trigonal antiprismatic in NaZn₄As₃ (Figure 2b). Furthermore, the stacking sequence of [Zn₄(As/Sb)₃] slabs is different: in NaZn₄As₃ the adjacent [Zn₄As₃] slabs are shifted by 1/3 in the \(ab\)-plane, to produce a \(R\)-centered
trigonal unit cell; while in NaZn$_4$Sb$_3$ two [Zn$_4$Sb$_3$] slabs are related by an inversion center with hexagonal layers of Na$^+$ cations in between. Therefore, the NaZn$_4$Sb$_3$ is a new representative for the family of Zintl phases which adopts a 1:4:3 stoichiometry but has its own unique layered crystal structure.

Considering Na and Zn as +1 and +2 cations, respectively, and the electronegative Sb having $-3$ oxidation state, the valence electron count for NaZn$_4$Sb$_3$ yields electron-balanced composition Na$^+$(Zn$^{2+}$)$_4$(Sb$^{-3}$)$_3$.

Table 2. Atomic coordinates and isotropic displacement parameters of NaZn$_4$Sb$_3$ ($P6_3/mmc$, $hP16$, $a = 4.43579(4)$ Å, $c = 23.41553(9)$ Å) synchrotron data, 298 K.

<table>
<thead>
<tr>
<th>Site</th>
<th>Wyckoff site</th>
<th>x</th>
<th>y</th>
<th>z</th>
<th>$U_{iso}$, Å$^2$</th>
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<tr>
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<td>4f</td>
<td>$\frac{1}{3}$</td>
<td>$\frac{2}{3}$</td>
<td>0.08580(4)</td>
<td>0.0105(2)</td>
</tr>
<tr>
<td>Sb(2)</td>
<td>2d</td>
<td>$\frac{1}{3}$</td>
<td>$\frac{2}{3}$</td>
<td>$\frac{1}{4}$</td>
<td>0.0220(3)</td>
</tr>
<tr>
<td>Zn(1)</td>
<td>4f</td>
<td>$\frac{1}{3}$</td>
<td>$\frac{2}{3}$</td>
<td>0.61404(5)</td>
<td>0.0350(4)</td>
</tr>
<tr>
<td>Zn(2)</td>
<td>4f</td>
<td>$\frac{1}{3}$</td>
<td>$\frac{2}{3}$</td>
<td>0.19542(5)</td>
<td>0.0361(3)</td>
</tr>
<tr>
<td>Na</td>
<td>2a</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.112(3)</td>
</tr>
</tbody>
</table>
Figure 1. Crystal structure of NaZn$_4$Sb$_3$ in comparison with structure of NaZn$_4$As$_3$ (left) and CaZn$_2$Sb$_2$ (right). The coordination of Zn and Sb atoms is emphasized; Na(Ca) – blue, Zn – orange, Sb(As) – cyan.
Figure 2. a) Schematic showing transformation of [Zn$_2$Sb$_2$] layer found in the CaZn$_2$Sb$_2$ structure into [Zn$_4$Sb$_3$] layer in structure of NaZn$_4$Sb$_3$; b) Structural comparison of anionic slabs [Zn$_4$As$_3$] and [Zn$_4$Sb$_3$]; dashed line emphasizes the alignment of Zn atoms within two stacked Zn(As/Sb)$_4$ tetrahedral units. The difference in coordination polyhedral for Sb(As) is shown. Na(Ca) – blue, Zn – orange, Sb(As) – cyan.

