Extremely Weakly Interacting $\Delta S_z = 0$ and $\Delta S_z = 1$ Excitations and Evidence for Fractional Quantization in a Magnetization Plateau: CeSb

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Abstract
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Extremely Weakly Interacting $\Delta S_z = 0$ and $\Delta S_z = 1$ Excitations and Evidence for Fractional Quantization in a Magnetization Plateau: CeSb

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The plateau at 1/3 of the saturation magnetization $M_s$ in the metamagnet CeSb is accompanied by a state of ferromagnetic layers of spins in an up-up-down sequence. We measured $M$ and the specific heat $C$ in the plateau, spin wave analyses of which reveal two distinct branches of excitations. Those with $\Delta S_z = 1$ as measured by $M$, coexist with a much larger population of $\Delta S_z = 0$ excitations measured by $C$ but invisible to $M$. The large density of $\Delta S_z = 0$ excitations, their energy gap, and their seeming lack of interaction with $\Delta S_z = 1$ excitations suggest an analogy with astrophysical dark matter. Additionally, in the middle of the plateau three sharp jumps in $M(H)$ are seen, the size of which, $0.15\% M_s$, is consistent with fractional quantization of magnetization per site in the down-spin layers.

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Over the last few decades, magnetization plateaus have provided a rich source for the study of quantum magnetism. These plateaus have been shown to arise in metamagnets, low-dimensional magnets, and geometrically frustrated systems and are understood to result from a gap in the many-body energy spectrum analogous to that underlying the fractional quantum Hall effect (QHE) [1,2]. In such systems, a physical quantity is quantized over specific magnetic field ranges due to a topological commensurability between localized excitations and the lattice, resulting in translational symmetry breaking [3]. For spin models, this quantization condition is expressed as $n(S-m) = \text{integer}$ in the plateaus, where $n$ is the translational period of the ground state, $S$ is the total spin per site, and $m$ is the magnetization per site in units of spin quantum number [1,3].

In order to better understand topological quantization in magnetic systems, we chose the metallic metamagnet CeSb, which in zero field $(H)$ undergoes simultaneous antiferromagnetic ordering and a structural transition from its high temperature NaCl phase to tetragonal symmetry at $T_N = 16$ K [4]. At finite $H$ and lower $T$, CeSb exhibits a large number of ordered phases which have been identified and extensively studied by magnetization [4–9], specific heat [4,10–13], neutron diffraction [6–8,12,14–19], x-ray diffraction [19,20], ARPES [21], and charge transport [9,22,23]. The Ce$^{3+}$ moments in CeSb arise from a $J = 5/2$ ($T_2$) doublet ground state (equivalent to an effective $S = 1/2$ and an effective $g$ factor $g = 4.28$) and an anisotropic spin-spin interaction, attributed to strong mixing of the Ce $f$ states with neighboring $p$ orbitals in Sb [5,18]. While the magnetic response is anisotropic with an easy axis [5], inelastic neutron scattering sees dispersive magnetic excitations [14,15] indicating only partial Ising character. In the ordered states, the spins are ferromagnetically aligned in layers perpendicular to $(0,0,1)$ with the multiplicity of states corresponding to different repeat patterns of spin planes, aligned and anti-aligned with $H|| (0,0,1)$ [12]. The plateau corresponding to 1/3rd of the saturation magnetization, $M_s$, occurring for $2.1 \leq H \leq 3.7$ T and $T < 10$ K, is defined by a quantization condition among layers which triples the unit cell in an up-up-down ($\uparrow \uparrow \downarrow$) sequence [1,3], and can be relatively flat in high quality crystals [9]. The quantization condition parameters for this plateau are thus $n = 3$, $S = 1/2$, and $m = (1/3)(1/2) = 1/6$.

