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Abstract
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Disciplines
Materials Chemistry | Other Chemistry | Physical Chemistry

Comments

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Zn$_{13}$Sb$_{10}$: A Structural and Landau Theoretical Analysis of Its Phase Transitions

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Composition, crystal structures, polymorphic transformations, and stability of the thermoelectric material known in the literature as "Zn$_4$Sb$_3$" have been studied on a polycrystalline sample and Bi-flux-grown single crystals using X-ray diffraction techniques, resistance, and Seebeck coefficient measurements at various temperatures ranging from 4 to 773 K. Microprobe analysis yields the composition of the flux-grown crystals to be close to Zn$_{13}$Sb$_{10}$ with minor Bi doping. High-temperature X-ray and Seebeck coefficient studies show that the phase is unstable at high temperatures in a vacuum because of Zn losses. Both X-ray diffraction and resistivity measurements indicate the presence of two consecutive symmetry-breaking transitions below room temperature, in agreement with our previous results on polycrystalline samples. Application of Landau theory suggests that the first $R3c \rightarrow C2/c$ symmetry breaking may be second-order in nature. The second, low-temperature symmetry breaking may proceed along two routes. One of these pathways, a first-order $C2/c \rightarrow C1$ symmetry reduction, may lead to an incommensurate structure and is consistent with our experimental observations.

Introduction

The recent elucidation of the crystal structure of the state-of-the-art thermoelectric material "Zn$_4$Sb$_3$" produces a better understanding of its unique physical properties.1-3 According to Slack’s nomenclature,4 Zn$_4$Sb$_3$ is a real “phonon-glass and electron-crystal”. Large atomic deficiencies (~10%) on the main Zn site and presence of additional, partially occupied electron-crystal”. Large atomic deficiencies (~10%) on the main Zn site and presence of additional, partially occupied Zn sites in room-temperature $\beta$-Zn$_4$Sb$_3$ effectively dampen heat-carrying phonons: the thermal conductivity of Zn$_4$Sb$_3$ approaches that of amorphous materials.5 On the other hand, the electrical conductivity retains values typical for heavily doped semiconductors.$^3,^6$

The process of establishing the crystal structure of $\beta$-Zn$_4$Sb$_3$ has been quite remarkable and shows how complementary approaches can yield a coherent picture. The first studies on Zn$_4$Sb$_3$ were fueled by the search for new semiconductors.5,6 The process of establishing the crystal structure of $\beta$-Zn$_4$Sb$_3$ has been quite remarkable and shows how complementary approaches can yield a coherent picture. The first studies on Zn$_4$Sb$_3$ were fueled by the search for new semiconductors.5,6 On the other hand, the electrical conductivity retains values typical for heavily doped semiconductors.$^3,^6$

The room-temperature $\beta$-structure was initially determined by Bokii and Klevtsova7 (giving the refined X-ray formula of Zn$_4$Sb$_3$) and then by Mayer et al.,13 who introduced and refined a Zn/Sb mixture on one of the two Sb sites to retain the initial Zn$_4$Sb$_3$ sample composition. Further research done by Tapiero et al.14 showed that Zn$_{13}$Sb$_{10}$ is zinc deficient (Zn$_{14-\delta}$Sb$_3$) and revealed its instability at elevated temperatures: annealing of the Zn$_{13}$Sb$_{10}$ sample in a vacuum at 673 K leads to a significant reduction of the Zn content.

Interest in Zn$_4$Sb$_3$ recently revived when a high thermoelectric figure of merit ($ZT=1.3$ at 670 K) was reported.$^5$ Attempts to establish the true crystal structure of $\beta$-Zn$_4$Sb$_3$ ensued. We performed room-temperature X-ray single-crystal analysis and proposed the formula Zn$_{10-\delta}$Sb$_3$ (we found there is no Zn/Sb mixture and the Zn site is ~90% occupied).15

As shown by other studies, this structural information was incomplete: additional, partially occupied Zn sites were not detected by us in $\beta$-Zn$_3$Sb$_2$. Three extra Zn sites with occupancies of 6.8, 6.8, and 3.3% were discovered using a maximum entropy method (MEM) analysis of synchrotron powder diffraction data.$^{1,2}$ The resulting Zn$_{13.83(5)}$Sb$_{10}$ (or Zn$_{53.85(2)}$Sb$_{35}$) composition$^2$ implies electron deficiencies (the full occupancy of the valence band is expected at Zn$_{13}$Sb$_{10}$) and, thus, $p$-type doping of $\beta$-Zn$_3$Sb$_2$, as found experimentally.$^5$

Further insight into the structural features of Zn$_3$Sb$_2$ comes from the work by Nylen et al.,$^3$ who studied the low-temperature $\alpha$-Zn$_3$Sb$_2$ at 150 K. They observed a rhombohedral-to-triclinic symmetry reduction upon cooling, accompanied by complete ordering of the additional interstitial Zn atoms in $\alpha$-Zn$_3$Sb$_2$. No deficiencies were found for either the “main” or the “extra” Zn atoms, thus yielding the Zn$_{13}$Sb$_{10}$ ($\alpha$-Zn$_3$Sb$_2$) composition for low-temperature $\alpha$-Zn$_3$Sb$_2$. As pointed out by Nylen et al., it is unlikely that the composition of Zn$_3$Sb$_2$ changes during the $\alpha \leftrightarrow \beta$ transition from Zn$_{13}$Sb$_{10}$ to Zn$_{12.83}$Sb$_{10}$. It is possible that slight Zn deficiencies were not detected by Nylen et al. in the low-temperature modification$^3$ and not all Zn atoms were located by Cargnoni et al. in the room-temperature modification.$^2$ Slight Zn deficiencies (the Zn$_{13.83}$-Sb$_{10}$ formula) could account for the observed $p$-type conductivity$^5$ and the temperature dependence of the conductivity,$^{15}$ which indicates an extrinsic character of the conductivity resulting from the presence of empty states in the valence band.