*Reversible NaZn$_4$Sb$_3$ to HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ transformation by in-situ HT-PXRD.* High-temperature synchrotron powder X-ray diffraction (HT-PXRD) of the NaZn$_4$Sb$_3$ sample sealed under vacuum in a silica capillary indicates its structural transformation into the HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase at $\sim$736 K (Figure 3). Binary ZnSb begins to emerge at $\sim$500 K upon heating, indicating partial Na elimination as a result of side reaction with the silica, but disappears (melts) above 736 K. With further heating of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ above 885 K, the sample converts to NaZnSb and melt. Upon cooling from 900 K, the reversible transformation takes place: NaZnSb + melt $\rightarrow$ HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ at 885 K $\rightarrow$ NaZn$_4$Sb$_3$ at 720 K. It should be noted that according to the HT-PXRD data, the HT-phase exists exclusively in the narrow temperature range 736-885 K. With the increasing of temperature above $\sim$736 K formation of the HT-phase is driven by Na/Zn elimination, and as a result its content is increasing, while fraction of NaZn$_4$Sb$_3$-phase is decreasing. Above 810 K, traces of NaZnSb appear, which becomes more pronounced above 885 K when the HT-phase completely decomposes. By comparing two PXRD patterns collected at 373 K on heating and cooling steps, the cooling step contains NaZn$_4$Sb$_3$ ($\sim$86%) with more impurities, such as NaZnSb, ZnSb, and unassigned peaks,
compared to heating data (*i.e.* initial sample). This suggests a shift in composition from the initial Na:Zn:Sb 1:4:3 ratio and partial decomposition of NaZn₄Sb₃ phase upon heating (Figure 3, 6).

*In-situ* high-temperature synchrotron powder X-ray diffraction is very sensitive to phase transitions, as it provides high resolution data, facilitating detection of even small amounts of crystalline phase(s) at different temperatures. Differential scanning calorimetry (DSC) on the other hand is not suitable for systems where many exo- and endothermic reactions take place simultaneously. The Na–Zn–Sb system is an example of such a case, in which samples that are heat treated under vacuum can lead to partial Na/Zn evaporation and possibly side reactions with the containment vessel (silica). DSC data of NaZn₄Sb₃ sample in an alumina crucible (Figure S4) indicates an endothermic process, possibly due to its melting or decomposition at ~750 K, followed by a smaller endothermic event at ~800 K, possibly because of NaZnSb formation. Upon heating of the sample in an alumina crucible, a 1% mass loss is observed, which may be due to a slight Na/Zn evaporation. On cooling, two exothermic peaks are observed: less intensive at ~765 K, possibly due the traces of $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ present, as a result in the composition shift, and a more intense peak at ~735 K, when NaZn$_4$Sb$_3$ is recovered. In turn, DSC data of samples run in silica is in accordance with *in-situ* high-temperature synchrotron powder X-ray diffraction data. However due to side/competing reactions at elevated temperatures, analysis is less sensitive. The PXRD data of the sample after DSC (in silica) indicates that NaZn$_4$Sb$_3$ is partially decomposed during the measurement, as peaks of Zn$_4$Sb$_3$ and ZnO are evident (Figure S5). This is further evidence that Na elimination processes may be due to a side reaction with the silica vessel.

**Synthesis of $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$.** Equipped with the knowledge regarding the temperature range, where $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ is stable, its synthesis was performed by quenching of the NaZn$_4$Sb$_3$ sample in evacuated and sealed silica ampoule from 800 K. Furthermore, $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ compound can be prepared by annealing of NaH, Zn and Sb in the Ta ampoule, but only when Na- and Zn-depleted composition NaH:Zn:Sb = 0.93:3.61:3 (molar ratio) is used, whereas 1.03:4:3 molar ratio always gives NaZn$_4$Sb$_3$ phase even after quenching from 800 K. This again indicates that during heating of NaZn$_4$Sb$_3$ in silica tube partial elimination of Na and Zn takes place, probably due to the side reaction of Na with SiO$_2$, thus shifting the composition toward the Na/Zn depleted facilitates formation of $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$. The Na/Zn deficiency in $HT$-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase was further confirmed by refinement of the crystal structure from single crystal diffraction data and EDX analysis (*vide infra*).
Figure 3. (top) High-temperature *in-situ* powder X-ray diffraction patterns, showing the transformation of powdered sample NaZn₄Sb₃ sealed in an evacuated silica capillary. The “waterfall” plot shows the evolution of PXRD patterns with the concomitant change in temperature from room temperature to 900 K followed by subsequent cooling to room temperature. The temperature regions with distinct phase contributions are highlighted in blue/yellow/red; (bottom) Selected high-temperature powder X-ray diffraction patterns showing the products of decomposition/transformation of the NaZn₄Sb₃ at different temperatures. Selected groups of peaks as “fingerprints” of the ternary and binary phases are highlighted: green (143) – NaZn₄Sb₃; blue (HT) – HT-Na₁₋ₓZn₄₋ₓSb₃; orange (111) – NaZnSb; L = liquid; 122 – “NaZn₂Sb₂”.

