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Analysis of transmit beamforming and fair OFDMA scheduling

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Analysis of transmit beamforming and fair OFDMA scheduling

by

Alex Leith

A thesis submitted to the graduate faculty
in partial fulfillment of the requirements for the degree of
MASTER OF SCIENCE

Major: Electrical Engineering

Program of Study Committee:

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2008

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ABSTRACT

Two promising candidates for beyond 3rd generation (B3G) and 4G communication standards are multiple input multiple output (MIMO) and orthogonal frequency division multiple access (OFDMA) systems. OFDMA is a new technique that enables multiple users to transmit parallel data streams, allowing a much higher data rate than conventional systems, such as time division multiple access (TDMA) or code division multiple access (CDMA). Another research topic involving MIMO systems use antenna arrays at both the transmitter and the receiver. By using multiple antennas, the transmitter can adapt to the channel as it varies across time. This is accomplished by using a codebook of beamforming vectors which are known to both the transmitter and receiver. As the receiver acquires information about the channel, it calculates which beamforming vector matches the channel the best. The receiver then sends back the index of that vector to the transmitter. The symbol being transmitted is multiplied by the beamforming vector and sent over the channel, this is known as transmit beamforming (TB).

Transmit beamforming can not only increase performance in wireless MIMO systems, but also add increased performance when put in combination with other MIMO systems like spatial multiplexing and space time codes. TB has advantages over other MIMO schemes because by measuring the channel, one can use adaptive modulation techniques to achieve a coding gain not obtainable without channel state information (CSI). Past research assumed the feedback channel was error free and had no delay. This isolated the effects of finite rate feedback. We assume there is delay in the

feedback channel along with imperfect channel estimation (ICE) at the receiver. We will show how detrimental these effects can be to TB's performance and can not be ignored.

OFDMA is a technique used to allow multiple users to communicate more reliably. This is possible because OFDMA utilizes CSI which can increase capacity, and decrease the total transmission power. With the amount of data being transmitted over wireless channels today, the need for faster, more efficient transmission techniques becomes essential. OFDMA uses adaptive modulation based on instantaneous channel conditions, to assign subcarriers to each user and allocate power to each carrier. Past research has focused on many different methods for OFDMA, using sum rate maximization techniques without fairness, or using short term fairness to improve the Quality of Service (QoS) to each mobile station. This thesis will address important issues that are missing, such as weighted SNR (w-SNR) based ranking with adaptive rate tracking to achieve long term rate proportional fairness (RPF) for downlink OFDMA. Long term RPF is less strict and performs better than short term RPF which is achieved through w-SNR ranking. The weight calculation can be implemented both online or offline. If channel statistics are known offline, a fixed weight vector can be calculated and used to allocate resources to each MS. When channel statistics are unknown, adaptive rate tracking can be used to calculate the weight vector online. Then resources are allocated based on each MS's weight factor. This sum rate maximization method with long term RPF and adaptive rate tracking has many advantages over traditional schemes, including ease of implementation, allowing a higher data rate with fairness, and allowing for distributed scheduling.

CHAPTER 1. Introduction

1.1 Background Information

Wireless Communication systems have been steadily evolving in order to improve performance for users. Two promising candidates for beyond 3rd generation (B3G) and 4G communication standards are multiple input multiple output (MIMO) and orthogonal frequency division multiple access (OFDMA) systems. OFDMA is a new technique that enables multiple users to transmit parallel data streams, allowing a much higher data rate than conventional systems, such as time division multiple access (TDMA) or code division multiple access (CDMA). This, in turn, could translate into better cellular coverage and fewer dropped calls. Another research topic involving MIMO systems use antenna arrays at both the transmitter and the receiver. Multiple input refers to multiple antennas at the transmitter, and multiple output refers to multiple antennas at the receiver. In addition, single input and single output refer to a single antenna at the transmitter and receiver, respectively. By using multiple antennas, the transmitter can adapt to the channel as it varies across time. This is accomplished by using a codebook of beamforming vectors which are known to both the transmitter and receiver. As the receiver acquires information about the channel, it calculates which beamforming vector matches the channel the best. The receiver then sends back the index of that vector to the transmitter. The symbol being transmitted is multiplied by the beamforming vector and sent over the channel, this is known as transmit beamforming (TB). The research in this thesis will investigate both OFDMA

and TB.

MIMO technology is essential in order to achieve high spectrum efficiency, enlarge system coverage, and support high data rates [1]. With these multiple antenna systems, several different techniques can be implemented when transmitting data to the receiver. The model for MIMO systems is shown in Figure 1.1. Along with MIMO, some other multiple antenna systems are multiple input single output (MISO), or single input multiple output (SIMO). One technique associated with MIMO systems is spatial multiplexing (SM).

Spatial multiplexing (SM) uses a demultiplexer to divide the data into N_t different streams, where N_t equals the number of transmit antennas. Each antenna then transmits a different symbol. This technique uses the allowed spectrum much more efficiently. STCs are less efficient because they only transmit one symbol per time slot.

The STC technique involves three steps: encoding and transmission of data at the transmitter, combining the data at the receiver, and the decision rule for detection. Since the same signal is encoded differently, the receiver will get a redundant version of it [1, 2]. The receiver can use this redundancy to correctly detect the transmitted data; this is called receive diversity.

Receive diversity is very important because wireless channels suffer from a variety of obstructions and refractions that cause scattering of the signals. The signals are also distorted by noise from other signals being transmitted, and interference. If all these distortions are severe enough, it is then impossible for the receiver to determine the transmitted signal. This is why having multiple copies help in determining what was transmitted [3]. Another way to transmit data is to use transmit beamforming.

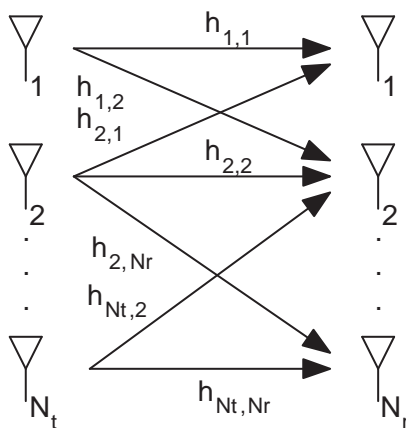


Figure 1.1 MIMO structure with N_t transmit antennas and N_r receive antennas

1.1.1 Transmit Beamforming

Transmit beamforming is very important to wireless communications because given accurate channel conditions it can enhance performance of SM,STCs, or stand alone. Refer to Table 1.1 for a list of abbreviations. TB uses information that the receiver acquires about the channel conditions.

Table 1.1 List of abbreviations

MIMO	Multiple Input Multiple Output
MISO	Multiple Input Single Output
SIMO	Single Input Multiple Output
TB	Transmit Beamforming
OFDMA	Orthogonal Frequency Division Multiple Access
STC	Space Time Codes
SM	Spacial Multiplexing
CSI	Channel State Information
ICE	Imperfect Channel Estimation

The channel measurements can be obtained by sending out known pilot symbols periodically from the transmitter to the receiver. The receiver can then use these pilot symbols to estimate the channel at different time intervals. This is known as pilot symbol-assisted modulation (PSAM), and is a good technique for rapidly fading environments [4].

With TB for MISO systems, the different antenna elements at the transmitter are designed to combine at the receiver adding a diversity gain of N_t over SISO systems. However, this gain requires that the transmitter have accurate knowledge of the channel, because TB cannot be used to achieve capacity unless there is accurate CSI available [5, 6].

Once the receiver knows the channel information, it can feedback this information to the transmitter. The transmitter uses that information to best adapt to the channel. In order to send all the information back, a large amount of bandwidth is necessary. This is not very feasible in practical systems. The information needs to be compressed due to the bandwidth constraint, and then sent back. This process is called finite rate feedback. By increasing the number of feedback bits, it is possible to increase the information supplied to the transmitter, which will lower the bit error rate (BER) of the system. This works well with the first couple bits, but then the increase is minimal with each subsequent bit [7]. Ideally, this feedback channel would be an error free, no-delay channel, but that is not true in practice. Past research has only dealt with this type of feedback channel, along with perfect CSI at the receiver.

Drawbacks to Transmit Beamforming

Each transmit antenna is associated with a single channel, or group of channels; some channels are better than others. The receiver can acquire information about the channel as it varies in time. There are two examples of this. One is when the receiver knows the channel perfectly; this is referred to as the perfect channel state information (CSI). Another example is when the receiver can only estimate the channel. This is the most practical case, and is called imperfect channel estimation (ICE). Having ICE at the receiver is more practical because having perfect CSI would either overload the receiver, or the channel could fluctuate too rapidly to get an accurate estimate. There are different types of ICE. One method is when the channel distribution is modeled

based on $\mathbf{h} \sim \mathcal{N}(\boldsymbol{\mu}, \alpha\mathbf{I})$, where the mean $\boldsymbol{\mu}$ is the estimate of the channel, and α is the variance of the estimation error. A second approach is used when the channel is varying too rapidly to obtain any instantaneous CSI, only channel statistics can be obtained. Therefore, the channel is modeled based on $\mathbf{h} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Sigma})$. Here, since the channel is changing too rapidly to acquire any accurate information, only the covariance matrix $\boldsymbol{\Sigma}$ is used because its change is much slower [8, 9]. The benefit of mean or covariance ICE is that capacity increases with more information about the channel [10].

CSI is essential for TB because the transmitter requires accurate knowledge of the channel. Some errors associated with TB include ICE, quantization errors, delays during feedback, and errors caused by the feedback channel. Quantization errors are incurred from using a finite number of bits to feed back the channel estimate to the transmitter. Moreover, if the channel varies too rapidly, the channel will have changed, and the feedback information becomes outdated by the time the transmitter is able to use that information. Lastly, any errors induced by the feedback channel itself will cause problems [9].

If the receiver does not know the actual channel realization, but only knows the channel covariance matrix $\boldsymbol{\Sigma}$, then it has no information about the attenuation of each channel. It is only aware of directional information that can instead be used based on the eigenvalues of $\boldsymbol{\Sigma}$ [11]. By using eigenvalue decomposition of $\boldsymbol{\Sigma}$, the different eigenvalues for each channel can be obtained. Beamforming along the largest of these eigenvalues is optimal for increasing capacity. TB achieves capacity as the quality of feedback improves in the mean feedback case, or the variation between eigenvalues of the channel covariance matrix increases for covariance feedback [8]. In addition, by increasing the number of antennas, TB schemes are better equipped to handle fading channels [12–16].

Proposed method for Transmit Beamforming

The proposed method will take the delay into account, along with ICE at the receiver. If there is no delay, the transmitter would have instantaneous knowledge of the channel, and could adapt perfectly to it. However, with the delay and ICE, the transmitter only knows past information about the channel estimates. It then has to use that knowledge to adapt to the channel. This knowledge will cause some errors because the channel changes with time. If the channel was not time varying, the delay would not affect the performance. The outdated and imperfect CSI can be very detrimental to the performance of the system, and needs to be taken into account. When designing practical systems using TB, if the effects of delayed feedback and ICE are neglected, the system could simply perform poorly, or in the worst case, completely break down. Transmit beamforming has been proven to achieve optimal performance in MISO systems based on signal to noise ratio (SNR) [17]. The second part of this thesis discusses Orthogonal Frequency Division Multiple Access (OFDMA).

1.1.2 Orthogonal Frequency Division Multiple Access

There have been several different models implemented to allow for multiple access, such as TDMA, frequency division multiple access (FDMA), and CDMA. TDMA allocates different time slots to each user. FDMA works in a similar manner by allocating a different frequency band to each user. CDMA assigns a different code to each user. This allows multiple users access to the same frequency band and time slot by encoding their transmissions. This works well because all other users look like noise to everyone else. However, this type of flat fading environment cannot support high data rates. These types of problems need to be addressed in 4G systems, in which not only voice is being transmitted but also multimedia services such as MPEG video, FTP, HTTP, and other data types as well [18, 19].

Wideband CDMA (WCDMA) release 4 is intended to account for a wide range of

these services. The data rate associated with WCDMA is still too low. Therefore, an upgrade to WCDMA called high speed downlink packet access (HSDPA) provides a much higher data rate up to 14 Mbps, which makes it suitable for real time services [20–22]. However, the Korean standard for wireless broadband internet (WiBro) utilizes OFDMA and outperformed HSDPA by providing a higher data rate transmission in multipath fading channels [22].

OFDMA is a technique used to allow multiple users to communicate more reliably. This is possible because OFDMA utilizes CSI which can increase capacity, and decrease the total transmission power. With the amount of data being transmitted over wireless channels today, the need for faster, more efficient transmission techniques becomes essential. OFDMA allows users to compete for resources to help eliminate resources from being wasted. However, as the number of users in the system grows each year, more people are battling to use the allocated bandwidth. That is why it is not only important for future techniques to be efficient, but also fair. OFDMA could be unfair to the users with weaker channels depending on how resources are allocated, which is why rate proportional fairness (RPF) methods are being designed. Past research involving short term RPF like in generalized processor sharing (GPS) assigns each user a fixed weight. Then resources are allocated based on each user's weight factor [23]. This method achieves short term fairness for each individual time slot, which is very strict and unnecessary. The proposed method in this thesis achieves long term fairness by assigning a weight vector to each user based on averaging their rate over multiple time slots. Also, by utilizing adaptive rate tracking these weight factors for each user can be updated online based on different quality of service requirements. Therefore, research in finding the optimal solution to this fairness problem is essential and will be discussed.

OFDMA System Model

OFDMA uses adaptive modulation based on instantaneous channel conditions, to assign subcarriers to each user and allocate power to each carrier. Based on this, the data rate is greatly improved over static resource allocation techniques. Different subcarriers experience different channel fades, which means they can transmit at different data rates as well. However, the more fading the channel experiences, results in higher gains being achieved.

In OFDMA, the allocated frequency band may be equally divided up into N different subcarriers. All users are possible candidates for resource allocation, and are able to transmit using all time slots. The model for OFDMA is shown in Figure 1.2.

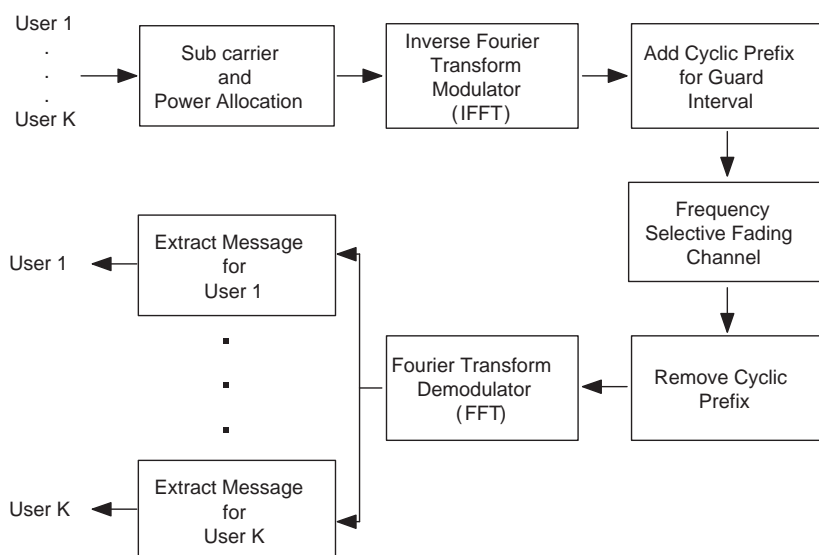


Figure 1.2 Block diagram for OFDMA downlink system model

There can be any number of users in the system. Each user feeds their bit stream into the subcarrier and power allocation block. The receiver knows the channel conditions for each user, and can assign the carriers to maximize the total data rate of the system. Once a set of subcarriers has been assigned to each user, then power can be allocated to each carrier. The symbols are transformed into the time domain using the inverse Fourier transform method (IFFT). Next, a cyclic extension is added

as a guard interval, which ensures orthogonality among the carriers. The signals are then transmitted across the channel. At the k^{th} user's receiver, the guard interval is removed to eliminate the intersymbol interference (ISI). This allows for higher data rates because ISI distorts the signals making it very difficult for the receiver to detect what was transmitted. The receiver then transforms the signals back into the modulated symbols using the Fourier transform demodulator. Lastly, based on the carrier set for the k^{th} user, the message is pieced back together [24]. This scheme uses dynamic allocation of resources and is optimal over static resource allocation.