Another unresolved issue is the number and nature of the low-temperature phase transitions. Souma et al.$^6$ studied resistivity and other physical properties of Zn$_3$Sb$_2$ at low temperatures and reported only one phase transition, known as the $\alpha \leftrightarrow \beta$ one. In our opinion, the anomalies in the resistivity, as seen in their plots, may have indicated two consecutive transitions. Their experiments also showed that the $\alpha \leftrightarrow \beta$ transition temperature depends strongly on the preparation technique: $T_e$ is 257.4 and 236.5 K, respectively, for samples prepared by gradient-freeze and sintering methods. Our recent studies of heat capacity and resistance on a polycrystalline sample indicated the existence of two low-temperature phase transitions: one at 234 K and the other at 254 K.$^{15}$ We believe that the triclinic structure at 150 K, reported by Nylen et al.$^3$ refers to the low-temperature polymorph $\alpha$-Zn$_3$Sb$_2$ and that the rhombohedral structure, given by Cargnoni et al.,$^2$ describes the room-temperature polymorph $\beta$-Zn$_3$Sb$_2$, while the structure of the intermediate polymorph is unknown. Also, the nature of the high-temperature $\beta \leftrightarrow \gamma$ transition at 767 K ($T_i$ is taken from Izard et al.$^{16,17}$) and the structure of the $\gamma$-phase remain unresolved. In this paper, we will address the composition of Zn$_3$Sb$_2$ as well as the number and nature of its structural transitions by using a combination of X-ray diffraction (XRD) and Landau theory. 


### Experimental Section

**Synthesis.** The starting materials were pieces of zinc (99.999 wt %, Alfa Aesar), antimony (99.9999 wt %, Alfa Aesar), and bismuth (99.9995 wt %, Alfa Aesar). We prepared both polycrystalline and single-crystal samples. Details on the preparation of the polycrystalline sample with the initial composition of Zn$_3$Sb$_2$ can be found in ref 15. Single crystals were grown from a ternary melt, with Bi acting as a flux.$^{18}$ The starting elements were combined in the molar ratio 20:10:70 Zn/Sb/Bi in an alumina crucible and sealed in a silica-glass ampule with a partial pressure of argon. The ampule was heated to 650 °C and then slowly cooled, over a period of 60 h, to 290 °C, at which point the remaining melt was decanted. Crystals grown in this way formed blocks with a typical diameter of 1–2 mm.

**Microprobe Analysis.** Quantitative electron probe microanalysis was performed on a JEOI JXA-8200 Superprobe with 20 kV acceleration potential and 20 nA beam current. Small crystals extracted from the polycrystalline Zn$_3$Sb$_2$ sample were not suitable for mounting and polishing; instead, millimeter-size, flux-grown crystals were chosen for the electron probe microanalysis. Pure elements were used as standards. The X-ray lines used for analysis were Zn Kα, Sb Lα, and Bi Mα. Counting times of 10 s on the peak and 5 s each for high and low background were used.

Because the fourth-order Zn Kβ line is close to Bi Mα and the third-order Bi Lα line is close to Sb Lα, the pure element standards were also analyzed as unknowns. No interference was detected above the 0.04 wt % level, which is the nominal limit of detection. Analysis of 33 points indicated only slight Bi doping of the structure and yielded the average composition of Zn$_{56.5(1)}$Sb$_{43.2(2)}$Bi$_{0.0(5)}$. Assuming presence of Bi atoms only on the Sb sites (a Sb/Bi substitution), the composition of a Bi-free crystal can be written as Zn$_{56.5}$Sb$_{43.5}$, which is very close to Zn$_{56}$Sb$_{43}$. The real composition of Zn$_3$Sb$_2$ is better represented with the Zn$_{56}$Sb$_{43}$ formula, as proposed by Nylen et al.$^3$

**Resistance Measurements.** Our previous studies on the polycrystalline sample showed that resistance measurements could serve as a sensitive probe for the number and nature of phase transitions in Zn$_3$Sb$_2$. Therefore, we employed the same technique for studying transformational behavior of crystals grown from the Bi flux. Resistance was measured in the 4–350 K range using the standard four-probe method in commercial (Quantum Design) laboratory equipment on a bar cut from one of the crystals (dimensions 0.6 × 0.3 × 2 mm). Contacts to the sample were made with Epok H20E silver epoxy and Pt wires. Heating and cooling were done at rates of less than 0.5 K/min, and resistance values were recorded every 0.5 K. To explore the nature of the transformations the crystal was cycled through the transition temperatures. Resistivity of the flux-grown single crystal is presented in Figure 1a (only data for the first cycle are plotted). For comparison, resistivity for a polycrystalline sample from ref 15 is shown in Figure 1b. Both samples show an increase in resistance with temperature, which is characteristic of both metallic phases and heavily doped (extrinsic) semiconductors.

A generalized look at the resistivity/resistance versus temperature ($R$ vs $T$) plots for both the single and the polycrystalline samples gives an impression of only one $\lambda$-shaped transition, but a closer analysis, outlined below, and crystallographic data, given later, clearly indicate two separate transitions. As for the polycrystalline sample, the high-temperature transition for the single crystal at 244 K ($T_i = 254$ K for the polycrystalline sample) exhibits no observed hysteresis and may be second-order (continuous) in nature. The newly formed phase is stable in a rather narrow temperature interval

between 244 and 218 K (254 and 234 K for the polycrystalline sample), below which it transforms into another polymorph, known as an R-form. The second transition bears two features of a first-order phase transition: (1) the presence of hysteresis upon heating and cooling and (2) a sudden change in the slope of $R$ versus $T$.