Crystal structure of HT-Na₁₋ₓZn₄₋ₓSb₃: structural complexity and disorder.

Single crystals were selected from an inhomogeneous sample prepared from the elements in the same nominal composition (Na:Zn:Sb = 1.7:4.7:3) as one used for crystal growth of NaZn₄Sb₃ compound; sample
was quenched to stabilize $HT$-$Na_{1-x}Zn_{4-y}Sb_3$. Sample contained considerable fraction of NaZnSb impurity (in a powdery form), while chunks mechanically separated from powders comprise mainly $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ phase (Figure S6). The complex crystal structure (Figure 5) of $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ was determined from single crystal X-ray diffraction data. $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ crystallizes in the monoclinic space group $P2_1/c$ (No. 14, $Z = 32$) and unit cell with monoclinic, pseudo-orthorhombic symmetry ($a = 19.508(3)$ Å, $b = 14.708(3)$ Å, $c = 20.736(4)$ Å, $\beta = 90.402(5)^\circ$) (Table 1). The unit cell of the ideal structure contains 96 Sb atoms distributed over 24 4$e$-sites, 124 Zn atoms distributed over 31 4$e$-sites, and 32 Na atoms occupying 8 4$e$-sites (Table 3). Searching of the Inorganic Crystal Structure Database (ICSD) using Pearson symbol ($mP252$), unit cell metrics, and Wyckoff sequence ($e^{63}$) indicate that this is a new structure type [50].

The structure is organized around Sb chains running along the $b$-axis (Figure 5a-b). These chains are surrounded by Zn atoms, which are further connected to a second shell of Sb atoms, forming tubular columns along $b$-axis (Figure 5a and c). Those columns are then linked in the $ac$-plane either via Zn–Sb intercolumnar bonds or via bridging Zn atoms to form a three-dimensional framework with large channels, hosting two columns of Na$^+$ cations (Figure 5d). The Zn–Sb distances range between 2.57 Å–2.94 Å, and are similar to the Zn–Sb distances in other ternary alkali metal zinc antimonides (vide supra). The Sb atoms are either 5- or 6-coordinated by Zn atoms, except Sb(8), Sb(14), Sb(16), Sb(18), and Sb(22), which are 3-coordinated (Table S3). Sb atoms surround Na within the channels, and thus are coordinated by 2-4 Na$^+$ at distances ranging from 3.13 Å to 3.67 Å. The relatively short Na–Sb distances of ~3.13 Å are not typical, but have been reported in other ternary and quaternary sodium antimonides, such as Na$_3$InSb$_2$ [62], Na$_2$Al$_2$Sb$_3$ [63], Na$_5$SnSb$_3$ [64], K$_2$NaInSb$_2$ [65], Na$_2$YbCdSb$_2$ [66]. Most of the Zn atoms are in a distorted tetrahedral coordination by four Sb sites, except for zinc atoms residing in split positions.