Static resource allocation techniques result in poor performance because they do not take CSI into account [25]. As a result, a large portion of carriers are wasted because no other users can access them. Assigning a channel resources, whether it be a time slot or frequency band to each user is not optimal. Using a dynamic resource allocation approach like in OFDMA, causes less waste and achieves a higher performance.

OFDMA Cellular Channel Model

The way mobile stations (MSs) communicate with the base station (BS) can be seen in Figure 1.3. The uplink channel can be used to feedback channel conditions to the BS. Since different users are located in different positions, their channel conditions are independent of each other. Therefore, a scheduler can select which MSs are allocated which resources to maximize the sum data rate, which is referred to as selective multiuser diversity (SMuD). In almost all wireless applications, reliable data rates are the most important factor in measuring the satisfaction of users [26]. There are many advantages to OFDMA, such as high spectral efficiency, simple implementation by FFT, low receiver complexity, and high data rate transmission over multipath fading channels [1].

OFDMA is divided up into two steps. First, carriers are assigned to each user,

and second, power is allocated among the carriers. This provides the maximum total data rate for the system. It was proven in [27] that exclusive carrier assignment maximizes the data rate for downlink channel models over shared carrier allocation. When multiple users share a specific carrier in shared carrier allocation, they end up interfering with each other. As one user increases its transmit power, the interference to other users is increased as well. The added interference makes this type of carrier assignment suboptimal.

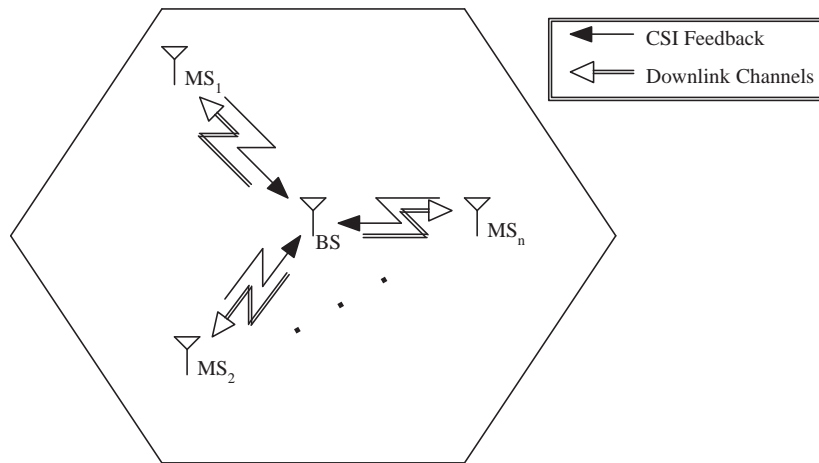


Figure 1.3 OFDMA cellular channel model

The optimal method for OFDMA is to jointly allocate carriers and power. Joint allocation methods are more complex for the uplink case than the downlink case because of the different power constraints at the mobile stations. The method found in [28] addresses this by calculating the data rate for each user and allocating resources to the user with the largest data rate. This method may be optimal in sum rate, but it is also unfair.

Proportional Fairness Techniques

In rate adaptive resource allocation, subcarriers and power are distributed in order to achieve the maximum performance while maintaining proportional fairness among

users. There are two classes of optimization techniques which have been proposed in OFDMA dynamic resource allocation literature. Margin adaptation (MA) achieves the minimal overall transmit power given the constraints on the user's data rates and error rates. Rate adaptation (RA) maximizes the sum capacity with a total transmit power constraint. In studying RA optimization techniques, several algorithms have been proposed. Selective multiuser diversity with absolute SNR based ranking, referred to as a-SNR SMuD OFDMA, is considered to be the conventional method that does not take fairness into account. This can often provide an upper bound for proportional fairness methods. Another method, called the Min-Max method, maximizes the worst user's capacity, but the overall capacity is sacrificed [29, 30]. There needs to be a balance between achieving maximum sum capacity and fairness.

There are several different techniques to ensure proportional fairness. For example, GPS scheduling can achieve a maximum sum rate while providing short term fairness. In [23], GPS assigns each user a fixed weight instead of a fixed bandwidth, then dynamically allocates carriers to each user according to their weight and traffic load. Each user is guaranteed a minimum bandwidth proportional to its weight. If a user does not use all of its guaranteed bandwidth, the unused portion is distributed to other users in proportion to their weights. However, it is difficult to implement in practice because of the following reasons. (1) Due to channel fading, the actual number of subcarriers the system can support can be less than the theoretical number of subcarriers because of poor channel gains. (2) If the number of backlogged sessions becomes larger than the number of subcarriers, the system may not be able to allocate the bandwidth to each user that GPS scheduling guarantees at each time slot.

Short term fairness ensures fairness for each individual time slot. Long term fairness ensures a uniform average channel access probability (AAP), in which all users have an equal number of assigned carriers over multiple time slots. Therefore, short term fairness may be too strict and is unnecessary. Instead, long term fairness tech-

niques are adequate and perform better. In [31] and [32] a long term fairness approach is taken called normalized SNR (n-SNR) SMuD. The normalized SNR equals the instantaneous SNR divided by the average SNR. Unlike the a-SNR SMuD, which uses the instantaneous SNR to assign carriers, the n-SNR scheme assigns carriers to the users with the highest normalized SNR. Next, power can then be allocated to each carrier.

The transmitter does not have infinite power for each channel, so there are a couple of options to allocate power. One option is to simply divide the power equally among each channel, whether the channel is reliable or not. This is called equal power allocation (EPA), which is not optimal. By giving the poor channels the same amount of power as the good channels, a large amount of power is being wasted. A better approach is to give the better channels more power, and give the degraded channels less power or no power at all. Using the Lagrangian method to solve the maximization problem with respect to the power constraint, and solving the Karush-Kuhn-Tucker (KKT) conditions, gives the optimal threshold. If a channel SNR does not reach this threshold, then no power is allocated, and that channel is simply turned off. This scheme is known as water filling (WF), because the better the channel, the more power one can pour into it. WF is optimal for all SNR ranges [26, 28]. The proposed method below takes a different approach to achieve long term fairness.

Proposed Method for OFDMA

The proposed method uses weighted SNR (w-SNR) based ranking with adaptive rate tracking to achieve long term RPF for downlink OFDMA. There are several different methods to obtain the optimal weight vector. (1) An offline algorithm is provided to calculate the optimal weight factor when channel statistics are known. (2) An online algorithm which utilizes adaptive rate tracking without future CSI to find the optimal weight vector. (3) Adaptive rate tracking with future CSI is used

to obtain the optimal weight vector online as well. Next, depending on the different users' quality of service (QoS) requirements, a target RPF is obtained. The weight factors for all users are then calculated based on this target RPF by any of the three methods described above. Subcarriers and power are then allocated based on each user's weight factor. This sum rate maximization method with long term RPF and adaptive rate tracking has many advantages over traditional schemes, including ease of implementation, allowing a higher data rate with fairness, and allowing for distributed scheduling.

Short term RPF schemes have a fixed weight factor where users are allocated resources based on this weight factor alone. This happens regardless of their channel conditions. A large amount of waste can occur because the channel cannot support the data rate. The reverse is also true, a user could have a very good channel, but is not allowed to utilize it because their weight factor is set to low. The proposed adaptive rate tracking method takes temporal diversity into consideration allowing more resources to be allocated beyond what is allowed by the user's weight factor. This is true if the user's channel becomes better than their average value. The opposite also holds, where if the user channel becomes poorer than their average value, less resources are allocated. The following chapters are organized as follows.

1.2 Organization of Thesis

Chapter 2 focuses on transmit beamforming. It analyzes some MIMO techniques and compares past TB research with the proposed method. Chapter 3 analyzes OFDMA systems for the downlink case. It compares different approaches to OFDMA and different resource allocation methods to the proposed method as well. Chapter 4 focuses on future work along with summarizing the results presented throughout this work.

Notation: Bold upper and lower case letters denote matrices and column vectors,

respectively. $|\cdot|$ and $\|\cdot\|$ denote absolute value and a vector norm, respectively; $(\cdot)^*$, $(\cdot)^T$, and $(\cdot)^H$ denote the conjugate, transpose, and Hermitian transpose, respectively. $E\{\cdot\}$ denotes expectation; \mathbf{I}_N denotes the identity matrix of size N ; \mathcal{C}^N stands for an N dimensional complex vector space; $\mathcal{CN}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$ denotes the complex Gaussian distribution with mean $\boldsymbol{\mu}$ and covariance $\boldsymbol{\Sigma}$.

CHAPTER 2. Transmit Beamforming

2.1 Introduction

Transmit beamforming can not only increase performance in wireless MIMO systems, but also add increased performance when put in combination with other MIMO systems like SM and STC [33, 34]. TB has advantages over other MIMO schemes because by measuring the channel, one can use adaptive modulation techniques to achieve a coding gain not obtainable without CSI. It is difficult to use TB in a broadcast mode because TB is designed to transmit in a single direction like in point to point links. Therefore, this chapter reviews SM,STCs, and past schemes involving TB. Then we focus on the proposed method, TB with limited delayed feedback and imperfect channel estimation. Past research assumed the feedback channel was error free and had no delay. This isolated the effects of finite rate feedback. We assume there is delay in the feedback channel along with ICE at the receiver. We will show how detrimental these effects can be to TB's performance and can not be ignored.

Both the transmitter and receiver have knowledge of the codebook that will be used for TB. Once the receiver knows the channel, it will search through the codebook to find the best beamforming vector and feedback the index of that vector to the transmitter. The codebook is a matrix of size $N_t \times N$, where N_t is the number of transmit antennas and N is total number of beamforming vectors. If B is the number of bits fed back, then $N = 2^B$. Basically there are three different techniques that are used with beamforming codebooks.

The first technique is called selection diversity transmission (SDT). This is where the number of beamforming vectors equals the number of transmit antennas. The codebook in this case is just the identity matrix \mathbf{I}_{N_t} . Here only the strongest channel is chosen to transmit and all other antennas are turned off. The next technique is called equal gain transmission (EGT). In this approach, the beamforming vectors are divided up equally among them based on the number of transmit antennas, where each beamforming vector $\mathbf{w} = \frac{1}{\sqrt{N_t}}\mathbf{1}_{N_t \times 1}$. The last approach is called maximum ratio transmission (MRT). Here each beamforming vector can basically be any unit vector. Transmitter complexity increases with these approaches with MRT being the most complex, but system performance increases as well [35]. MRT is assumed throughout this thesis when N_t is smaller than N . Besides TB, two additional schemes involving MIMO systems are spatial multiplexing and space time codes, as discussed next.

2.2 Some Available MIMO Schemes

Spatial multiplexing and space time codes are two different ways to transmit data over wireless channels. Spatial multiplexing utilizes all degrees of freedom (DoF) of the channel, which uses the spectrum more efficiently. STCs transmit encoded data over multiple antennas. This adds a diversity gain (G_d) to the system, and the receiver has a better chance of properly decoding the message. Both schemes are important in communications.

2.2.1 Spatial Multiplexing

Spatial multiplexing takes a stream of symbols and splits them up into smaller independent streams. The number of streams depends on the number of transmit antennas. Each antenna transmits a different stream. By increasing the numbers of transmit antennas and receiver antennas in the system, there is an increase in DoF.

Degrees of freedom refer to the number of signals that can be reliably distinguished at the receiver [36,37].

$$\text{DoF} = \min(N_t, N_r) \quad (2.1)$$

Spatial multiplexing starts off by sending a bit stream through an encoder and converting them to a stream of complex symbols. Those symbols are then sent through a demultiplexer. The demultiplexer divides the bit stream up into N_t independent data streams, and sends them to each transmit antenna. Each independent data stream is considered a layer [38]. There are three different ways to transmit using SM: vertical Bell Labs layered space time (V-BLAST), horizontal BLAST (H-BLAST), and diagonal BLAST (D-BLAST) (see Figure 2.1).

V-BLAST is a popular scheme because it is simple to implement. Each transmit antenna sends an independent data stream or layer over the channel. H-BLAST can be either coded or uncoded. If H-BLAST is uncoded it simply reduces to V-BLAST. Coded H-BLAST is designed in such a way that each transmit antenna's layer interferes with the layers below it, and can not interfere with layers above it. D-BLAST works differently because each of the layers are cycled periodically over each transmit antenna during a specified time slot [39–41].

The model for spatial multiplexing V-BLAST is defined as

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \eta, \quad (2.2)$$

where \mathbf{y} , \mathbf{H} , \mathbf{x} and η are the received signal, channel, data symbols, and additive Gaussian noise matrices, respectively. The received signal, data symbols, and noise matrices are of size $N_t \times 1$. There are several different techniques the receiver can use to decode the data. Maximum likelihood (ML) uses joint decoding which compares all

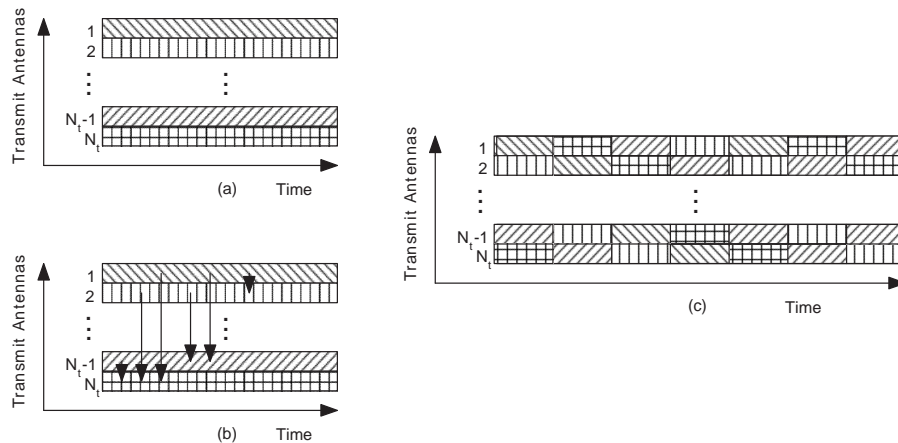


Figure 2.1 Spatial multiplexing models (a) V-BLAST (b) H-BLAST (c) D-BLAST

possible combinations of symbols. Joint decoding makes it optimal, but can become very complex. Another receiver can also be a decorrelator followed by a minimum distance decoder [1, 37]. Decorrelators work by nulling out the effect of the other symbol. Since the receiver has perfect CSI, the decorrelator decodes the received symbol as follows

$$\hat{\mathbf{x}} = (\mathbf{H}^H \mathbf{H})^{-1} \mathbf{H}^H \mathbf{y}. \quad (2.3)$$

Once the symbols are detected, the minimum distance decoder will estimate what was transmitted. One type of STCs called orthogonal space time codes (OSTC) is explained next.

2.2.2 MIMO Orthogonal Space Time Codes

OSTC is another way to use MIMO systems. As the numbers of transmit and receiver antennas increase, so does the diversity gain of the system. The diversity gain is the number of independently faded signal paths between the transmitter and receiver. It is important because it increases performance by minimizing the SER. G_d

is calculated by,

$$G_d = N_t N_r. \quad (2.4)$$

This system starts off again by converting the bit stream into complex symbols. The symbols are then encoded using an Alamouti encoder [2, 37].