In this work we present studies of the magnetization $M(T,H)$ and specific heat $C(T,H)$ in the 1/3rd plateau $(n = 3)$ of CeSb. We find that the slope of $M$ vs $H$ or “plateau susceptibility,” $\chi_p$, in the 1/3rd phase is $1.15 \times 10^{-2}$ emu/mole and weakly temperature dependent between 2–9 K. Application of spin wave theory to explain the temperature dependences in $M$ and $C$ leads to a large discrepancy in the spin wave stiffness between these two quantities, indicating the presence of two distinct excitation branches. The $\Delta S_z = 0$ excitations probed by $C$ are likely due to time-reversed pairs of spins across interfaces between up and down layers, revealing a spin flip density in the down layers of 9% at the high-temperature boundary of the plateau. The seeming invisibility of the large population of $\Delta S_z = 0$ excitations to $M$ suggests an analogy to dark matter. Furthermore, on close inspection, the shape of the plateau resembles a Brillouin function, characteristic of free spins, on top of which we observe distinct “mini” jumps whose magnitude and width suggest two-dimensional long-range ordering among $\Delta S_z = 1$.
excitations in the down layers. Moreover, by subtracting an arbitrary free-spin background, the jumps reveal plateaus which are consistent with fractional quantization conditions within the down layers.

Crystals of CeSb were grown from a flux (Supplemental Material [24]) and have a cubic morphology with an average cube side of 5 mm and mass of approximately 60 mg. For this work, we confirmed reproducibility of the data shown below on three different samples from two growth runs. The dc magnetization was measured in a Quantum Design superconducting quantum interference device (SQUID) magnetometer with hysteresis protocols described below for $H$ along a cubic axis to an accuracy of $\sim 1\%$. Measurements of $C(T)$ were made using the relaxation method in a Quantum Design physical property measurement system. The lattice contribution to $C(T)$ in CeSb was identified with the specific heat of a single crystal of nonmagnetic LaSb, grown for this purpose. All data presented here have this lattice contribution subtracted, and thus represent the magnetic contribution to $C(H,T)$; see Supplemental Material [24] for lattice subtraction methods, which includes Refs. [25–27].

In Fig. 1(a), we present $M(H,T)$ for both increasing and decreasing external fields, and find consistency with previous results. We note that the temperature dependence of $M(H)$ within the plateau is (i) small, with $dlnM/dT \approx 0.0013 \text{ K}^{-1}$ and, (ii) much less for decreasing $H$ than for increasing $H$, a point to which we will return later. As $H$ increases out of the plateau and into the aligned paramagnetic phase, $M$ reaches its saturation value $M_s = 1.116 \times 10^4 \text{ emu/mole} = 2.0 ~ \mu_B$, as observed previously [9]. The deviation from the free-ion value of $2.14 ~ \mu_B$ is ascribable to the presence of the near-lying $\Gamma_5$ quartet [28].

In Fig. 1(b), we present $C(H)/T$ from $H = 1–5 \text{ T}$, taken on increasing field with the 1/3rd plateau clearly delineated as a mesalike feature indicating an increase in available states within the plateau. Most importantly, the temperature dependence of $C(H)/T$ taken between 2 and 9 K is $\mid dln(C/T)/dT \mid \approx 0.29 \text{ K}^{-1}$, i.e., a factor of 200 times greater than $dlnM/dT$. By contrast, usual antiferromagnets such as Dy$_3$Al$_5$O$_{12}$ display $\frac{dln(C/T)}{dT} \approx \frac{dlnM}{dT}$ [29].