A considerable degree of disorder occurs within the structure of $HT$-$Na_{1-x}Zn_{4-y}Sb_3$, mainly associated with the Na(5) and Na(8) sites being ~81% occupied, as well as Sb and Zn split sites and two partially occupied zinc sites, Zn(23) and Zn(17) (Figure 5b-d). Split sites within the Sb chain (Figure 5b-c) evokes additional splitting in adjacent Zn sites. For instance, when Sb(24) is present, it is coordinated by Zn(30), while Sb(27) is coordinated by Zn(36). Likewise Sb(17), Zn(20) and Zn(17) atoms are present (s.o.f. of 95.5%) or Sb(25) and Zn(33) atoms (s.o.f. of 4.5%). The partial occupancy of Na(5) and Na(8) within the channels also leads to the splitting of the adjacent Zn positions, e.g. when Na is absent, Zn atoms slightly move toward the “hole” in the channel: either Na(5) and Zn(31) are present (s.o.f. 81.4%) or Zn(37) (s.o.f. 18.7(9)%). Similarly, when Na(8), Zn(16) and Zn(27) are occupied (s.o.f. 81.2%), then Zn(32) and Zn(34) are absent (s.o.f. 18.8%). Considering structural disorder, the refined composition from single crystal XRD for $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ is Na$_{0.953(3)}$Zn$_{3.865(1)}$Sb$_3$, which is consistent with the Na- and Zn-depleted composition needed for synthesis. This refined composition $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ suggests an electron imbalance, when +1
and +2 charges are assigned for Na and Zn, respectively, and the electronegative Sb has a −3 charge: 
\((\text{Na}^+)_{0.953}(\text{Zn}^{2+})_{3.865}(\text{Sb}^{-3})_{3}\) with 0.36 extra electrons per formula unit.

**Figure 4.** a) Crystal structure of \(HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3\) in \(ac\)-plane: Na – blue, Zn – orange, Sb – cyan. Split sites are not shown, various fragments are highlighted with red (Sb chains), green (Na channels), yellow and black circles; b) Sb chain running along \(b\)-axis; split Sb sites are shown in grey and their s.o.f. is given in %; the bond distances and longer interatomic distances are drawn with solid and dashed lines, respectively; c) Coordination of Sb atoms from the chain by Zn atoms; the split Zn sites are shown in black and their s.o.f. is given in %; the unrealistic Zn–Zn distances due to the split sites are shown with red dashed lines; d) Coordination of Na atoms within the channel; Na with partial occupancy is shown in red together with its s.o.f. (%); the split Zn sites are shown in black and their s.o.f. is given in %; the unrealistic Na–Zn distances due to the split sites are shown with yellow dashed lines; Na–Na distances exceed 3.59 Å.

**Vacancy formation in \(HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3\): computational input.** In order to evaluate the preference for the vacancy formation in the specific Na sites in the structure of \(HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3\), the vacancy formation energies \((E_{\text{vac}})\) for various Na sites were calculated by

\[
E_{\text{vac}} = E(\text{cell}_{\text{vac}}) + E(\text{Na}) - E(\text{cell}),
\]

where \(E(\text{cell})\) and \(E(\text{cell}_{\text{vac}})\) are the total energies of the optimized structures with and without a Na vacancy, respectively. \(E(\text{Na})\) is the energy of a Na atom in the bulk phase. The idealized structure model (without
split sites for Sb/Zn) considered for calculations has the composition Na$_{32}$Zn$_{124}$Sb$_{96}$ (≡NaZn$_{3.875}$Sb$_3$, \textit{cell}) and was further optimized to yield $E(\text{cell})$. One Na atom was removed from each of the eight Na sites in succession (Table 3), and the structure with the composition Na$_{31}$Zn$_{124}$Sb$_{96}$ (≡Na$_{0.96875}$Zn$_{3.875}$Sb$_3$, \textit{cell}_{\text{vac}}) was optimized to yield $E(\text{cell}_{\text{vac}})$. A positive value of $E_{\text{vac}}$ indicates an energy cost to create the vacancy. As it can be seen from Table 4, vacancies at Na(5) and Na(8) sites have the lowest formation energy compared to other Na sites, which is consistent with the experimentally determined structure from SC XRD with only Na(5) and Na(8) sites exhibiting partial occupancies (Table S2). Furthermore, based on the first-principle calculations, the formation of vacancies at Na(5) and Na(8) sites only causes slight local structural relaxations. The relaxation patterns around vacant Na(5) or Na(8) are rather similar: vacancy formation causes two adjacent Zn atoms and adjacent Na atoms to shift toward the vacancy, while overall structural motif remains unchanged. That is again consistent with the structure solved from SC XRD data (Figure 5d), where vacancies in Na(5) and Na(8) sites cause the splitting of the adjacent Zn sites.