Table 2.1 Alamouti scheme

Time slot 1	Time slot 2
x_1	$-x_2^*$
x_2	x_1^*

The encoder transmits signals according to Table 2.1 when two transmit antennas are used. The OSTC model is expressed as,

$$\begin{bmatrix} y_1 & y_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \end{bmatrix} \begin{bmatrix} x_1 & -x_2^* \\ x_2 & x_1^* \end{bmatrix} + \begin{bmatrix} n_1 & n_2 \end{bmatrix}. \quad (2.5)$$

Rearranging (2.5) will give

$$\begin{bmatrix} y_1 \\ y_2^* \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{12}^* & -h_{11}^* \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} n_1 \\ n_2^* \end{bmatrix}, \quad (2.6)$$

which is more intuitive when decoding the transmitted signals at the receiver. The receiver can be a maximum likelihood decoder which takes the received symbols, and using the channel information, decodes them to get the original symbols back. The model for a maximum likelihood decoder is expressed as

$$\hat{\mathbf{x}} = \arg \min \| \mathbf{y} - \mathbf{H}\mathbf{x} \|^2. \quad (2.7)$$

For OSTC the above equation will simplify to

$$\hat{\mathbf{x}} = \mathbf{x} - \frac{\mathbf{H}^H \mathbf{n}}{\|\mathbf{H}\|^2}, \quad (2.8)$$

where $\hat{\mathbf{x}}$ is the decoded received symbols. Since OSTCs transmit an encoded version of the same symbol during each time slot, they only send one symbol per channel use. SM utilizes all the DoF of the channel and sends N_t symbols per channel use. Therefore, SM has a much higher data rate than OSTCs, but since there is no coding at the transmit antennas, the diversity gain only comes from the number of receive antennas. This brings up an interesting point about the tradeoff between the diversity gain and degrees of freedom [37].

Diversity multiplexing tradeoff (DMT) is important to consider when analyzing the performance benefits of MIMO systems. DMT calculates the tradeoff between data rate and reliability. SM utilizes all the DoF which increases the data rate, but the reliability of the system is sacrificed. STCs exploit the diversity gain making them very reliable, but they neglect the DoF of the channel. Therefore, if the system needs to be very reliable it should use as much of the diversity gain as possible. Likewise, if the system can operate at a lower SER than it should use more DoF to increase the data rate [37].

2.3 Past Transmit Beamforming Performance Analysis

Past research involving transmit beamforming assumed perfect CSI at the receiver and finite rate feedback. In [17] the effects of using different numbers of beamforming vectors along with different MISO structures and constellation sizes were studied. Other papers have also investigated TB using a variety of different methods. In [42] SDT was used along with maximum ratio combining at the receiver to analyze the performance based on the SER. In [34] TB was combined with OSTC to investigate

how performance can be improved over conventional OSTC for MIMO systems. In [33] a different approach was used by combining TB with spatial multiplexing which analyzed how using knowledge of the channel could improve performance. In [43] the uplink cellular system is modeled with outdated CSI for the SIMO case. Also in [44], an adaptive modulation scheme is used for MISO systems using channel mean feedback with delay. In adaptive modulation schemes the transmitter not only adjusts the BF vectors, but also the power allocation for each transmit antenna and signal constellation size to maintain a target SER. If the channel is in deep fade, then nothing is transmitted. This type of scheme is less sensitive to channel imperfections than SISO systems, but feedback delay significantly degraded the performance of the system.

In [17], an analytical lower bound was compared to the actual simulated curve. This showed that the analytical lower bound was a tight approximation to the actual SER curve for good beamformers across the entire SNR range. The channels were assumed to be independent and identically distributed (i.i.d.), so the Grassmannian line packing problem has been proven to provide the best beamformers in that case [45].

When designing good beamformers, maximizing the minimum chordal distance between two beamforming vectors is the best option [17, 46]. The chordal distance is defined as

$$d(\mathbf{w}_i, \mathbf{w}_j) = \sin(\theta_{i,j}) = \sqrt{1 - |\mathbf{w}_i^H \mathbf{w}_j|^2}, \quad (2.9)$$

where $\theta_{i,j}$ denotes the angle between \mathbf{w}_i and \mathbf{w}_j . Good beamformers have been designed in [47] for a number of different transmit antennas and codebook sizes. The beamforming codebook, defined as

$$\mathbf{W} = [\mathbf{w}_1 \ \mathbf{w}_2 \ \dots \ \mathbf{w}_N], \quad (2.10)$$

consists of all the TB vectors. For example, the codebook for $N_t = 2$ and $N = 4$ is

$$\mathbf{W} = \begin{bmatrix} -.1612 - j * .7348 & -.5135 - j * .4128 \\ -.0787 - j * .3192 & -.2506 + j * .9106 \\ -.2399 + j * .5985 & -.7641 - j * .0212 \\ -.9541 & .2996 \end{bmatrix}^T. \quad (2.11)$$

When the number of beamforming vectors is equal to the number of transmit antennas, \mathbf{W} simply reduces to the identity matrix of size N_t , \mathbf{I}_{N_t} , which is SDT. Once these codebooks have been designed, the receiver having perfect CSI can compute the optimal beamforming vector. Each beamforming vector is associated with an index identifier, and the index of the optimal beamforming vector is fed back to the transmitter. The transmitter then multiplies the TB vector \mathbf{w} , with the symbol x to be transmitted, and sends that over the channel. The MISO model is made up of N_t transmit antennas and one receive antenna. The received symbol is defined as

$$y = \mathbf{w}^H \mathbf{h} x + \eta, \quad (2.12)$$

where η is complex Gaussian noise. The optimal TB vector is chosen based on the instantaneous SNR for a Gaussian channel. The received instantaneous SNR is given by

$$\gamma = |\mathbf{w}^H \mathbf{h}|^2 \frac{E_s}{N_0}, \quad (2.13)$$

where E_s is the average symbol energy, and N_0 is the variance of the noise. It can be seen from (2.13) that in order to maximize the instantaneous SNR, one needs to maximize $|\mathbf{w}^H \mathbf{h}|$. Therefore, the optimal TB vector is defined as

$$\mathbf{w}_{\text{opt}} = \arg \max_{\{\mathbf{w}_i\}_{i=1}^N} |\mathbf{w}^H \mathbf{h}|^2. \quad (2.14)$$

The performance analysis for the SER with finite-rate feedback is reviewed next. The first step is to identify the instantaneous SER based on a phase-shift keying (PSK) constellation, which is defined as [48]

$$\text{SER}(\gamma) = \frac{1}{\pi} \int_0^{\frac{(M-1)\pi}{M}} e^{-\frac{g_{\text{PSK}}\gamma}{\sin^2\theta}} d\theta, \quad (2.15)$$

where M is the constellation size and $g_{\text{PSK}} = \sin^2(\frac{\pi}{M})$. To find the average SER, the expectation of (2.15) with respect to the channel vector \mathbf{h} needs to be taken. The average SER is defined as $\overline{\text{SER}} = E_{\mathbf{h}}\{\text{SER}(\gamma)\}$. A good approximation for the average SER lower bound is derived in [17],

$$\overline{\text{SER}}_{LB} = \frac{1}{\pi} \int_{\theta=0}^{\frac{(M-1)\pi}{M}} \left(1 + \frac{g_{\text{PSK}}\bar{\gamma}}{\sin^2\theta}\right)^{-1} \left[1 + \left(1 - \left(\frac{1}{N}\right)^{\frac{1}{N_t-1}}\right) \frac{g_{\text{PSK}}\bar{\gamma}}{\sin^2\theta}\right]^{1-N_t} d\theta. \quad (2.16)$$

This equation has proven to be a very good lower bound for the average SER as the graphs in [17] show for different N_t and N . As the number of vectors N increases, the curve becomes closer to the case of perfect CSI at the transmitter (CSIT). Having two bits provides adequate feedback for $N_t = 2$, therefore, adding an additional bit does not yield a significant improvement in performance.

2.4 Transmit Beamforming with ICE, Delayed and Limited Feedback

In this section, the SER will be analyzed based on delayed and limited feedback. In [49] it is proven that as the delay increases, the SER increases as well, causing a significant loss in performance. While these results have been studied in the literature, they assumed perfect CSI at the receiver. While perfect CSI is often not possible in practice due to channel fading and interference, the effects of ICE have not been adequately studied and need to be considered [50]. We will show that ICE can cause a

loss in SNR at the receiver and cause the receiver to select a lower quality beamforming vector.

2.4.1 System Model

The system model for TB with delay is shown in Figure 2.2, where $x(t)$ is the input data stream and the beamforming vectors associated with each transmit antenna taking delayed feedback into account are $w_1(t|T_d)$ to $w_{N_t}(t|T_d)$. The feedback delay is $T_d > 0$, and $T_d = nT_s$, where T_s is the symbol duration. The channels associated with each transmit antenna are $h_1(t)$ to $h_{N_t}(t)$. There are some assumptions regarding the channel, \mathbf{h} has i.i.d. entries, and follows the Rayleigh distribution, where $\mathbf{h} \sim \mathcal{CN}(\mathbf{0}, \sigma_h^2 \mathbf{I}_{N_t})$. Furthermore, the receiver does not have perfect knowledge of the channel. Each data symbol $x(t)$ is multiplied with the beamforming vector given as

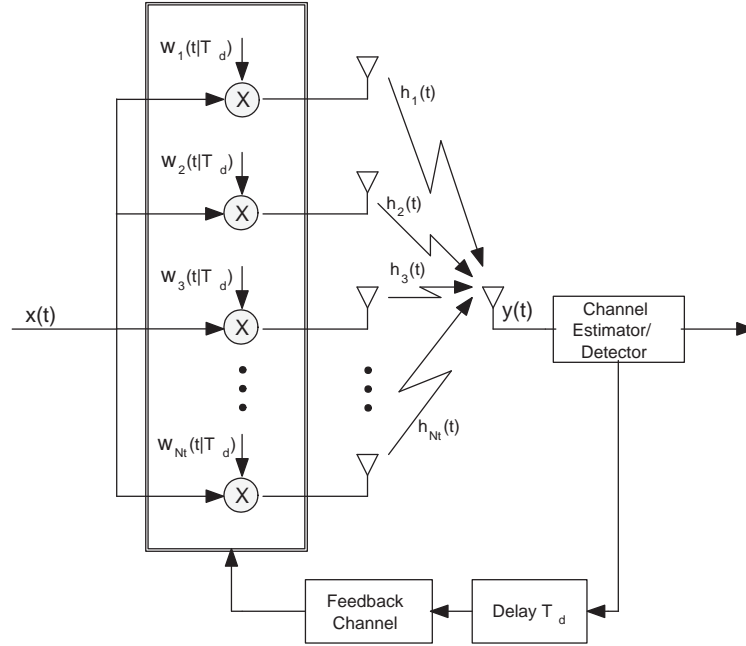


Figure 2.2 MISO system model

$$\mathbf{w}(t|T_d) = [w_1(t|T_d), \dots, w_{N_t}(t|T_d)]^T, \quad (2.17)$$

where $\mathbf{w}(t|T_d)$ has unit norm $\|\mathbf{w}(t|T_d)\| = 1$. Each antenna transmits simultaneously, and the received symbol is

$$y(t) = \mathbf{w}^H(t|T_d)\mathbf{h}(t)x(t) + \eta(t). \quad (2.18)$$

The delayed instantaneous SNR is defined as

$$\gamma(t|T_d) = |\mathbf{w}^H(t|T_d)\mathbf{h}(t)|^2\bar{\gamma}_s, \quad (2.19)$$

where $\bar{\gamma}_s = \frac{E_s}{N_0}$ is the average symbol SNR defined in (2.13). Instead of using the current channel to estimate the optimal beamforming vector, the outdated channel is used.

$$\mathbf{w}_{\text{opt}}(t|T_d) = \arg \max_{\{\mathbf{w}_i\}_{i=1}^N} |\mathbf{w}_i^H \mathbf{h}(t - T_d)|^2 \quad (2.20)$$

It can be seen from (2.20), that the BF vector that the transmitter uses is the outdated vector. This will affect the instantaneous SNR and reduce performance. Therefore, $\gamma(t|T_d) \leq \gamma(t)$ for $T_d > 0$. First, (2.19) can be decomposed into

$$\gamma(t|T_d) = \gamma_{\mathbf{h}}(t)(1 - z)\bar{\gamma}_s, \quad (2.21)$$

where $\gamma_{\mathbf{h}}(t) = \|\mathbf{h}(t)\|^2$ and z is the square of the minimum distance between the selected TB vector $\mathbf{w}_{\text{opt}}(t|T_d)$, and the normalized channel vector $\tilde{\mathbf{h}}(t) = \frac{\mathbf{h}(t)}{\|\mathbf{h}(t)\|}$. z is given by

$$\begin{aligned} z &= \min_i d^2(\mathbf{w}_i(t|T_d), \tilde{\mathbf{h}}(t)) = d^2(\mathbf{w}_{\text{opt}}(t|T_d), \tilde{\mathbf{h}}(t)) \\ &= 1 - |\mathbf{w}_{\text{opt}}^H(t|T_d)\tilde{\mathbf{h}}(t)|^2. \end{aligned} \quad (2.22)$$

In order to analyze the effects ICE will have on the system, we will consider the PSAM

scheme.

2.4.2 Channel Estimation using PSAM

Pilot symbol assisted modulation transmits a number of pilot symbols every P symbol durations. These pilot symbols are collected at the receiver and used to estimate the channel. We assume F pilot symbols are inserted to estimate $\mathbf{h}[i] = [h_1[i], \dots, h_{N_t}[i]]^T$, where $\mathbf{h}[i] = \mathbf{h}(iT_s)$. Since the elements of $\mathbf{h}[i]$ are i.i.d., each channel is estimated separately for all N_t channels. Moreover, indices $[i]$ and (t) denote discrete time and continuous time indexes, respectively. In this scheme, $h_{n_t}[i]$ is estimated separately for all $1 \leq n_t \leq N_t$. In order to estimate the channel coefficient $h_{n_t}[i]$, F pilot symbols are transmitted and can be expressed as an $F \times 1$ vector $\mathbf{s}_{n_t, \text{PS}} = [s[i - (F - 1)P - i_{n_t, \text{off}}], \dots, s[i - i_{n_t, \text{off}}]]^T$, where $i_{n_t, \text{off}} = (1, \dots, P - 1)$ is the offset of the closest pilot symbol to the desired symbol being estimated (see Figure 2.3).