Before addressing the sub-gap structure in $M(H)$, we attempt to model the dramatically different temperature dependences of $M$ and $C/T$ by spin waves. Viewing the FM layers as independent systems, as $H$ is increased the up layers see an increasing local field and the down layers see a decreasing local field. This dictates a decreasing spin wave density with $H$ for the up layers (larger local gap) and an increasing spin wave density for the down layers (smaller local gap). Thus, in the independent-layer scenario, the combined effect implies that the down layer will dominate temperature-induced changes in $M$. Following Niira’s modification [30] of Bloch’s theory to include an anisotropy-induced spin wave gap $\Delta$, the temperature dependence of $M$ can be expressed as $M(T)/M_s = 1 - AT^{3/2} e^{-\Delta M/\omega}$, where $A$ depends on fundamental constants $M_s$ and the spin wave stiffness, and the gap $\Delta M$ depends on the internal magnetic field. As shown in Figs. 2(a) and 2(b), we find good agreement to spin wave fits of $M(T)$ and a corresponding form for $C(T)/T$ [31] at constant fields in the 1/3rd phase. For the fits to $M(T)$ and $C(T)$ we used the data obtained on increasing $H$ and we discuss the down sweeps separately below. The spin wave stiffness for $M(T)$ and $C(T)$ was found to be $111–119$ and 10.3 $\text{ K}^2$, respectively. The spin wave gaps [Fig. 2(c)] extracted from the fits of $M$ and $C$ are $\Delta_M = 15–20$ and $\Delta_C = 22.9$ K, respectively. In contrast to the large difference in spin wave stiffness, the gap values from $C$ and $M$ are within 50% of each other, showing that the two excitation types probed by $C$ and $M$ see similar gaps but with vastly different density of states. The integrated entropy $\Delta S = \int C/T$ from 2 to 9 K in the plateau is $9\% R \ln 2$.

The simple spin wave analysis above belies the complex microscopic nature of the charge-spin-orbital degrees of freedom at play in CeSb. Although the degeneracy lifting represented by the various magnetic transitions below $T_N$ is among $J = 5/2$ doublets, the energy gap to the excited $S = 3/2$ ($\Gamma_8$) quartet is only 24 K [13], i.e., comparable to the gap inducing the plateau. Such an excited state for free spins in a field of 3 T would produce a total entropy between $2–9$ K, $(1/3)S_{\text{quartet}} = 2.36 \text{ J/mole K}$, greatly exceeding that of CeSb, $S = 0.55 \text{ J/mole K}$ (see Fig. 2, Supplemental Material [24]). Thus, because the density of states for these crystal field excitations is significantly reduced compared to that of free spins, the effect of the energy gap associated with 1/3 quantization extends to the suppression of the excited state population. Ambiguity in the precise nature of the $\Delta S = 0.1$ excitations does not alter the main observation, however, that they are extremely weakly interacting.
FIG. 2. (a) Magnetization vs temperature at fixed fields, the values of which are given in frame (b). The solid lines are fits to a spin wave form. (b) Specific heat/temperature vs temperature at different fields (data lie on top of each other). The solid lines are fits to a spin wave form. (c) The energy gaps resulting from the spin wave fits for both magnetization and specific heat. For all fits, $\gamma = 5 \text{ mJ/mole K}^2$, $D = 1.11 \text J/mole K^{5/2}$ and $\Lambda = -0.0023 \text{ K}^{-3/2}$ are held constant.

The situation of two types of excitations equal in energy but not interacting is reminiscent of Herring's description of accidental degeneracy of free electrons [32]. In magnetic systems, similarity is found in frustrated $s = 1/2$ Heisenberg spin models such as the frustrated spin chain [33,34] and the antiferromagnetic kagome lattice [35], both of which exhibit magnetization plateaus. For the kagome lattice at $H = 0$, however, both exact diagonalization and mean field analyses reveal distinct sectors of gapped triplet excitations coexisting with gapless singlet excitations [36,37]. The present situation differs from these $T = 0$ analogues in that the $\Delta S_z = 0$ excitations possess a gap reflecting the many-body spectrum and thus would arise from a mass term in an effective Hamiltonian. Because the $\Delta S_z = 0$ excitations are simultaneously dense in the down layer while also invisible to $M(H)$ suggests an analogy to astrophysical dark matter. While the origin of dark matter is of course unknown, the present situation is more tractable. Since the mini jumps are likely due to ordering among localized $\Delta S_z = 1$ excitations, an excitation not resulting in a change of $M$ must involve flips of two spins, one aligned and one anti-aligned with $H$. Thus, one of the two spins must come from the down layer and the other from a nearby up-layer. If half of the 9.0% $Rn$ entropy developed up to 9 K is in the down layer, which represents only 1/3rd of all spins, then approximately 15% of the down layer spins will be reversed. This large density of spin flips should lead to a similar effect in the mean field, evinced in both the plateau as well as $\Delta C$, as shown in Fig. 2(c).