Table 3. Vacancy formation energy at each Na site in the structure of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$. Two sites with the lowest vacancy formation energies are italicized.

<table>
<thead>
<tr>
<th>Site</th>
<th>$E_{\text{vac}}$ (eV)</th>
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<tbody>
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<td>Na(1)</td>
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<tr>
<td>Na(2)</td>
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<tr>
<td>Na(3)</td>
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<td>Na(6)</td>
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<td>Na(7)</td>
<td>0.881</td>
</tr>
<tr>
<td>Na(8)</td>
<td>0.763</td>
</tr>
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</table>

\textit{Thermal stability of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$.} High-temperature powder XRD data for the HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase indicates multiple transitions upon heating (Figures 6 and 7). A cascade of exothermic peaks is present on the DSC heating curve in alumina crucible at 470–575 K, indicating that HT-phase is indeed metastable at room temperature and its early transformation to NaZn$_4$Sb$_3$ was observed already at 520 K. The metastable nature of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ was also evident from its decomposition during spark plasma sintering already at 473 K, while sintering at a slightly lower temperature (453 K) resulted in 81% pellet compactness without any discernable changes based on PXRD.

From the \textit{in-situ} high-temperature synchrotron powder XRD data (Figures 5) the HT-phase was found to decompose according to the following equation:
HT-Na_{1-x}Zn_{4-y}Sb_{3} \rightarrow NaZn_{4}Sb_{3} + ZnSb + “NaZn_{2}Sb_{2}” in the temperature range 470 K–765 K. A new phase detected from synchrotron PXRD data, has composition richer in Na and Sb than 1:4:3; this phase will be reported in due course (tentative composition is \( \sim 122 \)). Upon further heating above 765 K, HT-Na_{1-x}Zn_{4-y}Sb_{3} phase reappears (also evident from DSC data, Figure S4) as a strong endothermic peak at 770 K), according to the following equation: NaZn_{4}Sb_{3} + ZnSb + new \rightarrow HT-Na_{1-x}Zn_{4-y}Sb_{3}. At around 850 K, the decomposition of HT-Na_{1-x}Zn_{4-y}Sb_{3} starts according to DSC data but the melting temperature of 885 K was not achieved in the HT-PXRD data. Upon cooling, HT-Na_{1-x}Zn_{4-y}Sb_{3} recovers, and with further cooling to room temperatures transforms to NaZn_{4}Sb_{3}, binary ZnSb, and a new phase; this transformation occurs within broad range of 760–665 K. At the end of the cooling cycle, binary ZnSb is the main product (Figure 5), which indicates that considerable Na/Zn elimination during heating at high temperatures took place, leading to the shift in composition, as schematically represented in Figure 8. DSC data of samples run in silica and alumina are in accordance with in-situ HT-PXRD data. More substantial shift in composition caused by more pronounced Na/Zn elimination in silica may lead to formation of intermediate side products, leading to the additional DSC-peaks on cooling. It should be noted that relative intensities of the peaks of the HT-Na_{1-x}Zn_{4-y}Sb_{3} phase (apparently visible at \( 2\theta \sim 1.4^\circ \) in Figure 5) vary at different temperatures, although PXRD of the quenched samples are always same. This could be due to the certain variation in composition or disorder occurring at the different temperatures, while the quenched HT-Na_{1-x}Zn_{4-y}Sb_{3} always retains its stable configuration.
Figure 5. (Top) High-temperature *in-situ* X-ray diffraction patterns, showing the transformation of powdered sample of $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ sealed into evacuated silica capillary. The “waterfall” plot shows the evolution of powder XRD patterns with the change in temperature from room temperature to 873 K followed by subsequent cooling to room temperature. The temperature regions with distinct phase contributions are highlighted in blue/yellow/purple/red/orange; (bottom) Selected high temperature powder X-ray diffraction patterns showing the products of decomposition/transformation of the $HT$-$Na_{1-x}Zn_{4-y}Sb_3$ at different temperatures. Selected groups of peaks as “fingerprints” of the ternary and binary phases are highlighted: green (143) – NaZn$_4$Sb$_3$; blue ($HT$) – $HT$-$Na_{1-x}Zn_{4-y}Sb_3$; orange (111) – NaZnSb; grey – ZnSb; 122 – “NaZn$_2$Sb$_2$”.
Figure 6. Schematic of the compositional ternary phase diagram for Na–Zn–Sb. Compositional shift along the line of transformation from NaZn$_4$Sb$_3$ (blue circle) and HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ (red circle) during heating in silica capillary. The 1:4:3 composition of NaZn$_4$Sb$_3$ is being shifted during heating due to Na/Zn elimination, therefore the HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase with Na/Zn depleted composition can be stabilized. The initial composition of the sample of HT-Na$_{1-x}$Zn$_4$Sb$_3$ phase prepared by quenching during its heating is shifted even greatly, and then unknown phase referred as “NaZn$_2$Sb$_2$” shows up on the phase equilibria.