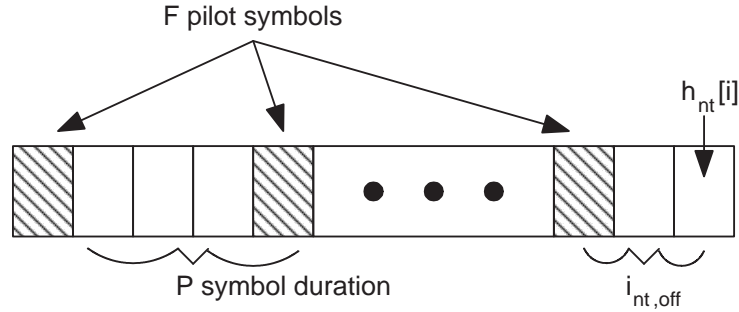


Figure 2.3 PSAM to estimate channel $h_{n_t}[i]$, using F pilot symbols

The larger $i_{n_t, \text{off}}$ is away from the desired symbol, the poorer the estimate will be. For estimating $\mathbf{h}[i]$, it is assumed that the transmit antennas are only active one at a time in the training mode to avoid interfering with each other. Therefore, $i_{n_t, \text{off}}$ are different for each antenna. The received signal at the pilot symbol positions are an

$F \times 1$ vector $\mathbf{y}_{n_t, \text{PS}}$, which is defined as

$$\mathbf{y}_{n_t, \text{PS}} = (\text{diag}(\mathbf{s}_{n_t, \text{PS}})) \mathbf{h}_{n_t, \text{PS}} + \boldsymbol{\eta}_{n_t, \text{PS}}, \quad (2.23)$$

where $\mathbf{h}_{n_t, \text{PS}} = [h_{n_t}[i - (F - 1)P - i_{n_t, \text{off}}], \dots, h_{n_t}[i - i_{n_t, \text{off}}]]^T$ and $\boldsymbol{\eta}_{n_t, \text{PS}} = [\eta_{n_t}[i - (F - 1)P - i_{n_t, \text{off}}], \dots, \eta_{n_t}[i - i_{n_t, \text{off}}]]^T$ are the complex channel gains and additive noise at the pilot symbol positions, respectively. The pilot symbols are transmitted with power P_{PS} . Therefore, (2.23) reduces to $\mathbf{y}_{n_t, \text{PS}} = \sqrt{P_{\text{PS}}} \mathbf{h}_{n_t, \text{PS}} + \boldsymbol{\eta}_{n_t, \text{PS}}$. The channel estimate for $h_{n_t}[i]$ is expressed as

$$\hat{h}_{n_t}[i] = \mathbf{g}_{n_t, \text{PS}}^H \mathbf{y}_{n_t, \text{PS}}, \quad (2.24)$$

where $\mathbf{g}_{n_t, \text{PS}}$ is a channel estimation filter. Using the estimated channel $\hat{h}_{n_t}[i]$ at time $t = iT_s$, the receiver calculates the optimal TB vector and feeds back that index to the transmitter. The transmitter then uses that vector at time $t = iT_s + T_d$. Due to the feedback delay. The optimal TB vector is calculated as follows,

$$\mathbf{w}_{\text{opt}}(t|T_d) = \arg \max_{\{\mathbf{w}_i\}_{i=1}^N} |\mathbf{w}_i^H \hat{\mathbf{h}}(t - T_d)|^2. \quad (2.25)$$

Based on this PSAM model, we consider the minimum mean squared error channel estimator (MMSE-CE), because it can best minimize the estimation MSE. The MMSE-CE filter is expressed as

$$\mathbf{g}_{n_t, \text{mmse}} = \mathbf{R}_{y_{\text{PS}}}^{-1} \mathbf{r}_{h, y_{\text{PS}}}, \quad (2.26)$$

where $\mathbf{r}_{h, y_{\text{PS}}} = E[h_{n_t}^* \mathbf{y}_{n_t, \text{PS}}] = \sqrt{P_{\text{PS}}} [R_h[(F - 1)P + i_{n_t, \text{off}}], \dots, R_h[i_{n_t, \text{off}}]]^T$, and $R_h[m] = E[h_{n_t}[i] h_{n_t}^*[i - m]]$ is defined as the channel temporal correlation coefficient. It is assumed that the channel conditions are slowly time varying, according to Clark's fading

ing spectrum, therefore, $R_h[m] = \sigma_h^2 J_0(2\pi B_f T_s m)$. $J_0(x)$ is the zeroth-order Bessel function, and B_f is the Doppler fading bandwidth [37]. Also, from (2.26) $\mathbf{R}_{y_{\text{PS}}} = E[\mathbf{y}_{n_t, \text{PS}} \mathbf{y}_{n_t, \text{PS}}^H]$ is a Toeplitz matrix defined as the auto correlation matrix of $\mathbf{y}_{n_t, \text{PS}}$. The first row of $\mathbf{R}_{y_{\text{PS}}}$ is given by $[P_{\text{PS}} R_h[0] + N_0, P_{\text{PS}} R_h^*[P], \dots, P_{\text{PS}} R_h^*[P(F-1)]]$. With the effects of ICE, and limited and delayed feedback to the system, quality will be severely degraded. To demonstrate this effect, the channel model with limited and delayed feedback errors will be analyzed next, followed by considering the effects of ICE at the receiver.

2.4.3 SER Lower Bound for Limited and Delayed Feedback

We propose to model the channel with delay alone as

$$\mathbf{h}(t) = \rho_d \mathbf{h}(t - T_d) + \mathbf{e}_d(t), \quad (2.27)$$

where $\rho_d = E[h_l(t)h_l^*(t - T_d)]$ is the correlation coefficient between the true channel and the outdated channel for $\{l = 1, \dots, N_t\}$. In addition, $\mathbf{e}_d(t)$ is the error vector with distribution $\mathbf{e}_d(t) \sim \mathcal{CN}(\mathbf{0}, \sigma_h^2(1 - |\rho_d|^2)\mathbf{I}_{N_t})$. Substituting (2.27) into (2.19), the new instantaneous SNR with delay and limited feedback can be written as

$$\begin{aligned} \gamma(t|T_d, z) &= |\mathbf{w}_{\text{opt}}^H(t|T_d)[\rho_d \mathbf{h}(t - T_d) + \mathbf{e}_d(t)]|^2 \bar{\gamma}_s \\ &= |\rho_d \mathbf{w}_{\text{opt}}^H(t|T_d) \mathbf{h}(t - T_d) + \mathbf{w}_{\text{opt}}^H(t|T_d) \mathbf{e}_d(t)|^2 \bar{\gamma}_s. \end{aligned} \quad (2.28)$$

Taking into account that $|\mathbf{w}_{\text{opt}}^H(t|T_d) \mathbf{h}(t - T_d)|^2 = (1 - z) \gamma_h(t - T_d)$, where $\gamma_h(t - T_d) = \|\mathbf{h}(t - T_d)\|^2$. Also, $\gamma_h(t - T_d)$ is a chi-square variable with $2N_t$ degrees of freedom [37]. Therefore, the moment generating function (MGF) of $\phi_{\gamma_h(t - T_d)}(s)$ is $\frac{1}{(1 - s\sigma_h^2)^{N_t}}$. It can

be seen from [51] that the MGF of (2.28) is

$$\begin{aligned}\Phi_{\gamma(t|T_d,z)}(s) &= \frac{(1 - \rho_d^2(1 - z)[s^{-1}\bar{\gamma}_{s,h}^{-1} - (1 - |\rho_d|^2)]^{-1})^{-N_t}}{1 - s\bar{\gamma}_{s,h}(1 - |\rho_d|^2)} \\ &= \frac{[1 - s\bar{\gamma}_{s,h}(1 - |\rho_d|^2)]^{N_t-1}}{[1 - s\bar{\gamma}_{s,h}(1 - |\rho_d|^2z)]^{N_t}} = \frac{(1 - \frac{s}{s_1})^{N_t-1}}{(1 - \frac{s}{s_2})^{N_t}},\end{aligned}\quad (2.29)$$

where $s_1 = \frac{1}{\bar{\gamma}_{s,h}(1-|\rho_d|^2)}$, $s_2 = \frac{1}{\bar{\gamma}_{s,h}(1-|\rho_d|^2z)}$, and $\bar{\gamma}_{s,h} = \bar{\gamma}_s\sigma_h^2$ adds in the effect of channel gain. By taking the expectation of (2.15) with respect to γ_h and z , where $\gamma = \gamma_h(1 - z)\bar{\gamma}_s$, the average SER of M-PSK modulation is given by

$$\overline{\text{SER}} = \int_{\gamma_h=0}^{\infty} \int_{z=0}^{z_0} \int_0^{\frac{(M-1)\pi}{M}} \frac{1}{\pi} e^{-\frac{g_{\text{PSK}}\gamma_h(1-z)\bar{\gamma}_s}{\sin^2\theta}} f_{\gamma_h}(\gamma_h)\tilde{f}_z(z)d\theta d\gamma_h dz, \quad (2.30)$$

where $f_{\gamma_h}(\gamma_h)$ and $f_z(z)$ are the probability density functions (PDFs) of γ_h and z , respectively. The cumulative distribution function (CDF) of z , which is defined as $F_z(z)$, needs to be found. This has proven to be a very difficult task, but a tight upper bound on the CDF of z has been derived in [17] for good TB codebooks. In [17] the tight upper bound of $F_z(z)$ was found to be

$$\tilde{F}_z(z) = Nz^{N_t-1}, \quad z \leq z_0, \quad (2.31)$$

where $z_0 = (\frac{1}{N})^{\frac{1}{N_t-1}}$. This upper bound holds for $0 \leq z \leq z_0$, and \sim represents the upper bound approximation. Next, by differentiating (2.31) an approximate PDF of z is given by $\tilde{f}_z(z) = N(N_t - 1)z^{N_t-2}$, for $z \leq z_0$. The MGF of γ_h is defined as

$$E[e^{-s\gamma_h}] = \int_{\gamma_h=0}^{\infty} f_{\gamma_h}(\gamma_h)e^{-s\gamma_h} d\gamma_h. \quad (2.32)$$

Therefore, substituting (2.29), where $s = \frac{-g_{\text{PSK}}}{\sin^2\theta}$ and $\tilde{f}_z(z)$ into (2.30), then inte-

grating over z will give the SER lower bound as

$$\begin{aligned} \overline{SER}_{LB} &= \frac{1}{\pi} \int_{\theta=0}^{\frac{(M-1)\pi}{M}} \frac{[1 + \frac{g_{\text{PSK}} \bar{\gamma}_{s,h}}{\sin^2 \theta} (1 - |\rho_d|^2)]^{N_t-1}}{1 + \frac{g_{\text{PSK}} \bar{\gamma}_{s,h}}{\sin^2 \theta}} \\ &\quad \times [1 + (1 - |\rho_d|^2) (\frac{1}{N})^{\frac{1}{N_t-1}} \frac{g_{\text{PSK}} \bar{\gamma}_{s,h}}{\sin^2 \theta}]^{1-N_t} d\theta, \end{aligned} \quad (2.33)$$

Furthermore, we assume the channel conditions are varying according to Clarke's fading spectrum, $\rho_d = J_0(2\pi B_f T_d)$, and $|\rho_d|$ does not decrease to zero but fluctuates around zero as $T_d \rightarrow \infty$. This can be seen in the numerical results with perfect CSI at the receiver (CSIR).

The numerical results in Figure 2.4 show the loss in performance for different SNR values, where $N_t = 3$, $B_f T_s = 0.05$, and $N = 16$ are assumed. It is shown that as T_d increases, the SER increases as well and then fluctuates around a constant value as $T_d \rightarrow \infty$. Figure 2.5 shows how delayed feedback can significantly reduce capacity over all SNR ranges. This simulation compares the analytical curve to the actual simulated curve when there are $N = 8$ TB vectors, and $B_f T_d = 0.2$ for the delay. Next, the results for ICE at the receiver will be investigated.

2.4.4 Capacity of Proposed TB Method with ICE, Limited and Delayed Feedback

By factoring ICE into the channel model without delay, the model becomes

$$\mathbf{h}(t) = \rho_e \left(\frac{\sigma_h}{\sigma_{\hat{\mathbf{h}}}} \right) \hat{\mathbf{h}}(t) + \mathbf{e}_h(t), \quad (2.34)$$

where $\rho_e = \frac{E[h_l(t)h_l^*(t)]}{\sigma_h \sigma_{\hat{\mathbf{h}}}}$ is the correlation coefficient between elements of $\mathbf{h}(t)$ and $\hat{\mathbf{h}}(t)$. Also, $\mathbf{e}_h(t)$ is the error vector with distribution $\mathbf{e}_h(t) \sim \mathcal{CN}(\mathbf{0}, \sigma_h^2(1 - |\rho_e|^2)\mathbf{I}_{N_t})$. By adding a delay to equation (2.34), and combining it with (2.27), the new channel

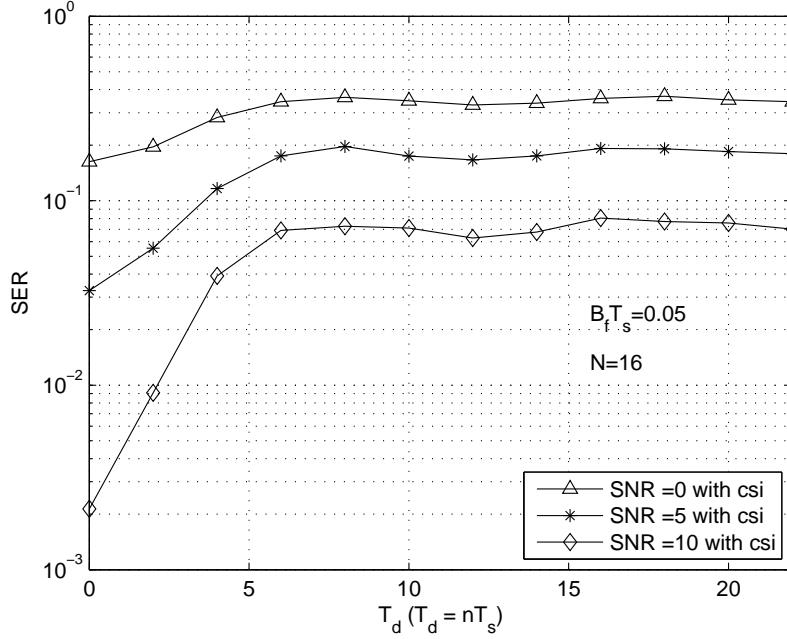


Figure 2.4 The actual SER for different values of SNR using QPSK modulation with $N_t = 3, N = 16$, and $B_f T_s = 0.05$

model with ICE, limited and delayed feedback can be expressed as

$$\mathbf{h}(t) = \rho_d \rho_e \left(\frac{\sigma_h}{\sigma_{\hat{h}}} \right) \hat{\mathbf{h}}(t - T_d) + \mathbf{e}(t), \quad (2.35)$$

where $\mathbf{e}(t) = \rho_d \mathbf{e}_h(t - T_d) + \mathbf{e}_d(t)$. The effects of ICE will not only hurt the quality of feedback information, but will also cause a loss in SNR. This loss factor is derived as [52, 53]

$$\beta = \frac{|\rho_{h_w}|^2}{(1 - |\rho_{h_w}|^2) N_t \bar{\gamma} + 1}, \quad (2.36)$$

where ρ_{h_w} is the normalized channel coefficient between the actual channel $h_w = \mathbf{w}_{\text{opt}}(t|T_d) \mathbf{h}(t)$ and the estimated channel $\hat{h}_w = \mathbf{w}_{\text{opt}}(t|T_d) \hat{\mathbf{h}}(t)$. Also, ρ_{h_w} depends on the PSAM scheme chosen along with system parameters. Combining equations (2.35) and (2.36), then substituting them into (2.19) will provide the received SNR including

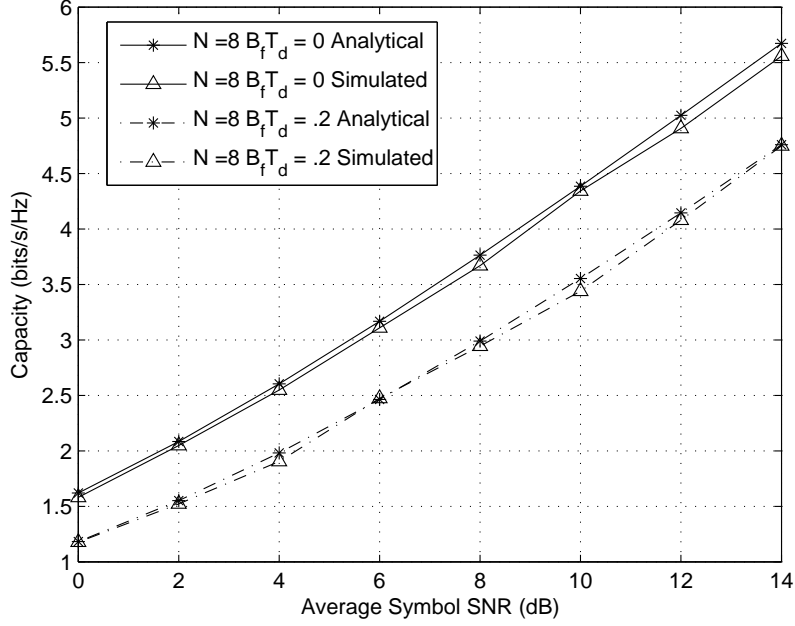


Figure 2.5 Analytical capacity curve vs. actual capacity curve with perfect CSI for $N = 8$, and $B_f T_d = .2$