The astrophysical analogy suggested above can be extended by considering that the term “dark” corresponds to the absence of elastic scattering of photons from a large amount of mass inferred from observations of galaxy expansion. One might ask whether an analogue of photons, namely neutrons, are able to image $\Delta S_z = 0$ excitations in CeSb. While it is unlikely that such excitations are directly observable in the neutron elastic channel, their presence might be inferred from accurate diffraction measurements as a decrease in ordered moment of the $\uparrow \downarrow \downarrow$ phase as $T$ is increased within the plateau. Of course, the present system also admits the possibility of inelastic scattering, which should allow direct imaging of $\Delta S_z = 0$ excitations as a flat band at the gap energy. Such a measurement would complement the specific heat by providing a way to image magnetically dark excitations using inelastic radiative processes. A class of systems with more relevance to CeSb are the QHE systems. Despite evidence that the fractional ground states are spin polarized, thus lacking a singlet degree of freedom, the observation of oscillations in $C(H)$ measurements [38] makes it reasonable to ask if measurements of the $T$ dependence would reveal magnetically dark excitations.

We now address the mini jumps in the middle of the plateau. Above a Brillouin-function-like background, three mini jumps are seen at 2.7, 2.9, and 3.1 T for $H$ up sweeps and one distinct jump at 2.85 T for $H$ down sweeps, as shown in the inset of Fig. 1(a). Often, small jumps in $M(H)$ are observed close to the major jumps straddling a plateau and are associated with incomplete ordering related to sample inhomogeneity. By contrast, the mini jumps in CeSb occur in the middle of the 1/3rd plateau. In addition, we observe these jumps in three different samples at virtually the same field values, as shown in Fig. 4(b), which argues against an extrinsic explanation. The jumps are characterized by their size, $\sim 0.0015$ of $M_s$, and by their width, which is comparable to the width of the major jumps. No corresponding features are observed in $C(H)$, consistent with the lower precision of this measurement compared to SQUID-based $M(H)$.

Since the large jumps in $M(H)$ occur at plateau boundaries, it is reasonable to ask if the mini jumps are associated with mini plateaus, and thus with an additional topological quantization condition. As discussed above, such a quantization condition relates the jump height inversely to the period of broken spatial symmetry.
If the broken symmetry is in the same direction as that associated with the $1/3$ quantization, (001), then $0.0015M_s$ implies a period of $\sim 670$ lattice constants, which is extremely unlikely. More likely is that the spatially broken symmetry is transverse to (001). Moreover, due to the order within the plateau, it is reasonable to assume that the mini jumps correspond to spin-flip ordering only within the $\uparrow$ layer since the $\uparrow$ layer spins should be nearly fully polarized along $H$. In this case, for the largest of the mini jumps such spin flips would be separated by $[(1/3M_s)/0.0015M_s]^{1/2} \sim 15$ lattice constants in the down layer and the smaller “satellite” jumps indicate a larger separation. While such a repeat period is still quite large on the scale of usual atomic spin ordered wavelengths, we note that skyrmion lattices can exhibit such large lattice constants [39].