For the flux-grown crystal, the change in slope of $F$ versus $T$ for the low-temperature transition is not as sharp as for the polycrystalline Zn$_4$Sb$_3$ sample, because of a steplike feature around the transition temperature, which is present during both heating and cooling. The nature of this feature is not clear at the moment, although it may indicate an additional structural perturbation.

The residual resistance ratio, $F(300 K)/F(5 K) \approx 2.6$, for the flux-grown crystal is much lower than that for the polycrystalline sample ($\approx 11$), which is probably due to the slight Bi doping in the flux-grown crystal and the possible presence of Zn on the grain boundaries of the polycrystalline sample. The transition temperatures are noticeably lower for the single crystal, which most likely results from a small amount of Bi doping, in support of an earlier observation that the transition temperature is dependent on the preparation method. Cycling through the transformation region increases the resistivity of the crystal, which can be associated with the formation of microcracks in the crystal as it is heated and cooled through its crystallographic phase transitions.

**Seebeck Coefficient Measurements.** A flux-grown single crystal was cut to obtain two parallel opposite faces with a distance of 2.5 mm between them. The Seebeck coefficient was determined by placing the crystal between two spring-loaded Ta wound BN heaters. A Mo core in each heater transferred heat to each end of the crystal. The heaters served both to heat the sample to the target temperature and to generate a temperature gradient across the sample. A 0.35 mm Mo plate was positioned between the crystal end and the Mo heater core. Pt−Pt13%Rh thermocouples were welded to each plate to form an extrinsic thermocouple. The Pt leg of each thermocouple serves as a voltage lead to measure the voltage difference $\Delta V$ generated across the sample as the thermal gradient $\Delta T$ is imposed. A linear least-squares fit is then applied to the measured $\Delta V/\Delta T$ to obtain the Seebeck coefficient. The average temperature between the top and bottom thermocouples is the reported measurement temperature. The sample was measured from 300 to 673 K under vacuum, and the results are shown in Figure 2.

The room-temperature Seebeck coefficient of 75 µV/K for the flux-grown single crystal is lower than the value of 113 µV/K reported by Caillat et al. for hot-pressed samples. This value is also lower than ≈135 µV/K for the sample prepared by the gradient-freeze method but comparable to ≈70 µV/K for the sintered polycrystalline sample as reported by Souma et al. (the Seebeck coefficient values are taken from the plot). This comparison clearly indicates that the Seebeck coefficient is strongly dependent on the preparation technique.

The temperature dependence of the Seebeck coefficient (Figure 2) reveals instability of the crystal during heating in a vacuum. On the basis of the high-temperature XRD powder data (Figure 3), the decrease in thermopower above 500 K can be associated with Zn sublimation and development of the zinc-poorer, ZnSb, phase ($\text{ZnSb}(s) \rightarrow \text{Zn}(g)$). Subsequent increase in thermopower after 600 K can be linked to further Zn losses and appearance of elemental antimony ($\text{ZnSb}(s) \rightarrow \text{Sb}(s) + \text{Zn}(g)$).

**X-ray Analysis.** Room-Temperature, Single-Crystal XRD. The diffraction data for two single crystals, one extracted from the polycrystalline Zn$_4$Sb$_3$ sample and the other Bi-flux-grown, were
Table 1. Crystal Data and Structure Refinements of the Single Crystal from the Polycrystalline Sample at 293 K

<table>
<thead>
<tr>
<th>composition</th>
<th>full Zn occupancy</th>
<th>deficient Zn</th>
<th>deficient Zn + extra Zn</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zn12Sb10</td>
<td>Zn10(7.5)Sb10</td>
<td>Zn11.82Sb50</td>
<td></td>
</tr>
<tr>
<td>data/parameters</td>
<td>438/19</td>
<td>438/20</td>
<td>438/35</td>
</tr>
<tr>
<td>goodness of fit on F²</td>
<td>1.185</td>
<td>1.094</td>
<td>1.122</td>
</tr>
</tbody>
</table>

R indices

<table>
<thead>
<tr>
<th>R indices (h0l) &gt; 2</th>
<th>0.0343, wR₁ = 0.0945</th>
<th>0.0296, wR₂ = 0.0751</th>
</tr>
</thead>
</table>

R indices

<table>
<thead>
<tr>
<th>R indices (all data)</th>
<th>0.0355, wR₁ = 0.0952</th>
<th>0.0238, wR₂ = 0.0547</th>
</tr>
</thead>
</table>

Extinction coefficient

<table>
<thead>
<tr>
<th>0.000 29(7)</th>
<th>0.000 27(5)</th>
<th>0.000 36(5)</th>
</tr>
</thead>
</table>

Peak/hole, eÅ²

<table>
<thead>
<tr>
<th>2.517/1.492</th>
<th>2.296/0.998</th>
<th>1.286 and –0.897</th>
</tr>
</thead>
</table>

Zn occupancy

<table>
<thead>
<tr>
<th>Zn = 1.00</th>
<th>Zn = 0.896(4)</th>
<th>Zn = 0.907(5)</th>
</tr>
</thead>
</table>

Table 2. Crystal Data and Structure Refinements of the Single Crystal from the Polycrystalline Sample at 238 K