ICE.

$$\gamma(t|T_d) = |\mathbf{w}_{\text{opt}}^H(t|T_d)[\rho_d \rho_e \left(\frac{\sigma_h}{\sigma_{\hat{h}}}\right) \hat{\mathbf{h}}(t - T_d) + \mathbf{e}(t)]|^2 \beta \bar{\gamma}_s \quad (2.37)$$

Also, (2.37) can be simplified to

$$\gamma(t|T_d) = |\rho_{\text{tot}} \mathbf{w}_{\text{opt}}^H(t|T_d) \hat{\mathbf{h}}(t - T_d) + \mathbf{e}_{\text{tot}}(t)|^2 \beta \bar{\gamma}_s, \quad (2.38)$$

where $\rho_{\text{tot}} = \rho_d \rho_e \left(\frac{\sigma_h}{\sigma_{\hat{h}}}\right)$, and $\mathbf{e}_{\text{tot}}(t) = \mathbf{w}_{\text{opt}}^H(t|T_d) \mathbf{e}(t)$. In order to derive the MGF of $\gamma(t|T_d)$, which is defined as $\phi_{\gamma(t|T_d, z)}(s) = E[e^{s\gamma(t|T_d, z)}]$, it needs to be expressed in a non-central Gaussian quadratic form conditioned on $\hat{\mathbf{h}}(t - T_d)$ [54]. This will give the conditional MGF $\phi_{\gamma(t|T_d, z)}(s|\mathbf{h})$. Therefore, the complex Gaussian quadratic form of $\gamma(t|T_d)$ conditioned on $\hat{\mathbf{h}}(t - T_d)$ equals $v^* \beta \bar{\gamma}_s v$, where $v = \rho_{\text{tot}} \mathbf{w}_{\text{opt}}^H(t|T_d) \hat{\mathbf{h}}(t - T_d) + \mathbf{e}_{\text{tot}}(t) \sim \mathcal{CN}(\rho_{\text{tot}} \mathbf{w}_{\text{opt}}^H(t|T_d) \hat{\mathbf{h}}(t - T_d), \sigma_h^2(1 - |\rho_{\text{tot}}|^2))$. Following the results for Gaussian

quadratic forms in [54], the conditional MGF of $\gamma(t|T_d)$ is obtained as

$$\phi_{\gamma(t|T_d,z)}(s|\mathbf{h}) = \frac{\exp\{|\rho_{\text{tot}}|^2|\mathbf{w}_{\text{opt}}^H(t|T_d)\widehat{\mathbf{h}}(t-T_d)|^2[(\beta\bar{\gamma}_s)^{-1}s^{-1} - \sigma_h^2(1-|\rho_{\text{tot}}|^2)]^{-1}\}}{1 - s\beta\bar{\gamma}_s\sigma_h^2(1-|\rho_{\text{tot}}|^2)} \quad (2.39)$$

Finally, $\phi_{\gamma(t|T_d,z)}(s|\mathbf{h})$ will need to be averaged over $\widehat{\mathbf{h}}(t-T_d)$ to obtain the average MGF $\phi_{\gamma(t|T_d,z)}(s)$.

$$\begin{aligned} \phi_{\gamma(t|T_d,z)}(s) &= \frac{[1 - s\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2)]^{N_t-1}}{[1 - s\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2z)]^{N_t}} \\ &= \frac{[1 - \frac{s}{s_1}]^{N_t-1}}{[1 - \frac{s}{s_2}]^{N_t}}, \end{aligned} \quad (2.40)$$

where $s_1 = \frac{1}{\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2)}$ and $s_2 = \frac{1}{\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2z)}$. See appendix for the complete proof. It can be seen from (2.40), that with no delay, and perfect CSIR, $\rho_{\text{tot}} = 1$ so $\rho_{h_w} = 1$, then $\beta = 1$, therefore, the MGF reduces to

$$\phi_{\gamma(t|T_d=0,z)}(s) = \frac{1}{[1 - s\bar{\gamma}_{s,h}(1-z)]^{N_t}}. \quad (2.41)$$

Next, with full rate feedback, imperfect receiver CSI, and the delay, the MGF becomes

$$\phi_{\gamma(t|T_d,z=0)}(s) = \frac{[1 - s\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2)]^{N_t-1}}{[1 - s\beta\bar{\gamma}_{s,h}]^{N_t}}. \quad (2.42)$$

Based on (2.40)-(2.42), one observes that the effects of delayed feedback and ICE at the receiver can significantly reduce the systems performance. Finally, by averaging out the quantization error, the MGF of $\gamma(t|T_d)$ can be obtained. In order to average out the effects of z , the approximate PDF of z needs to be used, then the average

approximate MGF of $\gamma(t|T_d)$ can be found as

$$\begin{aligned}
\tilde{\phi}_{\gamma(t|T_d)}(s) &= \int_0^{z_0} \phi_{\gamma(t|T_d,z)}(s) \tilde{f}_z(z) dz \\
&= \int_0^{z_0} \frac{N(N_t - 1) z^{N_t-2} [1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2)]^{N_t-1}}{[1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2 z)]^{N_t}} dz \\
&= N(N_t - 1) [1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2)]^{N_t-1} \int_0^{z_0} \frac{z^{N_t-2}}{[1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2 z)]^{N_t}} dz \\
&= N(N_t - 1) [1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2)]^{N_t-1} \int_0^{z_0} \frac{z^{N_t-2}}{[a + bz]^{N_t}} dz, \tag{2.43}
\end{aligned}$$

where $a = 1 - s\beta\bar{\gamma}_{s,h}$ and $b = s\beta\bar{\gamma}_{s,h}|\rho_{\text{tot}}|^2$. With the integral written in this manner, it can be solved by using the closed form expression

$$\int \frac{z^{N_t-2}}{(a + bz)^{N_t}} dz = \frac{z^{N_t-1}(a + bz)^{1-N_t}}{a(N_t - 1)}. \tag{2.44}$$

Based on this equality, the average MGF of $\gamma(t|T_d)$ becomes

$$\tilde{\phi}_{\gamma(t|T_d)}(s) = \frac{[1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2)]^{N_t-1}}{(1 - s\beta\bar{\gamma}_{s,h})[1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2 z_0)]^{N_t-1}}. \tag{2.45}$$

By using (2.45) the capacity of the system with limited and delayed feedback, along with ICE at the receiver, can now be analyzed. A good approximation is calculated by

$$\begin{aligned}
C &\approx \int_0^\infty \int_0^{z_0} \log(1 + x) f_{\gamma(t|T_d)}(x) \tilde{f}_z(z) dz dx \\
&= \int_0^\infty \log(1 + x) \tilde{f}_{\gamma(t|T_d)}(x) dx, \tag{2.46}
\end{aligned}$$

where $\tilde{f}_{\gamma(t|T_d)}(x)$ is the approximate PDF of $\gamma(t|T_d)$ by taking the inverse Laplace transform of (2.45). Based on these calculations it can be seen in Figure 2.6 how detrimental limited, delayed feedback, and ICE at the receiver can be to the system. This demonstrates the importance of taking these factors into account when designing

a TB system to be used in practice.

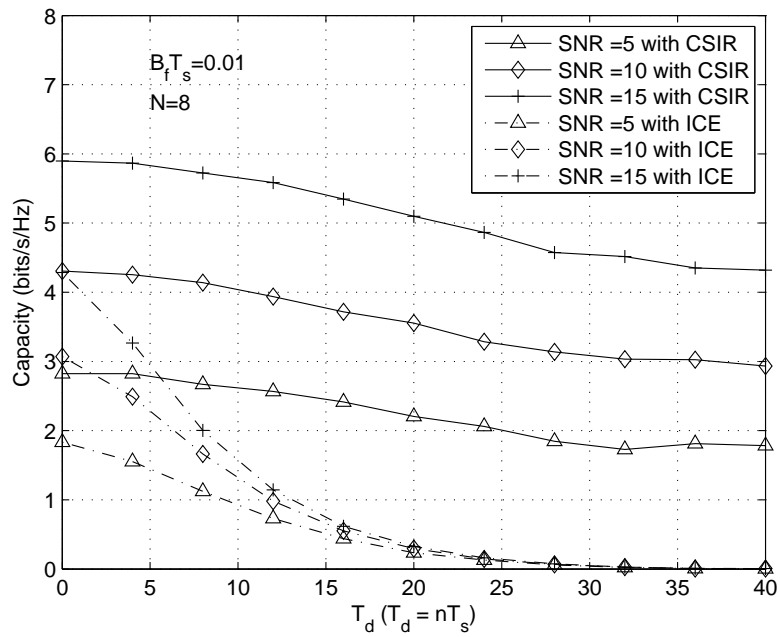


Figure 2.6 Capacity vs. delay T_d for simulated perfect CSIR and ICE curves, where $N = 8$, $N_t = 3$, and $B_f T_s = .01$

CHAPTER 3. Orthogonal Frequency Division Multiple Access

3.1 Introduction

In this chapter, the OFDMA cellular structure along with various multicarrier allocation strategies will be studied. Past research has focused on many different methods for OFDMA, using sum rate maximization techniques without fairness, or using short term fairness to improve the Quality of Service (QoS) to each mobile station. This was achieved by using rate adaptive techniques to maximize the overall data rate, while maintaining short term fairness by adding an extra constraint where each MS's rate R_k follows a predetermined rate ratio $R_1 : \dots : R_k = \alpha_1 : \dots : \alpha_k$. This thesis will address important issues that are missing, such as w-SNR ranking SMuD with long term RPF and adaptive rate tracking (ART). Long term RPF is less strict and performs better than short term RPF which is achieved through w-SNR ranking. The weight calculation can be implemented both online or offline. If channel statistics are known offline, a fixed weight vector can be calculated and used to allocate resources to each MS. When channel statistics are unknown, adaptive rate tracking can be used to calculate the weight vector online. Then resources are allocated based on each MS's weight factor.

The OFDMA cellular channel model is comprised of a BS, MSs, uplink channels, and downlink channels. These channels are used as a way for MSs and BSs to communicate with each other. For example, when assigning resources, the BS sends out

pilot symbols to the MSs on the downlink channels. The MSs then feed back their CSI to the BS on the uplink channels. Finally the BS communicates with the MSs on the downlink channels again with the assigned resources. For the uplink case, the power constraint for each MS needs to be considered when allocating resources. This is due to the various requirements for each MS. However, for the downlink channels there is only one power constraint. Therefore, in assigning resources the optimal method of joint power and subcarrier assignment is more complex for the uplink case.

3.2 Past Research Involving Multicarrier Based Resource Allocation Strategies

Multicarrier based resource allocation falls under two categories: static and dynamic assignment. Static assignment refers to fixed allocation strategies, where each user is assigned a certain subset of carriers pertaining to a fixed time slot or frequency band. With regards to dynamic assignment, any user can be assigned any subcarrier pertaining to any time slot or frequency band depending on their channel strength. Different systems use different allocation techniques depending on what the system is trying to accomplish. Static resource allocation provides the least complicated receiver designs because no feedback CSI is needed. However, this causes an abundance of waste when channel conditions become poor. Dynamic assignment on the other hand causes less waste, but could possibly increase complexity at the receiver side and for the scheduler. There are a couple of different strategies for static channel assignment.

3.2.1 Static Resource Assignment

There are many different kinds of static methods to assign carriers. These methods range from the simplest round robin (RR) technique, to the more involved methods

such as, allocating a specific frequency band or time slot to a specific user [24,55]. For OFDMA, RR allocates each time slot, one at a time, to each MS. RR does not take any type of CSI into account. It evenly divides up the carriers, but does not come close to being optimal [55].

An alternate static assignment method would be to allow each user to transmit during a specific time slot that is unique to each MS. This provides each MS an equal share of time to transmit data, but does not take into account any CSI. The MSs are allowed to use any carriers during their allocated time slot.

Another approach designates each MS carriers for a particular bandwidth. Therefore, the MSs can transmit during all time slots. However, due to the fading characteristics of the channel, the capacity over the short term for static allocation methods would vary widely as a result of a user's channel being in a deep fade.

Since the users are dispersed throughout the cell, each MS's channel is different and independent, resulting in different fading and path loss effects. Path loss can be expressed as a ratio between transmitted and received power [56]. The smaller the path loss, the better. There are many factors contributing to path loss, these include both BS and MS antenna heights, each MS's distance from the BS, the subcarrier's frequency, and the terrain surrounding each MS. Therefore, multicarrier resource allocation will be significantly affected by all of these factors.

When allocating resources both sum rate maximization and fairness among users need to be considered. Static resource allocation techniques perform poorly in these areas because they do not take CSI into account. The resources are allocated equally, but due to the effects of fading channels and path loss the data rate suffers greatly. Dynamic resource allocation deems the more interesting case.

3.2.2 Dynamic Carrier, Power and Rate Assignment

Dynamic resource assignment takes CSI into account in order to optimally allocate resources to each user with minimal waste. Resources can be allocated a few different ways. Carriers can be assigned using exclusive carrier assignment (ECA) or shared carrier assignment (SCA). Resources can also be allocated based on each MS's SNR alone or rate maximization techniques. Finally, fairness metrics can also be implemented to ensure each MS gets an equal share of the resources.

ECA only allows one MS to utilize a given carrier at any one time. This ensures there is no interference between MSs since all carriers are orthogonal with each other. In order to maximize the data rate, it was proven in [27] that ECA is optimal for centralized schemes described in this thesis.

SCA allows more than one MS to be assigned a given carrier. This causes problems since interference becomes an issue. As one MS increases transmit power, the signal-to-interference-plus-noise ratio (SINR) of the other MSs goes down. This added interference also decreases the overall data rate when compared to ECA. SCA is more suitable for ad hoc networks where interference between MSs could be significantly less [57]. The basic scheme allocating resources using ECA is described next.

Allocating carriers based on each MS's SNR, is referred to as absolute SNR (a-SNR) ranking based SMuD scheme [31]. This method maximizes capacity without being fair to each MS. When allocating resources dynamically, it is essential to know each MS's CSI. Utilizing this information, the base station computes each MS's SNR, and assigns the carrier to the MS with the highest SNR value. Once all carriers have been assigned, power can be allocated using either EPA or WF.

For EPA, the transmit power is divided equally among each carrier. Since the channels are assumed to be Rayleigh fading they will experience different channel gains. Therefore, this is not optimal since assigning the weaker channels the same amount of power as the stronger channels will result in a lot of power being wasted.

Instead, using the WF method to allocate power is a better approach.

WF utilizes the Lagrangian function to maximize the sum rate under the total power constraint. Since the sum rate is a concave function, taking the derivative of the Lagrangian function with respect to power, and setting the result to zero gives a series of equations called KKT conditions. Solving these equations with regards to the maximum power constraint yields an optimal SNR threshold, termed as the waterfilling level. Based on this threshold, power can then be allocated to each carrier. This method has proven to be optimal when allocating power [28].

Channel dependant scheduling techniques use CSI to calculate each MS's data rate and then allocate resources depending on which MS has the largest rate. This technique is shown in [29], where power and carriers are allocated jointly. Since the data rate is dependant on the product of channel SNR and transmit power. These constraints need to be taken into account together which greatly increases the complexity of the system. Dynamic allocation techniques also need to be fair.

Fairness metrics ensure each MS gets an equal share of the resources allocated. This can be accomplished in the short term, or long term. Short term fairness ensures fairness among MSs for each individual time slot. Long term fairness allows each MS access to an equal number of carriers over a period of time [58]. There are different ways of implementing short term or long term fairness.

Proportional fair scheduling (PFS) transmits to the user with the largest normalized data rate or received SNR [32]. In [58] PFS is implemented for both short and long term fairness cases. It was proven that long term fairness outperformed the more strict short term fairness based on n-SNR ranking. PFS schemes are able to ensure fairness, but they are not able to adjust for different quality of service requirements.