If, as argued above, the mini jumps correspond to plateaus related to spatial symmetry breaking in the $\downarrow$ layers, then the finite $M(H)$ slope in the $1/3$rd plateau masks the mini plateaus. Is it possible, then, to separate the spin-wave background from the mini-plateau $M(H)$? Since the spin wave analysis above describes $M(H)$ well and since it has the shape of a Brillouin function, $B(x)$, we model the background spin-wave contribution as $M_{\text{Brillouin}} = n g S \mu_B B(x)$, where $n$ is a molar spin density, $x = g S \mu_B H_{P_{\text{eff}}} / k_B T$, and $H_{P_{\text{eff}}} = H - H_{P0}$, with $H_{P0} = 2.4-2.55$ T, from 9–2 K, respectively, being the lower boundary at which the Brillouin function fit was made. We subtract from each up-sweep isotherm $M_{\text{Brillouin}}(H; T)$, with $n$ adjusted to achieve flatness in $M - M_{\text{Brillouin}}$. As shown in Fig. 3, for each isotherm a single $B(x)$ function produces plateau like regions for all three mini jumps and the inset of Fig. 3 shows the values of $n$ required to produce such flatness. Since the spin-wave spectrum is probably quite complex, given the different sublattices and exchange constants [18], it is surprising that a simple Brillouin function parameterization produces such flat mini plateaus.

![FIG. 3. Magnetization data on field up sweep in the 1/3rd plateau vs magnetic field difference from the lower boundary $H_{P0}$ of the plateau region. The data shown are those in Fig. 1 with a Brillouin function subtracted, as described in the text. The inset shows the fraction of free spin density per formula unit used in the Brillouin function subtraction.](image)

![FIG. 4. (a) Field derivative of the magnetization in the 1/3rd plateau region vs field, indicating the positions of the mini jumps. The open circles mark the $f_p = 1/2$ field value for each temperature. (b) Positions of the mini jumps in multiple samples of CeSb. Sample peaks were scaled to comparable magnitudes and set relative to the field width of the 1/3rd plateau in each sample.](image)
For any plateau system, the magnitude of field where $M(H)$ enters a plateau is significant only for providing information on the internal mean field. Nevertheless, it is of possible future interest to note the precise location of the mini jumps. In Fig. 4(a), $dM/dH$ for the jumps provides their precise positions and variation with $H$ and $T$. We see that the central, and largest, of the jumps asymptotically approaches as $T \to 2\,K$, a field value corresponding to $H = H_i + f_p \Delta H_{1/3}$ where $\Delta H_{1/3} = 1.7 \pm 0.1\,T$ is the width of the 1/3rd plateau and $f_p = 1/2$ (see Supplemental Material [24]). Small variations in the width, lower, and upper field boundaries are seen from 2–9 K, which adjust the $f_p = 1/2$ field value at each temperature. The $f_p = 1/2$ field values appear to converge upon decreasing $T$ [open circles Fig. 4(a)]. The other two jumps seem to approach $f_p = 3/8$ and 5/8.

Finally, we address the hysteresis of $M(H)$ observed in the 1/3rd plateau region. Such hysteresis is not uncommon and usually appears near the steps straddling the plateau. The cause of hysteresis in such cases is likely similar to and usually appears near the steps straddling the plateau. The magnitude of such a mechanism may explain the small difference in pinning of domain walls by defects or impurities. While $\Delta T$ seem to approach $T$ decreasing $H$, the $1$ seems to approach $T$ decreasing $H$, $1$ provides their precise positions and variation with $H$ and $T$. The $f_p = 1/2$ field value at each temperature. The $f_p = 1/2$ field values appear to converge upon decreasing $T$ [open circles Fig. 4(a)]. The other two jumps seem to approach $f_p = 3/8$ and 5/8.

To summarize, we have shown via $C(T)$ measurements within the 1/3rd plateau of CeSb, the presence of a separate $\Delta S_c = 0$ branch of excitations invisible to $M(H)$ and interacting with $\Delta S_c = 1$ in a manner evocative of dark matter in the astrophysical context. In addition, the $\Delta S_c = 1$ excitations reveal sharp small jumps in $M(H)$ that imply additional translational symmetry breaking in the down-spin layers. Further study of these phenomena will include small angle neutron scattering, ultralow temperature magnetothermal and transport measurements, and theoretical studies. Also of interest would be an exploration of the integer and fractional QHEs to test for excitations analogous to the $\Delta S_c = 0$ magnetically dark excitations we have observed in CeSb.

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