Figure 6 represents schematically a compositional shift from NaZn$_4$Sb$_3$ to the HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ and finally to the “new phase” as a result of a continuous Na/Zn elimination during heating. Upon heating, NaZn$_4$Sb$_3$ transforms to HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ and with further heating, i.e. further Na/Zn elimination, NaZnSb appears on phase equilibria. The composition of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$ phase is already Na/Zn depleted compared to that of NaZn$_4$Sb$_3$, therefore upon heating of HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3$, composition further shifts allowing for the crystallization of a “NaZn$_2$Sb$_2$” phase together with considerable amount of binary ZnSb, indicating considerable deviation from initial 1:4:3 composition.

**Elemental analysis of NaZn$_4$Sb$_3$ and HT-Na$_{1-x}$Zn$_{4-y}$Sb$_3**. Scanning electron microscopy (SEM) images using back-scattered electrons (BSE) and secondary electrons (SE) modes were collected for the polished pellets sintered by SPS for both NaZn$_3$Sb$_3$ and the HT-phase (Figure 7). Compositions were determined by energy-dispersive X-ray (EDX) analysis using 8–11 different areas for each sample. The elemental
distribution appears to be homogeneous, and the average compositions were found to be \( \text{Na:Zn:Sb} = 1.83(9):3.66(8):3.00(9) \) for \( \text{NaZn}_4\text{Sb}_3 \) and \( \text{Na:Zn:Sb} = 1.50(9):3.5(1):3.00(9) \) for \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \) phase, respectively. \( \text{Na/Zn} \) is overestimated because of the overlap between \( \text{Na–K} \alpha \) and \( \text{Zn–L} \alpha \) lines, leading to the difficulties in deconvoluting \( \text{Na} \) and \( \text{Zn} \) characteristic lines in the EDX spectrum. Similar inconsistency was seen for the stoichiometric \( \text{NaZnSb} \), with \( \text{Na:Zn:Sb} \) ratio as determined by EDX 1.3:1:1 [20]. More importantly, the compositions determined by EDX analysis indicates the lower \( \text{Zn} \) and \( \text{Na} \) content in the case of \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \) phase as compared to \( \text{NaZn}_4\text{Sb}_3 \), which is consistent with the structure of \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \) determined from SC XRD data as well as \( \text{Na/Zn} \) depleted composition required for its synthesis.