<table>
<thead>
<tr>
<th>composition</th>
<th>Zn12Sb10</th>
</tr>
</thead>
<tbody>
<tr>
<td>space group</td>
<td>C2/c</td>
</tr>
<tr>
<td>lattice parameters, Å</td>
<td>a = 10.878(2)</td>
</tr>
<tr>
<td></td>
<td>b = 12.225(2), β = 100.044(2)</td>
</tr>
<tr>
<td></td>
<td>c = 8.185(1)</td>
</tr>
<tr>
<td>volume, Å³</td>
<td>1071.8(3)</td>
</tr>
<tr>
<td>Z</td>
<td>2</td>
</tr>
<tr>
<td>diffractometer</td>
<td>SMART 1000</td>
</tr>
<tr>
<td>2θ range</td>
<td>5.06–56.64°</td>
</tr>
<tr>
<td>index ranges</td>
<td>–13 ≤ h ≤ 14, –16 ≤ k ≤ 16, –10 ≤ l ≤ 10</td>
</tr>
<tr>
<td>independent reflections</td>
<td>1343 (Rₛ = 0.0330)</td>
</tr>
<tr>
<td>completeness to 2θₛ</td>
<td>95.7%</td>
</tr>
<tr>
<td>data/parameters</td>
<td>1343/70</td>
</tr>
<tr>
<td>goodness of fit on F²</td>
<td>1.055</td>
</tr>
<tr>
<td>final R indices [Fo/</td>
<td>R₁ = 0.0260, wR₂ = 0.0621</td>
</tr>
<tr>
<td>l] &gt; 2</td>
<td>R₂ = 0.0334, wR₃ = 0.0662</td>
</tr>
<tr>
<td>extinction coefficient</td>
<td>0.000767(7)</td>
</tr>
<tr>
<td>largest diff. peak/hole, eÅ³</td>
<td>1.360/–1.113</td>
</tr>
</tbody>
</table>

Table 3. Atomic and Equivalent Isotropic Displacement Parameters* for the Single Crystal from the ZnSb50 Polycrystalline Sample

<table>
<thead>
<tr>
<th>atom</th>
<th>occup.</th>
<th>x/a</th>
<th>y/b</th>
<th>z/c</th>
<th>Ueq Å²</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zn</td>
<td>36f</td>
<td>0.907(5)</td>
<td>0.2441(8)</td>
<td>0.0972(6)</td>
<td>0.09657(7)</td>
</tr>
<tr>
<td>Zn₁</td>
<td>36f</td>
<td>0.025(4)</td>
<td>0.074(3)</td>
<td>0.250(3)</td>
<td>0.095(2)</td>
</tr>
<tr>
<td>Zn₂</td>
<td>36f</td>
<td>0.032(6)</td>
<td>0.202(3)</td>
<td>0.094(3)</td>
<td>0.025(2)</td>
</tr>
<tr>
<td>Zn₃</td>
<td>36f</td>
<td>0.022(5)</td>
<td>0.236(3)</td>
<td>0.130(4)</td>
<td>0.234(3)</td>
</tr>
<tr>
<td>Sh₁</td>
<td>18e</td>
<td>1.35588(4)</td>
<td>0.14(1)</td>
<td>0.167(2)</td>
<td></td>
</tr>
<tr>
<td>Sh₂</td>
<td>12c</td>
<td>0.0</td>
<td>0.0</td>
<td>0.1364(1)</td>
<td>0.0162(2)</td>
</tr>
</tbody>
</table>

* Anisotropic temperature factors and other crystallographic details can be obtained in Supporting Information.

collected on a Bruker Apex CCD diffractometer in a full reciprocal frame and with 2θₛ = 70°, data completeness to 2θₛ = 96.3%.

Structures of both crystals were solved and refined in the R₃c space group. Because of Zn deficiencies and a small amount of Bi doping, the Bi concentration in the flux-grown crystal could not be reliably refined. The atomic coordinates and occupancies of the flux-grown crystal are analogous within three standard deviations to those of the crystal extracted from the polycrystalline sample.

The quality of the flux-grown crystal appears to be lower than that of the crystal extracted from the polycrystalline sample as judged by the R indices residual values (0.0461 vs 0.0260). Therefore, only data for the latter are discussed hereafter. In agreement with earlier results, significant deficiencies (~10%) were found for the “main” Zn atoms, site 36f. A difference Fourier map revealed pockets of small electron density around the main Zn site, among which three peaks stood out as possible Zn positions. In line with the single-crystal and MEM powder structural data, three interstitial Zn sites were introduced into the structure. The refined coordinates of the additional Zn sites are similar to those reported by Snyder et al. Improvements in the residual values and electron density difference map are outlined in Table 1. The Hamilton test indicated that every consecutive structural model (deficient Zn site and then three extra Zn sites) can be accepted with larger than 0.995 probability. The refinement of the additional Zn positions was done isotopically (anisotropic refinement produced physically unreasonable thermal ellipsoids), and the final crystallographic and atomic parameters standardized through the program TIDY are summarized in Tables 1 and 3. While introducing extra Zn atoms into the structure raised the Zn concentration (Table 1), the refined room-temperature composition Zn₁₁.₈₂Sb₅₀ still differs much from the room-temperature Zn₁₂Sb₅₀ and low-temperature Zn₁₃Sb₈₀ compositions reported by Snyder et al. 1 or by Nylen et al. 3, respectively. A lower Zn concentration in Zn₁₁.₈₂Sb₅₀ may be due to both intrinsic factors (lower Zn concentration in the crystal, distribution of Zn atoms on.

temperature, three parameters, $U$, $V$, and $W$, describing the peak full width at half-maximum ($W = [U \tan^2 \theta + V \tan \theta + W]^2$) as a function of the angle $\theta$ were refined. The variables $V$ and $W$ were then fixed, and only the $U$ parameter was refined at lower temperatures. (In general, the $V$ parameter is negative, $U$ and $W$ are positive, and $U \gg W$. Thus, the biggest positive contribution and the principal angle-dependent broadening of the peaks are associated with the $U$ parameter.) As seen from Figure 5, the value of $U$ nearly doubles upon cooling from 294 to 220 K, which is indicative of symmetry reduction, and then, as expected, it decreases with temperature. A plateau in $U$ at 245 and 240 K separates two sharp increases in the peak width at 250 and 235 K, which can be associated with two consecutive phase transitions observed from the physical property measurements. While it is difficult to evaluate exact transition temperatures because of small temperature resolution and stability during the X-ray powder studies, the transition temperatures of $\sim$250 and $\sim$235 K match well the values obtained by other techniques.