Since a lot of different multimedia services are being transmitted over wireless channels, some MSs require higher data rates than others. RPF allocates resources to ensure each MS's data rate follows a predetermined rate ratio vector [30]. Therefore,

resources are allocated based on each MS's weight factor, where more resources are allocated to higher weights.

3.2.3 Past Research Involving Rate Proportional Fairness Techniques

RPF techniques are needed to ensure fairness among MSs. In [29] and [30] sum rate maximization techniques were used along with RPF to ensure short term fairness. The algorithm in [29] is much like the a-SNR ranking case, except a constraint is added where each MS's rate R_k follows a predetermined rate ratio $R_1 : \dots : R_K = \alpha_1 : \dots : \alpha_K$. In the first step, each MS's power and carriers are set to zero, where N is the total number of carriers, and K is the total number of MSs. Next, each MS finds a carrier that maximizes their SNR, where $\gamma_k = \max_n \gamma_{k,n}$. Each user is then assigned that specific carrier, and power is allocated to that user. Power is divided up using EPA, and based on these initial values, each MS's rate is calculated by

$$R_k = \frac{B}{N} \log(1 + P_k \gamma_k), \quad (3.1)$$

where B is the total bandwidth. After each user is assigned one carrier, the rest of the carriers will be assigned using the RPF technique [29]. Out of the rates calculated in (3.1), the i^{th} MS with the smallest ratio is selected to be assigned the next carrier.

$$\frac{R_i}{\alpha_i} \leq \frac{R_k}{\alpha_k} \quad (3.2)$$

From the remaining $N - K$ carriers, the carrier n that maximizes that MS's SNR $\gamma_{i,n}$ is assigned to MS i . Their power is then increased by $P_i = P_i + \frac{P_i}{N}$, and the sum rate for MS i is calculated. However, before the sum rate can be calculated, power has to be allocated to each carrier using the WF technique.

The algorithm for WF uses the Lagrangian function to maximize the sum rate subject to (s.t.) the total power constraint. The optimization model for downlink rate

maximization is defined as

$$\max_{\{P_n\}} \sum_{n \in S_i} \log(1 + P_n(t)\gamma_{i,n}(t)), \quad s.t. \quad \sum_{n \in S_i} P_n(t) \leq P_i, \quad (3.3)$$

where $\gamma_{i,n}(t)$ is the channel SNR of the selected user at carrier n , and S_i is a set of all carriers assigned to the i^{th} mobile station. The Lagrangian function is then used to maximize (3.3), which is expressed as

$$\mathcal{L}(\lambda(t), \{P_n(t)\}) = \sum_{n \in S_i} \log(1 + P_n(t)\gamma_{i,n}(t)) - \lambda(t) \left(\sum_{n \in S_i} P_n(t) - P_i \right), \quad (3.4)$$

where $\lambda(t)$ is the Lagrangian multiplier. The index t will be dropped for simplicity, for example $P_n(t) = P_n$, unless otherwise stated. By taking the derivative of (3.4) with respect to (w.r.t.) $\{P_n\}$, and setting the resulting equations equal to zero, we get the maximum value for P_n because the capacity is a concave function.

$$\frac{d\mathcal{L}}{dP_n} = \frac{\gamma_{i,n}}{1 + P_n\gamma_{i,n}} - \lambda = 0 \quad (3.5)$$

Rearranging (3.5), and solving for P_n gives

$$P_n^* = \left(\frac{1}{\lambda} - \frac{1}{\gamma_{i,n}} \right)^+ \quad s.t. \quad \sum_{n \in S_i} P_n^* \leq P_i, \quad (3.6)$$

where $(x)^+$ is the maximum value between 0 and x . Solving (3.6) for λ gives the solution for optimal SNR threshold level giving by

$$\lambda = \frac{N_{\text{eff}}}{P_i + \sum_{n \in S_i} \frac{1}{\gamma_{i,n}}}, \quad (3.7)$$

where, $N_{\text{eff}} \leq N$. The power for MS i is then allocated by using (3.6). The sum rate

is calculated by

$$R_i = \sum_{n \in S_i} \frac{B}{N} \log(1 + P_n^* \gamma_{i,n}). \quad (3.8)$$

The process then starts over and compares each MS's rate ratio using equation (3.2) to assign the next carrier. This type of joint subcarrier and power allocation technique is a suboptimal approach to maximizing the sum rate, while achieving short term fairness. Other research has been done to maximize the sum rate while achieving long term fairness. In [59], they use the normalized SNR (n-SNR) ranking to help improve performance for the TDMA model, while [31] and [58] used n-SNR ranking for the OFDMA model. It was shown in [31], that the n-SNR ranking scheme with long term fairness outperformed the more strict short term fairness scheme. Normalized SNR ranking achieves long term fairness by averaging each MS's SNR over multiple time slots. By finding the average SNR $\bar{\gamma}_{k,n}$, for each MS $k = 1, \dots, K$, and each carrier $n = 1, \dots, N$, each MS's SNR can be normalized, $\tilde{\gamma}_{k,n} = \frac{\gamma_{k,n}}{\bar{\gamma}_{k,n}}$. Based on this normalized SNR, the MS k^* with the highest n-SNR value is selected for each carrier.

$$\tilde{\gamma}_{k^*,n} = \max_n \{\tilde{\gamma}_{1,n}, \dots, \tilde{\gamma}_{K,n}\} \quad (3.9)$$

Once each carrier has been assigned to each user, the power is then allocated by either EPA or WF. If EPA is used, then the sum rate becomes

$$R = \sum_{n=1}^N \frac{B}{N} \log\left(1 + \gamma_{k^*,n} \frac{P_t}{N}\right), \quad (3.10)$$

where $\gamma_{k^*,n}$ is the instantaneous SNR of user k^* at carrier n . If the WF method is used to allocate power, then each carrier will be allocated a certain amount of power P_n^* based on KKT conditions for WF. When each carrier is allocated power, the sum

rate will be

$$R = \sum_{n=1}^N \frac{B}{N} \log(1 + \gamma_{k^*,n} P_n^*). \quad (3.11)$$

This method ensures a long term fairness by normalizing each MS's SNR before allocating carriers. That way the effects caused by noise and path loss can be canceled out, and MS's with weaker channels will get the same amount of resources allocated to them as the MS's with stronger channels. However, there is no way of tracking the different QoS requirements for different traffic types such as MPEG video or HTTP. Instead, we propose to use a weighted SNR (w-SNR) ranking SMuD method with long term RPF and adaptive rate tracking to account for this.

3.3 Long Term RPF with w-SNR Ranking and Adaptive Rate Tracking

In the proposed method, each MS can be assigned a different weight factor to fit for the different traffic types and QoS requirements. Depending on what those requirements are, MS's with a larger weight will be allocated more resources than MS's with a smaller weight. By using long term fairness, each MS is guaranteed a fair share of the available resources. In addition, by using adaptive rate tracking, when a MS's channel becomes better than average more resources can be allocated to that user by updating their weight factor online, or vice versa. This type of adaptive rate tracking can significantly increase the sum rate for the system. There are three methods that can be implemented to find the optimal weight vector (\mathbf{w}_{opt}). The first method calculates the SNR weight vector for all MS's offline when channel statistics are known. The second method uses adaptive rate tracking without future CSI online to calculate each MS's data rate, and then dynamically adjusts each MS's weight factor until \mathbf{w}_{opt} is found. Lastly, the third method uses adaptive rate tracking with

future CSI online to calculate \mathbf{w}_{opt} . Finally, when \mathbf{w}_{opt} is obtained by any of the three methods, the scheduler allocates resources online according to each MS's weight to maintain the target RPF. The system model for the OFDMA downlink case will be explained next.

3.3.1 System Model

Assume the downlink OFDMA has K MSs and N total available carriers. Note, all variables defined here are independent of any variables defined earlier in the transmit beamforming section. Also, the time index t will be dropped for simplicity. The channels are independent between MS's, and follow a Rayleigh distribution. The instantaneous SNR of user k , at subcarrier n , is defined as

$$\gamma_{k,n}^h = \frac{|h_{k,n}|^2}{N_{k,n}}, \quad (3.12)$$

where $h_{k,n}$ is the complex channel gain, and $N_{k,n}$ is the band-limited noise power. The BS has a maximum power expressed as P_t , which is divided among all the N carriers. Therefore, P_n is the power allocated to the n^{th} carrier, and

$$\sum_{n=1}^N P_n \leq P_t \quad (3.13)$$

is the total power constraint. Due to WF some carriers may be wasted. Also, S_k is the set of carriers allocated to user k , subject to

$$\bigcup_{k=1}^K S_k \subset \{1, \dots, N\}.$$

Based on these variables, the sum rate for the system is expressed as

$$\sum_{k=1}^K \sum_{n=1}^N a_{k,n} R_{k,n}, \quad (3.14)$$

where $a_{k,n} = \{0, 1\}$ denotes if user k is assigned carrier n , and $\sum_{k=1}^K a_{k,n} \leq 1$ is based on the fact that each carrier n can be assigned to at most one user. Moreover, $R_{k,n}$ is the k^{th} MS's data rate at carrier n , defined as

$$R_{k,n} = \frac{B}{N} \log(1 + P_{k,n} \xi_k \gamma_{k,n}^h), \quad (3.15)$$

where ξ_k is the SNR gap function, which equals one for ergodic capacity, and $\xi_k = \frac{-1.5}{\log(5P_{e,k})}$ for the continuous rate QAM constellation [60]. $P_{e,k}$ is defined as the target bit error rate (BER) for user k . In addition, $\sum_{k=1}^K \sum_{n=1}^N a_{k,n} P_{k,n} = P_t$ is the total power constraint based on ECA. Using the SNR channel assignment method, it can be seen from (3.15), that in order to maximize the sum rate, each MS's SNR should be maximized at each carrier. Therefore, by combining the SNR gap function with each MS's instantaneous SNR, the new SNR is defined as $\gamma_{k,n} = \xi_k \gamma_{k,n}^h$. The BS calculates this quantity based on the CSI from each user. By adding in RPF and using ECA, the sum rate maximization technique subject to power and long term fairness constraints is

$$\begin{aligned} \max_{\{a_{k,n}\}\{P_{k,n}\}} \quad & \sum_{k=1}^K \sum_{n=1}^N a_{k,n} R_{k,n} \\ \text{s.t.} \quad & \sum_{k=1}^K \sum_{n=1}^N a_{k,n} P_{k,n} \leq P_t \\ \{\bar{R}_1 : \dots : \bar{R}_K\} \quad & = \quad \{\alpha_1 : \dots : \alpha_K\}. \end{aligned}$$

ECA means $\sum_{k=1}^K a_{k,n} \leq 1$, and the average rate of the k^{th} MS is $\bar{R}_k = E_t[R_k]$, where $E_t[\cdot]$ means taking the expectation with respect to t . The sum rate for MS k is given by

$$R_k = \sum_{n \in S_k} R_{k,n}. \quad (3.16)$$

Once all the carriers have been assigned, power can be allocated by either EPA, or

WF methods.

3.3.2 Resource Allocation and Different Methods Involving Optimal Weight Vector Calculation

The proposed method is divided up into three parts. The first part finds the optimal weight vector offline using known channel statistics. The second part utilizes ART without future CSI to calculate the optimal weight vector online. The Third method uses ART with future CSI to calculate the optimal weight vector online as well. Once \mathbf{w}_{opt} has been obtained by any of the three methods, resources can be allocated accordingly.

Online Allocation of Resources Using w-SNR Ranking Method

For weighted SNR ranking, the weight factor w_k is multiplied by the normalized instantaneous SNR. Each MS's weight factor is calculated based on the target RPF $\{\bar{R}_1 : \dots : \bar{R}_K\} = \{\alpha_1 : \dots : \alpha_K\}$. Therefore, the adjusted normalized SNR is defined as

$$z_{k,n} = \frac{w_k \gamma_{k,n}}{\bar{\gamma}_k}, \quad (3.17)$$

where the average channel gain $\bar{\gamma}_k = E[\gamma_{k,n}]$, and the weight factor is subject to $\sum_{k=1}^K w_k = K$. Allocation of resources depends on the normalized adjusted SNR value found in (3.17). Since $z_{k,n} = \frac{w_k \gamma_{k,n}}{\bar{\gamma}_k}$, then $\gamma_{k,n} = \frac{z_{k,n} \bar{\gamma}_k}{w_k}$. The w-SNR ranking selection at carrier n is defined as

$$k^* = \arg \max_k \{z_{1,n}, \dots, z_{K,n}\}. \quad (3.18)$$

When all carriers have been assigned. Power is allocated by either EPA or WF. Once all resources have been allocated to each MS, the average weighted rate vector

$\bar{\mathbf{R}}(\mathbf{w})$ can be obtained. The average rate for MS k^* at carrier n can be calculated based on EPA as follows,

$$\bar{R}_{k^*,n}(\mathbf{w}) = E \left[\frac{B}{N} \log \left(1 + \gamma_{k^*,n} \frac{P_t}{N} \right) \right]. \quad (3.19)$$

The average sum rate for MS k is simply $\bar{R}_k(\mathbf{w}) = \sum_{n \in S_k} \bar{R}_{k^*,n}(\mathbf{w})$. For the WF method, λ can be obtained from (3.6). Therefore, the average rate based on WF is expressed as

$$\bar{R}_{k^*,n}(\mathbf{w}) = E \left[\frac{B}{N} \log (1 + \gamma_{k^*,n} P_n^*) \right], \quad (3.20)$$

and the average sum rate is calculated the same as the EPA case. Once the average individual rate is obtained, the optimal weight vector can be calculated.

Offline Weight Vector Calculation

The weight vector is needed to allocate resources to each MS. The steps taken to find the optimal weight vector follow an iterative method based on each MS's average rate. The weight vector and average weighted rate vector are defined as $\mathbf{w} = [w_1, \dots, w_K]^T$ and $\bar{\mathbf{R}}(\mathbf{w}) = [\bar{R}_1(\mathbf{w}), \dots, \bar{R}_K(\mathbf{w})]^T$, respectively. Also, the average sum rate is

$$\bar{R}_{\text{tot}}(\mathbf{w}) = \sum_{k=1}^K \bar{R}_k(\mathbf{w}). \quad (3.21)$$

To achieve a target RPF, the prespecified rate ratio vector $\boldsymbol{\alpha} = [\alpha_1, \dots, \alpha_K]^T$ is set where

$$\sum_{k=1}^K \alpha_k = 1. \quad (3.22)$$

Therefore, the target RPF is $\bar{\mathbf{R}}_{\text{RPF}}(\mathbf{w}) = \bar{R}_{\text{tot}}(\mathbf{w})\boldsymbol{\alpha}$. Based on these values for each MS, the iterative approach defines a rate ratio vector as

$$\mathbf{r} = [r_1, \dots, r_K]^T = \left[\frac{\bar{R}_1}{\alpha_1}, \dots, \frac{\bar{R}_K}{\alpha_K} \right]^T. \quad (3.23)$$

This vector is then normalized by $\tilde{\mathbf{r}} = \frac{K\mathbf{r}}{\sum_{k=1}^K r_k}$, where $\sum_{k=1}^K \tilde{r}_k = K$. The target RPF is attained when $\tilde{\mathbf{r}} = \mathbf{1}_{K \times 1}$. In order to accomplish this, the optimal weight vector \mathbf{w}_{opt} needs to be found using the following steps, where $\{s = 1, 2, \dots\}$ is the index for each step. Therefore, from $\tilde{\mathbf{r}}(s) = [\tilde{r}_1(s), \dots, \tilde{r}_K(s)]^T$, both the maximum and minimum normalized rate ratio need to be obtained.