Figure 7. Scanning electron microcopy (SEM) images obtained in back-scattered electrons (BSE, left) and secondary electrons (SE, right) modes for the samples of \( \text{NaZn}_4\text{Sb}_3 \) (top) and \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \) (bottom) prepared via hydride route and further densified by SPS. The compositions of \( \text{NaZn}_4\text{Sb}_3 \) and \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \) phases determined by EDXS and averaged for the 8–11 different areas of each sample.

**Low-temperature transport properties of \( \text{NaZn}_4\text{Sb}_3 \) and \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \).** The temperature dependence of thermoelectric properties (Figure 8) in the 10–300 K temperature range has been measured for the SPS sintered pellets of \( \text{NaZn}_4\text{Sb}_3 \) (compactness of 85%; 7 wt. % of ZnSb impurity) and \( HT-\text{Na}_{1-x}\text{Zn}_{4-y}\text{Sb}_3 \).
γSb₃ (compactness 81%). Electrical resistivities for both compounds are slightly temperature dependent but exhibit different types of behavior with increasing temperature. The electrical resistivity of the NaZn₄Sb₃ decreases from 2400 mΩ·cm to 1200 mΩ·cm with increasing temperature, indicative of heavily doped semiconductor. On the other hand, the electrical resistivity of HT-Na₁₋ₓZn₄₋ₓSb₃ phase is overall ~2 orders of magnitude lower than its NaZn₄Sb₃ counterpart and increases from 33 mΩ·cm to 36 mΩ·cm with increasing temperature, dependence similar to that of a metal.

Both materials have positive Seebeck coefficients which steadily increase with temperature up to 40 and 50 µV·K⁻¹ at 300 K for HT-Na₁₋ₓZn₄₋ₓSb₃ and NaZn₄Sb₃ phases, respectively. This is consistent with p-type and holes as charge carries. Lower overall Seebeck coefficient for HT-Na₁₋ₓZn₄₋ₓSb₃ and lower electrical resistivity with the metal-like temperature dependence agree with its more metallic character, compared to NaZn₄Sb₃. Furthermore, the Na/Zn deficiency in HT-Na₁₋ₓZn₄₋ₓSb₃ would be responsible for more metallic nature of HT-Na₁₋ₓZn₄₋ₓSb₃ as compared to formally charge-balanced Na⁺(Zn²⁺)₄(Sb⁻³)₃. Two orders of magnitude difference in resistivity for NaZn₄Sb₃ and HT-Na₁₋ₓZn₄₋ₓSb₃ and a subtle difference in Seebeck coefficients suggests that the variation in band structure plays a significant role in determining electronic transport of these structurally different and compositionally similar compounds.

The total thermal conductivity κ_{total} has contributions from charge carriers, κₑ (electronic thermal conductivity), and a lattice, κₐ (the lattice thermal conductivity): κ_{total} = κₑ + κₐ = LT/ρ + κₐ, where L is the Lorenz number and ρ is resistivity. For the metals and degenerate semiconductors with high carrier concentrations, Lorenz number approaches the Sommerfeld limit, \( L = 2.45 \times 10^{-8} \text{ W} \cdot \Omega \cdot \text{K}^{-2} \) (free electron model). The \( L \) estimated using experimental Seebeck coefficients [67] yields similar values of \( L \) within the 2.15 – 2.48 \times 10^{-8} \text{ W} \cdot \Omega \cdot \text{K}^{-2} range for HT-Na₁₋ₓZn₄₋ₓSb₃ and NaZn₄Sb₃ phases in 300–10 K temperature range. Thus, the conservative value of \( L = 2.45 \times 10^{-8} \text{ W} \cdot \Omega \cdot \text{K}^{-2} \) was used. The estimated contribution of electronic thermal conductivity into total thermal conductivity is less 0.1% and less the 2.5% of for NaZn₄Sb₃ and HT-Na₁₋ₓZn₄₋ₓSb₃ phases, respectively. The thermal conductivity of both phases increases with temperature from 0.2 W·m⁻¹·K⁻¹ to 0.9 W·m⁻¹·K⁻¹ at 300 K. Both NaZn₄Sb₃ (\( N_{\text{cell}} = 16 \) atoms; \( V_{\text{cell}} = 394.2 \text{ Å}³ \)) and structurally more complex HT-Na₁₋ₓZn₄₋ₓSb₃ (\( N_{\text{cell}} = 192 \) atoms; \( V_{\text{cell}} = 5986.1 \text{ Å}³ \)) have low thermal conductivity. The layered structure of NaZn₄Sb₃ may favor a high density of stacking faults similar to the SrZnSb₂, where the boundary scattering was found to reduce thermal conductivity by approximately 30% at room temperature as compared to structurally related SrZn₂Sb₂ [31-32]. Additionally, the low thermal conductivity could partially be attributed to the lower pellet densities of measured samples (81% and 85%). Moreover, both compounds are lacking the peak in thermal conductivity at lower temperatures. Such a peak is typical for temperature dependence of thermal conductivity of crystalline insulating-semiconducting solids [68-69].
Such “glass-like” temperature dependence of thermal conductivity, typical for amorphous materials, suggests that the disordered complex crystal structure as in $HT$-$Na_{1-x}Zn_{4-y}Sb_3$, and “rattling” of Na atoms in the interlayer space in the crystal structure of NaZn$_4$Sb$_3$ (Na atom has large ADPs, Table 2) can be responsible for the phonon scattering at low temperatures.