Low-Temperature, Single-Crystal XRD. The low-temperature data for the crystal extracted from the polycrystalline Zn$_3$Sb$_3$ sample were taken on a Bruker SMART 1000 CCD diffractometer at 243-(1), 238(1), 233(1), 228(1), and 203(1) K. Diffraction data were collected and processed the same way as the room-temperature ones. Indexing of the reflections at 243 and 238 K, below the first $\beta$-to-intermediate phase transition temperature, in the rhombohedral setting with unconstrained lattice parameters and angles (i.e., a triclinic approximation) did not indicate significant deviation of the lattice parameters and angles from the rhombohedral ones ($a = b = c$ and $\alpha = \beta = \gamma$); for example, $a = 8.189(1)$ Å, $b = 8.190(1)$ Å, $c = 8.191(1)$ Å, $\alpha = 96.641(2)^\circ$, $\beta = 96.681(2)^\circ$, and $\gamma = 96.649(2)^\circ$ from 989 reflections at 238 K. However, according to the physical property measurements there is a significant structural perturbation on cooling to 238 K. In addition, the low-temperature powder diffraction indicates symmetry reduction in this temperature region. The translationsungleiche, lower-symmetry subgroups of the $R3c$ space group are the monoclinic space groups $R12c$ ($C2/c$), $R12$ ($C2$), and $R11c$ ($Cc$) and the triclinic space groups $R11$ ($C1$ or $P1$) and $R11$ ($C1$ or $P1$). Because the symmetry reduction proceeds further upon cooling (it is a two-step process according to Figure 5; the resistance measurements (Figure 1) also indicate two consecutive phase transitions), the lattice symmetry at 238 K is likely to be monoclinic and the symmetry at lower temperatures is likely to be triclinic. Analysis of the extinction conditions at 238 K indicated presence of a $c$ glide plane and thus supported formation of the monoclinic lattice upon the first phase transition. Among the two monoclinic space groups $C2/c$ and $Cc$, $C2/c$ was chosen as the correct one because it led to a stable structural refinement with fewer refined parameters and a smaller number of correlation factors. Besides, the $R3c \rightarrow C2/c$ symmetry reduction satisfies the Landau conditions for a second-order phase transition (see below) and, thus, can account for the absence of the hysteresis during the first low-temperature phase transition. Also, only a further symmetry reduction of the $C2/c$ space group and not of the $Cc$ one can yield the $C1$ space group, as reported by Nylen et al.\textsuperscript{1}

The $R3c \rightarrow C2/c$ symmetry breaking can proceed along three equivalent pathways (due to the equivalence of the twofold axis and the $c$ glide planes as discussed below), and because the monoclinic distortion of the rhombohedral cell is very small, the resulting twinning is merohedral according to the single-crystal XRD techniques used. Because of the merohedral nature of twinning, the monoclinic lattice parameters obtained from the least-squares refinement will resemble those derived using the rhombohedral unit cell. The following axial transformation between the rhombohedral and monoclinic settings was used to generate a reference $C$-centered monoclinic cell with $a = 10.888(2)$ Å, $b = 12.237(2)$ Å, $c = 8.190(1)$ Å, and $\beta = 100.025(2)^\circ$:

$$
\begin{pmatrix}
a_{\text{mon}} \\
b_{\text{mon}} \\
c_{\text{mon}}
\end{pmatrix} = \begin{pmatrix}
1 & 0 & 1 \\
1 & 0 & -1 \\
0 & 1 & 0
\end{pmatrix}
\begin{pmatrix}
a \\
b \\
c
\end{pmatrix}
$$

During structural refinement the crystal was treated as a twin with three components. This refinement produced a smoother difference electron density map, on which only three sites stood out as possible Zn positions. The refinement with three additional,
Analysis of the Phase Transitions of Zn_{13}Sb_{10}

partially occupied Zn sites yielded a Zn_{12}Sb_{10} composition, which is within one standard deviation from the room-temperature one. The final crystallographic and atomic parameters for the crystal at 238 K are standardized through the program TIDY\textsuperscript{21} and are summarized in Tables 2 and 3.

At 233 K, near the second transition temperature, the diffraction spots could be indexed to the above-mentioned monoclinic cell. Cooling to 228 K, below the second transition temperature, led to the formation of the C-centered supercell with \( a = 32.637(5) \) Å, \( b = 12.246(2) \) Å, \( c = 10.876(1) \) Å, \( \alpha = 90^\circ \), \( \beta = 90.100(4) \), and \( \gamma = 90^\circ \), which was reported before.\textsuperscript{3,15} As indicated by Nylen et al.\textsuperscript{3} for 150 K, this cell has triclinic symmetry (C1) but is metrically monoclinic. We could not perform a satisfactory structure solution and refinement of the 228 K data because of the small number of superstructure reflections observed. Further cooling to 203 K produced extra diffraction spots that could not be fitted to the cell observed at 228 K (Figure 6). Although some of the partial indices may have indicated tripling of the \( c \) parameter (e.g., see the two spots with the \( hkl \) values of \(-3 3 3.30\) and \(-3 3 3.62\) in Figure 6), the separation between them and the main diffraction spots was not regular (e.g., see the \(-3 3 3.425\) reflection in Figure 6), which is a sign of an incommensurately modulated \( c \) parameter. In addition, there were diffraction spots that clearly expressed the incommensurate nature of the unit cell in the two other directions, \( a \) and \( b \). Attempts were made to establish an approximate structure of this low-temperature (203 K) form using only reflections from the C-centered supercell by utilizing the structural model of Nylen et al.\textsuperscript{3} and introducing twin laws. However, the refinement was not successful: the difference electron density map was very rough with a number of large electron density peaks closely spaced to the existing Zn atoms. Indeed, this was an expected outcome because the additional reflections were of significant intensity, which indicated a large structural modulation.