Furthermore, the error in the normalized rate ratio vector is defined as $e(s) = \tilde{r}_{\text{max}}(s) - \tilde{r}_{\text{min}}(s)$. When the magnitude of error $|e(s)|$ is smaller than some arbitrarily small value ($\epsilon_e > 0$), then the target RPF is achieved. For the first step, $s = 1$, set $\mathbf{w}(1) = \mathbf{1}_{K \times 1}$, then find the average weighted rate vector $\bar{\mathbf{R}}(\mathbf{w})$. From that we calculate the normalized rate ratio vector $\tilde{\mathbf{r}}(1)$, and find the error $e(1)$.

$$e(1) = \tilde{r}_{\text{max}}(1) - \tilde{r}_{\text{min}}(1) \quad (3.24)$$

Compare the magnitude of the error to the threshold as follows,

$$|e(s)| < \epsilon_e. \quad (3.25)$$

If (3.25) is true then stop and \mathbf{w}_{opt} is found, otherwise find the MS whose current RPF is the smallest and largest out of all the MS's.

$$\begin{aligned} k_{\text{min}} &= \arg \min_k \tilde{r}_k \\ k_{\text{max}} &= \arg \max_k \tilde{r}_k \end{aligned} \quad (3.26)$$

Next, these weight vectors can be updated by

$$w_k(s+1) = w_k(s) - \beta(s)e(s),$$

where $\beta(s)$ is a scalar value that decreases as s increases. The remaining elements of $\mathbf{w}(s+1)$ are the same as $\mathbf{w}(s)$, where $\sum_{k=1}^K w_k(s) = K$ for all s . Based on the updated weight vector $\mathbf{w}(s+1)$, recalculate $\bar{\mathbf{R}}(w)$ and $\tilde{\mathbf{r}}(s+1)$, increase s by one and find the error again. If (3.25) holds true, then the optimal weight vector has been obtained, otherwise go back to (3.26) and increase s by one. The optimal weight vector is then used in the proposed method for w-SNR ranking, which achieves the desired long term RPF. The algorithm for finding \mathbf{w}_{opt} is provided next.

1. Set $s = 1$ and $\mathbf{w} = \mathbf{1}_{K \times 1}$.
2. Calculate $\bar{\mathbf{R}}(w)$ and then the rate ratio vector, $\mathbf{r} = \left[\frac{\bar{R}_1}{\alpha_1}, \dots, \frac{\bar{R}_K}{\alpha_K} \right]^T$.
3. Normalize the rate ratio vector $\tilde{\mathbf{r}} = \frac{K\mathbf{r}}{\sum_{k=1}^K r_k}$.
4. For $\tilde{\mathbf{r}}(s) = [\tilde{r}_1(s), \dots, \tilde{r}_K(s)]^T$, find $\tilde{r}_{\min}(s)$ and $\tilde{r}_{\max}(s)$.
5. Calculate error factor $e(s)$, where $e(s) = \tilde{r}_{\max}(s) - \tilde{r}_{\min}(s)$.
6. Compare the error factor with threshold ϵ_e , where $|e(s)| < \epsilon_e$. If inequality holds true then stop and output \mathbf{w}_{opt} , otherwise continue on to step 7.
7. Find $k_{\min} = \arg \min_k \tilde{r}_k$, and $k_{\max} = \arg \max_k \tilde{r}_k$.
8. Update these weight vectors where $w_k(s+1) = w_k(s) - \beta(s)e(s)$, while leaving the remaining elements of $\mathbf{w}(s)$ alone, as long as $\sum_{k=1}^K w_k(s) = K$ for all s .
9. Based on $\mathbf{w}(s+1)$ calculate $\bar{\mathbf{R}}(w)$ and $\tilde{\mathbf{r}}(s+1)$.
10. Increment s by one, and go back to step 4.

Adaptive Rate Tracking w-SNR Method with and without Future CSI

ART involves either using future channel realizations, or not using future CSI to make sure each MS's rate is following the optimal rate ratio for each user. This assumption allows the effects of ART to be analyzed along with the benefits of future CSI. Each MS's rate can be tracked without future CSI as follows,

$$\overline{R}_k(t) = \beta_k \overline{R}_k(t - T_s) + (1 - \beta_k) R_k(t). \quad (3.27)$$

If future CSI is taken into account then each MS's rate is tracked by

$$\overline{R}_k(t) = \beta_k \overline{R}_k(t - T_s) + \frac{(1 - \beta_k)}{N} [R_k(t), \dots, R_k(t + (N - 1)T_s)], \quad (3.28)$$

where β_k is called the forgetting factor, and N is the number of future channel realizations. These forgetting factors can be adjusted to how much future estimates effect the average rate for MS k . The larger the forgetting factor means the larger the sliding window size becomes, where $\beta_k = 1 - \frac{1}{T_c}$ and T_c is the window size. Once $\overline{\mathbf{R}}_k(t)$ is known for each MS, a MMSE approach is used to calculate the error given by

$$e_k(t) = \frac{\overline{R}_k(t) - \overline{R}_{k,\text{tar}}(t)}{\overline{R}_{k,\text{tar}}(t)} = \frac{\overline{R}_k(t)}{\overline{R}_{k,\text{tar}}(t)} - 1, \quad (3.29)$$

where $\overline{R}_{k,\text{tar}}(t) = \overline{R}_{\text{tot}}(t)\alpha_k$. Next, the weight factor can be updated using

$$w_k(t + T_s) = w_k(t) - \beta e_k(t), \quad (3.30)$$

where β is a scaler value.

This online approach is very beneficial when channel statistics cannot be obtained offline. ART can be shown in Figures 3.1 and 3.2. In Figure 3.1 each MS's rate is tracked and compared to a statistical optimal rate with future CSI included, where

the number of channel realizations $N = 10$ and $\beta_k = .997$. Figure 3.1 can also be compared to Figure 3.2, where ART does not use future CSI and $\beta_k = .997$. It can be seen that by utilizing future CSI, the time needed to converge to the optimal rate is dramatically reduced. Figure 3.3 shows different w-SNR schemes with and without ART, where $N = 16$, $K = 4$, $\alpha = [1 : 2 : 4 : 8]$, and $L = 4$ paths with a uniform power delay profile (PDP).

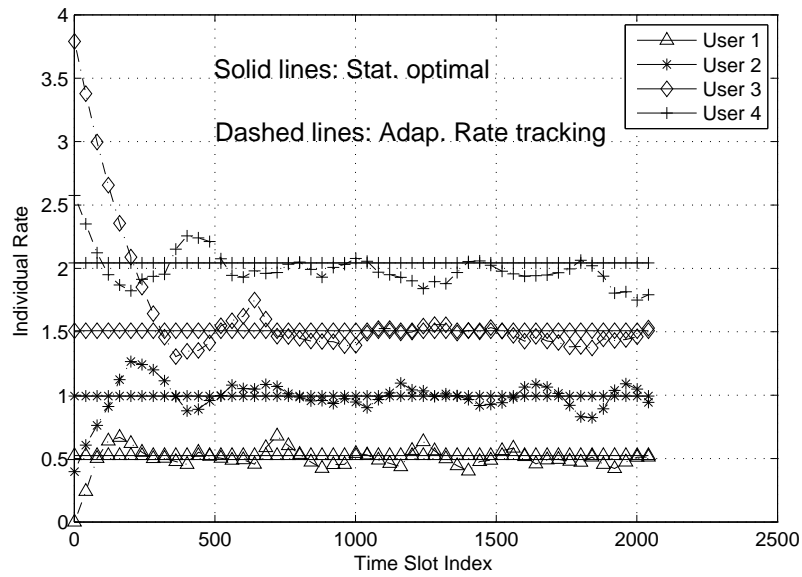


Figure 3.1 OFDMA downlink using adaptive rate tracking with future channel realizations, where $N = 10$, and $\beta_2 = .997$

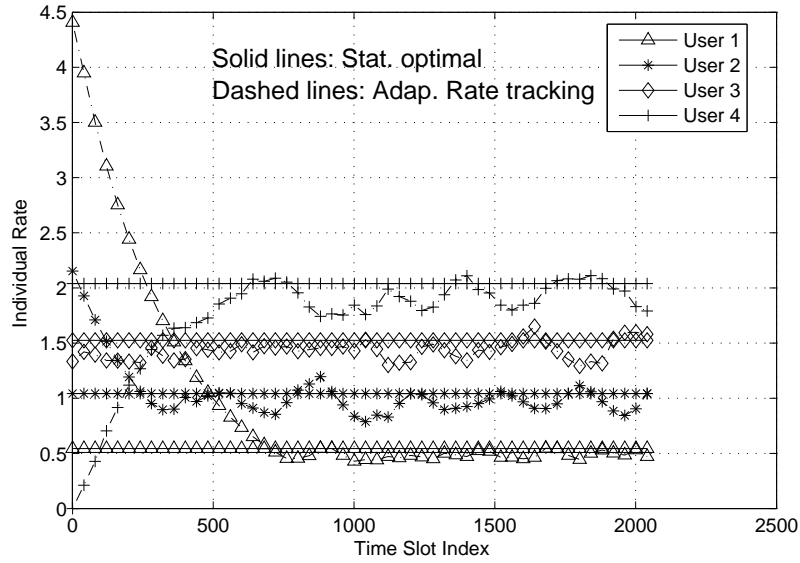


Figure 3.2 OFDMA downlink with adaptive rate tracking without future channel realizations, where $\beta_1 = .997$

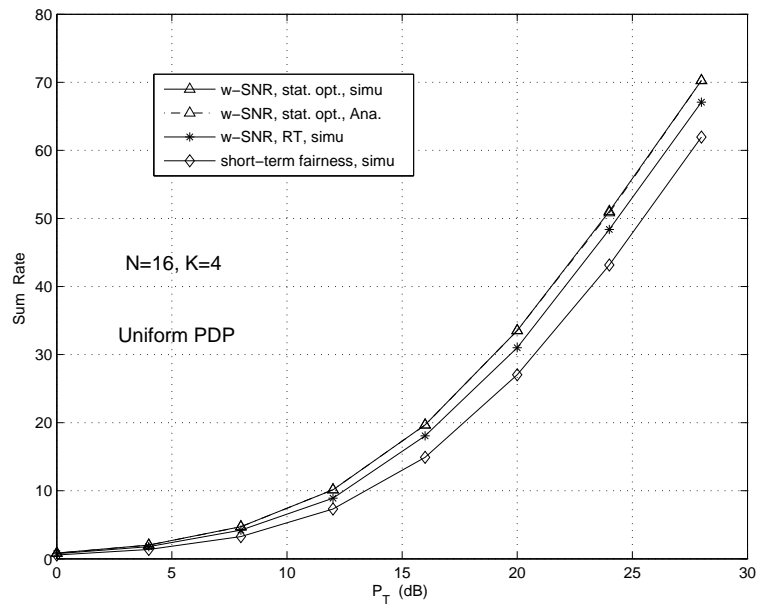


Figure 3.3 Sum rate vs. P_T for downlink OFDMA with rate tracking. (dynamically adjusted \mathbf{w}) $N = 16, K = 4$, and equal target BERs ($1e-3$ for all users). User rate ratio follows $[1 : 2 : 4 : 8]$. $L = 4$ paths with a uniform power delay profile (PDP)

CHAPTER 4. Conclusion

4.1 Summary

This thesis showed what the effects of limited delayed feedback, along with ICE at the receiver, has on transmit beamforming. This model demonstrated that both finite rate and delayed feedback, can significantly reduce performance as the delay increases. This was shown for both SER and capacity curves. With just a moderate delay, the SER increased substantially for medium to high SNR ranges, where capacity decreased over all SNR ranges. Capacity is very sensitive to the effects of ICE at the receiver. If the delay in feedback increases, with ICE at the receiver, capacity can be reduced to practically zero. Therefore, these effects can not be ignored for future systems.

OFDMA systems do have issues that need to be addressed as well. OFDMA has proven to be a very good candidate for 4G systems, but it can also be unfair to potential users. Therefore, the conventional method a-SNR SMuD proved to be an upper capacity bound for systems trying to improve fairness. Short term rate proportional fairness was too strict, and a more long term RPF method was found to be adequate. Based on these facts, w-SNR ranking with SMuD and long term RPF proved that it could maximize performance and provide long term RPF for every user. Furthermore, by adding in adaptive rate tracking, each MS's rate can be tracked and compared against their optimal rate to ensure the system is operating within the required range. It was shown that by taking future CSI into account, the convergence time to the optimal rate was greatly reduced when compared to adaptive

rate tracking without utilizing future CSI. Therefore, the proposed method has proven to outperform other methods for maximizing capacity and achieving long term fairness for each MS.

4.2 Future Work

The proposed methods in this thesis for transmit beamforming and OFDMA can be expanded for future work in a couple of different ways. TB assumed each channel was independent and followed a Rayleigh distribution. This assumption needs to be expanded to the point where the channels are correlated with each other. Furthermore, future work is being done to improve the pilot symbol assisted modulation method. Rather than having only pilot symbols for past channel realizations, to estimate the current channel at time t , the pilot symbols can be divided into two groups. Half of the pilot symbols can be inserted for past estimates of the current channel, along with the other half of the pilot symbols inserted with predicted future estimates of the current channel. This will in turn, give a much better estimate, improving the effects that ICE has on the system. Moreover, with these predicted future values of the channel, a more suitable TB vector can be selected to overcome the effects feedback delay produces. Also, precoding can be implemented to further increase gains, and also reduce the receiver complexity. Lastly, this thesis only considered MISO systems, TB with finite rate, delayed feedback, and ICE at the receiver, should be analyzed in regards to MIMO systems as well, to observe what occurs when the number of antennas are increased at the receiver.

Likewise, there is a great deal of future work needing to be accomplished for OFDMA. The proposed method for OFDMA assumed perfect channel knowledge of future channel realizations, when adaptive rate tracking is performed. For practical systems, these future channel realizations need to be predicted as stated in the TB case. With these predicted estimates, adaptive rate tracking will converge to the

optimal rate much faster.

Also, A MISO system was considered in the downlink case because of practical reasons. Most cellular phones have only one antenna, future phones will be equipped with multiple antennas. Therefore, the MIMO case should be considered as well. Furthermore, this thesis considered only a centralized scenario, where MSs communicate with the BS alone, and vice versa. Instead, a multihop network, where MSs can relay messages from other MSs to the BS should also be considered.

In addition, combining OFDMA with TB would make for an interesting research problem. This could further improve performance in terms of coding and multiplexing gains. However, these topics are beyond the scope of this thesis, but should be addressed in future research.