The thermoelectric figure-of-merit $zT$ at room temperature amounts to $7.3 \times 10^{-5}$ for NaZn$_4$Sb$_3$ and to $1.4 \times 10^{-3}$ for $HT$-$Na_{1-x}Zn_{4-y}Sb_3$. The low $zT$ for both compounds can be attributed to low Seebeck coefficient and high electrical resistivity, especially in the case of formally charge balanced NaZn$_4$Sb$_3$. Aliovalent substitutions in NaZn$_4$Sb$_3$ compound (for instance Na for Ca) may lead for increase of carrier concentration and decrease of its high resistivity.
Figure 8. Temperature dependence of transport properties for NaZn₄Sb₃ (blue) and HT-Na₁₋ₓZn₄₋ₓSb₃ (red): (top) electrical resistivity; (middle) Seebeck coefficient, (bottom) thermal conductivity (the estimated electronic thermal conductivity contribution is negligible less than 0.1% for NaZn₄Sb₃ phase and less than 2.5% for HT-Na₁₋ₓZn₄₋ₓSb₃ phase).

Conclusions.

In-situ synchrotron powder diffraction analysis provided a “panoramic view” on the ternary phases in the Na–Zn–Sb system. Two compositionally similar, but structurally different phases NaZn₄Sb₃ and HT-Na₁₋ₓZn₄₋ₓSb₃ were detected on phase equilibria below and above 736 K, respectively. The HT-phase can be prepared by quenching samples from high temperatures only if Na- and Zn-depleted composition is used for synthesis. Moreover, in-situ powder X-ray diffraction experiments show an additional ternary phase, stabilized due to considerable Na/Zn elimination under vacuum at elevated temperatures. The structure and properties of this phase will be reported in due course. Transport properties of NaZn₄Sb₃ and HT-Na₁₋ₓZn₄₋ₓSb₃ phases show low thermal conductivities at room temperature of 0.9 W·m⁻¹·K⁻¹. Both polymorphs exhibit moderate positive Seebeck coefficients of 40-50 µV·K⁻¹ at 300 K, indicative of p-type conduction. The observed resistivities differs by two orders of magnitude, possibly indicating complex transport behaviors. The presented here synthetic hydride approach coupled with in-situ high-temperature powder X-ray diffraction allows for the fast compositional and temperature screening of the phase space, leading to the discovery of the phases, stable in a narrow compositional and temperature range.

Associated content.

Supporting Information. Additional Tables with interatomic distances, Rietveld refinement plots and Tables with parameters of XRD data collection and refinement can be found in the Supporting Information. This material is available free of charge via the Internet at http://pubs.acs.org.

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References


Panoramic Hydride Synthesis