High-Temperature, Single-Crystal XRD. High-temperature XRD was done on a Bruker SMART Apex CCD diffractometer with Mo K\( \alpha \) radiation, equipped with a Nonius crystal heater.\textsuperscript{22} To minimize oxygen and nitrogen contamination, no glue or cement was used for mounting the crystal, which was extracted from the polycrystalline sample. The crystal was put at the bottom of the 0.2 mm capillary and fixed in place by another thinner capillary (Hampton research #50 glass capillaries), and then the outer capillary was sealed off with argon inside.\textsuperscript{23} Sixty frames were recorded at 293, 473, 573, 673, and 773 K to identify phases and determine unit cell parameters. The \( a \) and \( c \) parameters, as well as the \( a/c \) ratio, increase with temperature (Figure 7). Heating to 773 K, above the \( \beta \rightarrow \gamma \) transition temperature of 767 K, produced a diffraction pattern similar to that of a crystal with many components. Attempts to derive unit cell symmetry and dimensions were unsuccessful. However, when the crystal was cooled to 753 K, 15 min after the temperature was raised to 773 K, the Bragg peaks could be indexed to multiple ZnSb components. Visual inspection of the capillary indicated that its inner walls were covered with a thin black deposit, which is mostly likely to be zinc lost by the crystal (Zn_{13}Sb_{10} \rightarrow 10ZnSb + 3Zn). Thus, these studies agree with X-ray powder diffraction results on the bulk polycrystalline sample, which showed decomposition of Zn_{13}Sb_{10} at high temperatures (Figure 4).

Electronic Structure Calculations. To understand the relationship between the structure, composition, and physical properties of Zn_{13}Sb_{10}, tight-binding linear-muffin-tin-orbital calculations using the atomic sphere approximation (TB-LMTO-ASA)\textsuperscript{24} were carried out for the Zn_{12}Sb_{10} motif of the room-temperature structures of Zn_{13}Sb_{10}. The main Zn sites were assumed to be fully occupied, and the interstitial Zn atoms were neglected. To satisfy the overlap criteria of the atomic spheres in the TB-LMTO-ASA method, empty spheres were included into the unit cell. For the Zn_{12}Sb_{10} composition (74 electrons/formula), the Fermi level is located in the upper part of the valence band. Assuming the rigid band model, the valence band is filled at 76 electrons/formula, which corresponds to the Zn_{13}Sb_{10} composition (see Figure 11).

Results and Discussion

A thorough structural study of the phase transitions in Zn_{13}Sb_{10} below ambient temperature is complicated by the presence of disorder associated with certain Zn sites as well as the relatively narrow temperature range for existence of one of the phases. Characterization by diffraction as well as physical property measurements are critical to establish a sound picture of how these samples behave. However, as we have seen, flux-grown crystals and polycrystalline samples exhibit characteristics optimal for one characterization method and not for another. Our results indicate the existence of an intermediate phase between the low-temperature \( \alpha \)-form and the ambient-temperature \( \beta \)-form in the temperature range of about 234—254 K.

Symmetry-Breaking Transitions and Landau Theory. The possibility of a phase transition being second-order in nature can be examined using Landau theory.\textsuperscript{25,26} This theory gives symmetry constraints for symmetry-breaking transi-
tions; that is, it answers the question whether a transition between the high- and low-symmetry structures can occur as a continuous (second-order) one. The theory can also provide a structural model for one of the phases during the continuous symmetry-breaking process.\(^{27}\) Application of Landau theory to structural transitions involves several steps: (1) determination of a wavevector \( \mathbf{k} \) corresponding to the distortion; (2) determination of irreducible representations of \( \mathbf{k} \) vector; (3) analysis of irreducible representations for absence of a third-order invariant in the expansion of the Gibbs free energy in the order parameter; (4) finding minima in the Gibbs free energy with respect to the basis functions of the relevant irreducible representations; (5) determination of space groups from the invariance of the Gibbs free energy under the symmetry operations; and (6) verification that a minimum in the Gibbs free energy as a function of the \( \mathbf{k} \) vector is fixed by symmetry in the reciprocal space.

\( R3c \to C2/c \) Symmetry Reduction \((T = 254 \text{ K})\). Because no superstructure is created during the phase transition at 254 K (the primitive cells of the rhombohedral and monoclinic lattices are similar), the wavevector of the distortion is \( \mathbf{k} = 0 \) and irreducible representations of \( \mathbf{k} \) are isomorphous with those of the \( D_{3d} \) point group of the \( R3c \) space group. There are five irreducible representations breaking the symmetry: three one-dimensional and two two-dimensional.