APPENDIX

Moment Generating Function of Received SNR Including ICE

The complex Gaussian quadratic form of $\gamma(t|T_d)$ conditioned on $\widehat{\mathbf{h}}(t - T_d)$ equals $v^* \beta \overline{\gamma}_s v$, where $v = \rho_{\text{tot}} \mathbf{w}_{\text{opt}}^H(t|T_d) \widehat{\mathbf{h}}(t - T_d) + \mathbf{e}_{\text{tot}}(t) \sim \mathcal{CN}(\rho_{\text{tot}} \mathbf{w}_{\text{opt}}^H(t|T_d) \widehat{\mathbf{h}}(t - T_d), \sigma_h^2(1 - |\rho_{\text{tot}}|^2))$. Following the results for Gaussian quadratic forms in [54], the conditional MGF of $\gamma(t|T_d)$ is obtained.

$$\phi_{\gamma(t|T_d, z)}(s|\mathbf{h}) = \frac{\exp\{|\rho_{\text{tot}}|^2 |\mathbf{w}_{\text{opt}}^H(t|T_d) \widehat{\mathbf{h}}(t - T_d)|^2 [(\beta \overline{\gamma}_s)^{-1} s^{-1} - \sigma_h^2(1 - |\rho_{\text{tot}}|^2)]^{-1}\}}{1 - s \beta \overline{\gamma}_s \sigma_h^2 (1 - |\rho_{\text{tot}}|^2)} \quad (\text{A.1})$$

Based on the quantization error z , it was shown earlier that $|\mathbf{w}_{\text{opt}}^H(t|T_d) \widehat{\mathbf{h}}(t - T_d)|^2 = (1 - z) \|\widehat{\mathbf{h}}(t - T_d)\|^2$, where $\gamma_h(t - T_d) = \|\widehat{\mathbf{h}}(t - T_d)\|^2$. Therefore, with this change of variables, the new equation with quantization error becomes

$$|\mathbf{w}_{\text{opt}}^H(t|T_d) \widehat{\mathbf{h}}(t - T_d)|^2 = (1 - z) \gamma_h(t - T_d). \quad (\text{A.2})$$

Since $\gamma_h(t - T_d)$ is a scaled chi-square variable with $2N_t$ degrees of freedom, the MGF becomes $\phi_{\gamma_h(t - T_d)}(s) = E[e^{s\gamma_h(t - T_d)}] = \frac{1}{(1 - s\sigma_h^2)^{N_t}}$. Substituting (A.2) into (A.1) the conditional MGF becomes

$$\phi_{\gamma(t|T_d, z)}(s|\mathbf{h}) = \frac{\exp\{|\rho_{\text{tot}}|^2 (1 - z) \gamma_h(t - T_d) [(\beta \overline{\gamma}_s)^{-1} s^{-1} - \sigma_h^2(1 - |\rho_{\text{tot}}|^2)]^{-1}\}}{1 - s \beta \overline{\gamma}_s \sigma_h^2 (1 - |\rho_{\text{tot}}|^2)}, \quad (\text{A.3})$$

where $s = |\rho_{\text{tot}}|^2 (1 - z) ((\beta \overline{\gamma}_s)^{-1} s^{-1} - \sigma_h^2(1 - |\rho_{\text{tot}}|^2))^{-1}$. Substituting s into (A.3) and

taking the expectation with respect to the channel \mathbf{h} , the average MGF is defined as

$$\begin{aligned}\phi_{\gamma(t|T_d,z)}(s) &= E\left[\frac{e^{s\gamma_h(t-T_d)}}{1 - s\beta\bar{\gamma}_s\sigma_h^2(1 - |\rho_{\text{tot}}|^2)}\right] \\ &= \frac{(1 - s\sigma_h^2)^{-N_t}}{1 - s\beta\bar{\gamma}_s\sigma_h^2(1 - |\rho_{\text{tot}}|^2)}.\end{aligned}\tag{A.4}$$

By replacing s with its actual value and simplifying (A.4), the average MGF becomes

$$\begin{aligned}\phi_{\gamma(t|T_d,z)}(s) &= \frac{[1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2)]^{N_t-1}}{[1 - s\beta\bar{\gamma}_{s,h}(1 - |\rho_{\text{tot}}|^2z)]^{N_t}} \\ &= \frac{[1 - \frac{s}{s_1}]^{N_t-1}}{[1 - \frac{s}{s_2}]^{N_t}},\end{aligned}\tag{A.5}$$

where $s_1 = \frac{1}{\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2)}$ and $s_2 = \frac{1}{\beta\bar{\gamma}_{s,h}(1-|\rho_{\text{tot}}|^2z)}$.

BIBLIOGRAPHY

- [1] T. B. M. Gadze, D. Nogulic, “Smart antenna systems for broadband technologies,” *48th International Symposium*, pp. 171–174, 7-9 June 2006.
- [2] S. Alamouti, “A simple transmit diversity technique for wireless communications,” *IEEE J. Sel. Areas Commun.*, vol. 16, pp. 1451–1458, Oct. 1998.
- [3] N. S. V. Tarokh and A. R. Calderbank, “Space-time codes for high data rate wireless communication: Performance criterion and code construction,” *IEEE Transactions on Information Theory*, vol. 44, pp. 744–765, Mar. 1998.
- [4] S. Zhou and G. B. Giannakis, “Optimal transmitter eigen-beamforming and space-time block coding based on channel correlations,” *IEEE Transactions on Information Theory*, vol. 49, pp. 1673–1690, Jul. 2003.
- [5] M. D. T. A. Narula, M. J. Lopez and G. W. Wornell, “Efficient use of side information in multiple-antenna data transmission over fading channels,” *IEEE J. Sel. Areas Communications*, vol. 16, pp. 1423–1436, Oct. 1998.
- [6] J. H. Winters, “The diversity gain of transmit diversity in wireless systems with rayleigh fading,” *IEEE Transactions on Veh. Technol.*, vol. 47, pp. 119–123, Feb. 1998.
- [7] S. Z. P. Xia and G. B. Giannakis, “Multi-antenna adaptive modulation with beamforming based on bandwidth-constrained feedback,” *IEEE Transactions on Communications*, vol. 53, pp. 526–536, Mar. 2005.
- [8] E. Visotsky and U. Madhow, “Space-time transmit precoding with imperfect feedback,” *IEEE Transactions on Information Theory*, vol. 47, pp. 2632–2639, Sep. 2001.
- [9] S. Zhou and G. B. Giannakis, “Optimal transmitter eigen-beamforming and space-time block coding based on channel mean feedback,” *IEEE Transactions on Signal Process.*, vol. 50, pp. 2599–2613, Oct. 2002.
- [10] N. J. A. Goldsmith, S. A. Jafar and S. Vishwanath, “Capacity limits of MIMO channels,” *IEEE J. Sel. Areas Commun.*, vol. 21, pp. 684–702, Jun. 2003.
- [11] H. Boche and E. A. Jorswieck, “Optimal power allocation for MISO systems and complete characterization of the impact of correlation on the capacity,” *Proc. Int. Conf. Acoust., Speech, and Signal Process.*, pp. 373–376, Apr. 2003.

- [12] S. Simon and A. Moustakas, "Optimizing MIMO antenna systems with channel covariance feedback," *IEEE J. Sel. Areas Commun.*, vol. 21, pp. 406–417, Apr. 2003.
- [13] S. A. Jafar and A. Goldsmith, "On optimality of beamforming for multiple antenna systems with imperfect feedback," *Proc. IEEE int. Symp. Information Theory*, p. 321, June 2001.
- [14] A. Moustakas and S. Simon, "Optimizing multiple-input single-output MISO communications systems with general Gaussian channels: Non-trivial covariance and nonzero mean," *IEEE Transactions on Information Theory*, vol. 49, pp. 2770–2780, Oct. 2003.
- [15] H. Sampath and A. Paulraj, "Linear precoding for space-time coded systems with known fading correlations," *IEEE Commun. Lett.*, vol. 6, pp. 239–241, Jun. 2002.
- [16] R. Blum, "MIMO with limited feedback of channel state information," *Proc. of IEEE int. Conf. Acoust., Speech, and Signal Process.*, vol. 4, pp. 89–92, Apr. 2003.
- [17] G. B. G. S. Zhou, Z. Wang, "Quantifying the power loss when transmit beamforming relies on finite rate feedback," *IEEE Transactions on Wireless Commun.*, vol. 4, pp. 1948–1957, Jul. 2005.
- [18] R. B. Theodore S. Rappaport, A. Annamalai and W. H. Tranter, "Wireless communications: past events and a future perspective," *IEEE Commun. Mag.*, vol. 40, pp. 148–161, May 2002.
- [19] V. Singh and V. Sharma, "Efficient and fair scheduling of uplink and downlink in IEEE 802.16 OFDMA networks," *IEEE Wireless Communications and Networking Conference*, vol. 2, pp. 984–990, Apr. 2006.
- [20] W. X. Robert Love, Amitava Ghosh and R. Ratasuk, "Performance of 3GPP high speed downlink packet access HSDPA," *IEEE Vehicular Technology Conference*, vol. 5, pp. 3359–3363, 26–29 Sept. 2004.
- [21] P. Li and W. Wu, "The comparison of performances when WCDMA and HSDPA coexist in two different environments," *International Conference on Wireless Communications Networking and Mobile Computing*, vol. 2, pp. 824–828, 23–26 Sept. 2005.
- [22] J.-C. K. Simon Shin, Chan-koo Kang and S.-H. Oh, "The performance comparison between WiBro and HSDPA," *International Symposium on Wireless Communication Systems*, pp. 346–350, 5–7 Sept. 2005.
- [23] X. S. Jun Cai and J. W. Mark, "Downlink resource management for packet transmission in OFDM wireless communication systems," *IEEE Trans. on Wireless Communications*, vol. 4, pp. 1688–1703, July 2005.

- [24] C. Y. Wong and R. S. Cheng, "Multiuser OFDM with adaptive subcarrier, bit, and power allocation," *IEEE Journal on Selected Area in Communications*, vol. 17, pp. 1747–1758, Oct. 1999.
- [25] W. Yu and J. M. Cioffi, "FDMA capacity of gaussian multiple-access channels with ISI," *IEEE on Transactions Communications*, vol. 50, pp. 102–111, Jan. 2002.
- [26] G. Song and Y. G. Li, "Adaptive subcarrier and power allocation in OFDM based on maximizing utility," *IEEE Vehicular Technology Conf.*, pp. 905–909, Apr. 2003.
- [27] J. Jang and K. B. Lee, "Transmit power adaptation for multiuser OFDM systems," *IEEE Journal on Selected Areas in Communications*, vol. 21, pp. 171–178, Feb. 2003.
- [28] Y. H. Keunyoung Kim and S.-L. Kim, "Joint subcarrier and power allocation in uplink OFDMA systems," *IEEE Communications Letters*, vol. 9, pp. 526–528, June 2005.
- [29] C. Mohanram and S. Bhashyam, "A sub-optimal joint subcarrier and power allocation algorithm for multiuser OFDM," *IEEE Communications Letters*, vol. 9, pp. 685–687, Aug. 2005.
- [30] J. G. A. Zukang Shen and B. L. Evans, "Adaptive resource allocation in multiuser OFDM systems with proportional rate constraints," *IEEE Trans. on Wireless Comm.*, vol. 4, pp. 2726–2737, Nov. 2005.
- [31] Y. Ma, "Proportional fair scheduling for downlink OFDMA," *Proc. IEEE ICC'07*, pp. 4843–4848, June 2007.
- [32] L. Yang and M.-S. Alouini, "Performance analysis of multiuser selection diversity," *IEEE Trans. on Vehicular Technology*, vol. 55, pp. 1848–1861, Nov. 2006.
- [33] D. Love and J. R. W. Heath, "Limited feedback precoding for spatial multiplexing systems," *Proc. Global Telecommunications Conf.*, vol. 4, pp. 1857–1861, Dec. 2003.
- [34] F. Jöngren and M. Skoglund, "Utilizing quantized feedback information in orthogonal space-time block coding," *Proc. Global Telecommunications Conf.*, vol. 2, pp. 995–999, Nov. 27-Dec. 1 2000.
- [35] D. J. Love and R. W. Heath, "Equal gain transmission in multiple-input multiple-output wireless systems," *IEEE Transactions on Communications*, vol. 51, pp. 1102–1110, Jul. 2003.
- [36] J. Robert W. Heath and A. J. Paulraj, "Switching between diversity and multiplexing in MIMO systems," *IEEE Trans. on Commun.*, vol. 53, pp. 962–968, June 2005.

- [37] D. Tse and P. Viswanath, *Fundamentals of Wireless Communication*. Cambridge University Press, 2005.
- [38] R. N. Rui Zhang, Ying-Chang Liang and J. M. Cioffi, "Approaching MIMO-OFDM capacity with per-antenna power and rate feedback," *IEEE Journal on Selected Areas in Communications*, vol. 25, pp. 1284–1297, Sept. 2007.
- [39] G. D. G. P. W. Wolniansky, G. J. Foschini and R. A. Valenzuela, "V-blast: An architecture for realizing very high data rate over the rich scattering wireless channel," *URSI International Symposium on Signals, Systems, and Electronics*, pp. 295–300, 29 Sept.-2 Oct. 1998.
- [40] J. Choi, "Capacity/throughput optimization for H-BLAST with SC receiver over MIMO channels," *IEEE Transactions on Wireless Channels*, vol. 7, pp. 1016–1024, March 2008.
- [41] M. J. G. C. P. Gerald J. Foschini, Dmitry Chizhik and R. A. Valenzuela, "Analysis and performance on some basic space-time architectures," *IEEE Journal on Selected Areas in Communications*, vol. 21, pp. 303–320, Apr. 2003.
- [42] B. G. S. Thoen, L. Van der Perre and M. Engels, "Performance analysis of combined transmit-SC/receive-MRC," *IEEE Transactions on Communications*, vol. 49, pp. 5–8, Jan. 2001.
- [43] M. J. V. K. N. Lau and Y. Liu, "Cross layer design of uplink multi-antenna wireless systems with outdated csi," *IEEE Transactions on Wireless Commun.*, vol. 5, pp. 1250–1253, Jun. 2006.
- [44] S. Zhou and G. B. Giannakis, "Adaptive modulation for multiantenna transmissions with channel mean feedback," *IEEE Transactions on Wireless Commun*, vol. 3, pp. 1626–1636, Sep. 2004.
- [45] R. H. H. J. H. Conway and N. J. A. Sloane, "Packing lines, planes, etc.: Packings in grassmannian space," *Exp. Math*, vol. 5, no. 2, pp. 139–159, 1996.
- [46] J. D. J. Love, R. W. Heath and T. Strohmer, "Grassmannian beamforming for multiple-input multiple-output wireless systems," *IEEE Transactions on Information Theory*, vol. 49, pp. 2735–2747, Oct. 2003.
- [47] D. Love, <http://dynamo.ecn.purdue.edu/djlove/grass.html>. Jun. 2005.
- [48] M. K. Simon and M. S. Alouini, *Digital communications over generalized fading channels: A unified approach to the performance analysis*. New York: Wiley, 2000.
- [49] Y. Ma and D. Zhang, "Error rate of transmit beamforming with delayed and limited feedback," *IEEE Global Telecommunications Conference*, pp. 4071–4075, 26-30 Nov. 2007.

- [50] A. L. Yao Ma and R. Schober, "Predictive feedback for transmit beamforming with delayed feedback and channel estimation errors," 2008. submitted for publication.
- [51] A. L. Yao Ma, Dongbo Zhang and Z. Wang, "Error rate of transmit beamforming with delayed and limited feedback," *IEEE Trans. on Wireless Communications*, 2008. submitted for publication.
- [52] R. S. Yao Ma and S. Pasupathy, "Performance of M-PSK with GSC and EGC with Gaussian weighted errors," *IEEE Transactions on Vehicular Technology*, vol. 54, pp. 149–162, Jan. 2005.
- [53] Y. Ma and J. Jin, "Effect of channel estimation errors on M-QAM with MRC and EGC in nakagami fading channels," *IEEE Transactions on Vehicular Technology*, vol. 56, pp. 1239–1250, May 2007.
- [54] A. Mathai and S. Provost, *Quadratic forms in random variables: Theory and applications*. New York 10016: Marcel Dekker, 1992.
- [55] F. K. L. M. C. Oghenekome Oteri, Nicolae Chiurtu and A. Paulraj, "Studies in downlink spectral efficiency of OFDMA networks with MIMO and opportunistic scheduling," *IEEE Global Telecommunications Conf.*, pp. 1–6, Nov. 2006.
- [56] D. C. M. S. V.S. Abhayawardhana, I.J. Wassell and M. Brown, "Comparison of empirical propagation path loss models for fixed wireless access systems," *IEEE Vehicular Technology Conference*, vol. 1, pp. 73–77, 30 May-1 June 2005.
- [57] A. L. Yao Ma and D.-I. Kim, "Sum rate optimization of multi-cell cognitive radio networks with spectral mask constraint," *Proc. IEEE Global Comm*, 2008. accepted for publication.
- [58] Y. Ma, "Rate-maximization for downlink OFDMA with proportional fairness," *IEEE Trans. Veh. Technol.*, 2007.
- [59] M.-S. A. Lin Yang and D. Gesbert, "Further results on selective multiuser diversity," *Proc. MSWiM'04*, pp. 25–30, Oct. 25-30 2004.
- [60] A. Goldsmith, *Wireless Communications*. Cambridge University Press, 2005.