The one-dimensional representations yield space groups containing a threefold axis and are not of interest because they are not consistent with our observations. The two-dimensional irreducible representations, \( E_g \) and \( E_u \), do not produce any third-order invariants in the expansion of the Gibbs free energy in the order parameter and, thus, can correspond to a continuous, symmetry-breaking transition within the Landau framework. Minimization of the Gibbs free energy with respect to the basis functions gives two identical solutions for the \( E_g \) and \( E_u \) representations. The resulting particle density, \( \rho \), can be expressed as a sum of that of the symmetrical form, \( \rho^o \), and the two basis functions:

Solution 1 \((E_g \) and \( E_u)\):

\[
\rho = \rho^o \pm \frac{1}{\sqrt{2}} \eta(q_1 \mp q_2)
\]

Solution 2 \((E_g \) and \( E_u)\):

\[
\rho = \rho^o \pm \frac{1}{\sqrt{2}} \eta(q_1 \mp q_2)
\]

The symmetry elements remaining upon symmetry breaking and, thus, the resulting space groups follow from the invariance of the particle densities under the operations of the \( R3c \) space group. Only for solution 1 of the \( E_g \) irreducible representation (Table 4) does the particle density remain identical under the \( (C_{2x+y+z}|c'y_2/2) \), \( (i|0) \), and \( (a|0) \) operations of the \( R3c \) space group (\( c_y \) is a translation along the \( c \) axis in the hexagonal setting, and \( c_y = a \pm b + c \)). The standard monoclinic setting (the \( C2 \) axis parallel to \( b_m \)) can be achieved through the following transformations:

\[
\begin{pmatrix}
a_m \\
b_m \\
c_m
\end{pmatrix}
= \begin{pmatrix}
a_r \\
b_r \\
c_r
\end{pmatrix} \begin{pmatrix}
1 & 0 & 1 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{pmatrix}
\]

The monoclinic cell is \( C \)-centered as a result of the presence of the \( l/2 \) \((a_m + b_m) = a \) translation. In the new cell, the \( (C_{2x+y+z}|c'y_2/2) \) operation becomes \( (C_{2}|(a_m + b_m)/2) \), and \( (a|0) \) transforms into \( (a_r|b_m + c_m/2) \) under the \( C \)-centering translation. Combination of these two symmetry operations constitutes the \( C2/c \) space group. Finally, an origin shift by \((a_m + b_m)/4\) puts all symmetry elements into a standard setting, with the inversion center at the origin. Presence of the inversion center locks the minimum of the Gibbs free energy at \( \mathbf{k} = 0 \), which excludes further structural modulation around \( \mathbf{k} = 0 \) and, thus, proves that the \( R3c \to C2/c \) symmetry reduction can be continuous (second-order) in nature. Equivalence of the three two-fold axes in the \( R3c \) space group implies three \( R3c \to C2/c \) distortion pathways (Figure 8) and, thus, the possibility of twinning. Twin laws for two components with respect to a component chosen as a “reference” are

\[
\begin{pmatrix}
1/2 & 1/2 & 1 \\
-1/2 & -1/2 & 1 \\
1/2 & -1/2 & 0
\end{pmatrix}
\]

(twin component 2).

\[
\begin{pmatrix}
1/2 & -1/2 & 1 \\
1/2 & -1/2 & 1 \\
1/2 & 1/2 & 0
\end{pmatrix}
\]

(twin component 3).

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The minimum in the Gibbs free energy during the $C2/c \rightarrow C1$ symmetry reduction is not fixed by symmetry at $k = 1/4c_{cm}$, and, thus, this transition can follow an incommensurate pathway, because a small variation in $k$ will produce a new minimum in $G$:

$$G(k + \delta k) = G(k) + \alpha \delta k + ...$$

Thus, this transition will be first-order in nature.

Development of reflections with fractional indices below the transition temperature during our experiments indicates that the low-temperature transition is likely to follow the $C2/c \rightarrow C1$ symmetry reduction accompanied by incommensurate modulation. Thus, this transition is first-order according to Landau theory. Some future experiments will be performed to establish the symmetry of this incommensurate structure and test our theoretical conclusions. On the other hand, the $C2/c \rightarrow C1$ distortion observed by Nylen et al. is confined to $k = 1/4c_{cm}$ because the minimum in $G$ is fixed by the inversion center. Although all Landau conditions are met and this symmetry breaking can be continuous, there is also a possibility that the $C2/c \rightarrow C1$ transition is first-order in nature.

An unusual aspect of this low-temperature transition is the possibility of a structural distortion along two distinct routes: commensurate $C2/c \rightarrow C1$ or incommensurate $C2/c \rightarrow C1$. The extension of the Gibbs free energy in the order parameter does not answer which distortion is thermodynamically preferred. However, from the Gibbs free energy/entropy relationship, it can be stated that the structure with higher entropy, that is, the $C1$ one, is more stable than the $C1$ structure especially at higher temperatures, provided the enthalpy change is equal along the two distortion pathways. If, however, there is a larger enthalpy gain (e.g., in electronic energy) during the $C2/c \rightarrow C1$ symmetry reduction, the distortion will follow this path. The preference for $C1$ or $C1$ symmetry may be influenced by the Zn/Sb ratio or presence of impurities. It is also likely that because of slight crystal inhomogeneities, different domains of the crystal may exhibit different symmetries.

**Structural Analysis.** The idealized $\text{Zn}_{12}\text{Sb}_{10}$ (or $\text{Zn}_{2}\text{Sb}_{3}$) atomic motif of the $\beta$-phase can be built from Sb atoms with Zn in tetrahedral voids. Although that structural approach accounts for the 6:5 Zn/Sb ratio, it does not provide a rationale for either the $\text{Zn}_{12}\text{Sb}_{10}$ composition or the interatomic interactions and is also inconvenient for analyzing ordering of Zn atoms during the symmetry breaking. Recently, Haußermann et al. showed that interconnected $\text{Zn}_{2}\text{Sb}(1)$ diamond units with multicenter bonding are essential in forming the idealized $\text{Zn}_{12}\text{Sb}_{10}$ framework. These diamond units also account for the observed $\text{Zn}_{12}\text{Sb}_{10}$ composition as the $\text{Zn}_{12}\text{Sb}_{10}$ framework requires two more.

References:


electrons (from an additional Zn atom) to satisfy all bonding interactions. In H"assermann’s approach, the additional Zn atoms of the room-temperature $\beta$-form were treated as simple electron donors to the $\text{Zn}_{11}\text{Sb}_{10}$ framework. To visualize major structural changes associated with the two phase transitions, we believe that a different structural representation, depicted in Figures 9 and 10 and similar to the one used by Nylen et al.,\textsuperscript{3} is more beneficial. An idealized $\text{Zn}_{12}\text{Sb}_{10}$ framework of the rhombohedral $\text{Zn}_{13}\text{Sb}_{10}$ $\beta$-phase consists of the Zn channels centered by Sb2 atoms and with Sb1 atoms located between the channels (Figure 9a). As seen from the side (Figure 10a), the Zn channels are formed from six-membered crownlike rings that stack along the $c$ axis and sandwich the Sb2–Sb2 dimers. In the room-temperature $\beta$-phase, additional Zn atoms (sites 1–3) are located along the channel walls (Figure 9b), and they can be found within and between the six-membered rings (Figure 10a). Some of the distances between the “main” and interstitial Zn atoms are quite short ($d_{\text{min}} = 1.09$ Å), but because XRD yields the average crystal structure, the Zn atoms are not all necessarily present in the same unit cell. The $\text{Zn}–\text{Sb}$ bonds are reasonable for both the main ($d_{\text{min}} = 2.69$ Å) and additional ($d_{\text{min}} = 2.55$ Å) Zn sites. The nearest neighbor interactions and possible ordering schemes are extensively discussed in ref 2.

The $R3\bar{c} \rightarrow C2/c$ transition leads to significant ordering of the interstitial Zn atoms, as reflected by a smaller number (Figure 10b) and correspondingly higher occupancy of the interstitial Zn sites (Table 3). This ordering can be visualized as a collapse of three interstitial Zn sites into one during the transition. Surprisingly, total occupancy of the resulting Zn sites surpasses the occupancy of the original Zn sites in the $R3\bar{c}$ structure. Similar, although somewhat less pronounced, is the increase in the total occupancy of the main Zn sites in the $C2/c$ structure. At present, there is no solid understanding of what causes this phenomenon. Most of the interatomic distances in the distorted $C2/c$ structure closely resemble those in the $R3\bar{c}$ structure. The largest change is observed for the shortest distance between the main and the interstitial Zn atoms: it increases from $d_{\text{min}} = 1.09$ Å to $d_{\text{min}} = 1.20$ Å.

The commensurate $C1$ structure of the low-temperature $\alpha$-polymorph (Figure 10c) is based on the data by Nylen et al.\textsuperscript{3} Here, the interstitial Zn atoms are located on two fully occupied sites, and the main Zn sites are also fully occupied. This yields a stoichiometric $\text{Zn}_{13}\text{Sb}_{10}$ formula. Ordering associated with the $C2/c \rightarrow C1$ symmetry reduction appears to be quite different from that of the $R3\bar{c} \rightarrow C2/c$ transition. During the $C2/c \rightarrow C1$ transition the interstitial Zn atoms go into the main Zn sites until these sites are completely filled, and then the remaining Zn atoms order on two individual sites, whereas the interstitial Zn atoms seem to order on fewer interstitial sites during the $R3\bar{c} \rightarrow C2/c$ transition. This distinct ordering behavior has its structural consequences. Because in the $R3\bar{c}$ and $C2/c$ phases both the main and the interstitial Zn sites within the crownlike rings are deficient, they can occupy geometrically the same space but in different unit cells. However, in the $C1$ polymorph all sites are fully occupied and the presence of interstitial Zn atoms within the crownlike rings introduces local structural perturbations, which distorts these rings (Figure 10c).

**Composition, Electronic Structure, and Electrical Conductivity.** The microprobe analysis yielded the $\text{Zn}_{6.5(1)}\text{Sb}_{3.2(2)}\text{Bi}_{0.35(2)}$ (or $\text{Zn}_{13.00(2)}\text{Sb}_{9.44(5)}\text{Bi}_{0.080(5)}$) composition for the flux-grown single crystals of the room-temperature $\beta$-phase. Assuming presence of Bi just on the Sb site, the formula of a Bi-free crystal can be written as $\text{Zn}_{13.0827}\text{Sb}_{10.0266}$, which is within one standard deviation from the stoichiometric $\text{Zn}_{13}\text{Sb}_{10}$ composition. The $\text{Zn}_{13}\text{Sb}_{10}$ composition was obtained by Nylen et al. from the low-temperature single-crystal refinement of the ordered $\alpha$-structure.\textsuperscript{3} Inaccuracies in the compositions $\text{Zn}_{11.82}\text{Sb}_{10}$ and $\text{Zn}_{12.03}\text{Sb}_{10}$ refined from our X-ray single-crystal data at 293 and 238 K are likely to stem from both extrinsic factors related to the XRD (absorption, extinction, etc.) and intrinsic factors associated with highly disordered structures (interstitial Zn atoms can be present on more than three sites with smaller occupancies).
When Zn–Zn interactions in Zn$_{13}$Sb$_{10}$ are neglected, the Zintl–Klemm formalism for valence compounds provides an accurate electron count. The Sb1 atoms in the R$3c$ structure (Sb1-2 atoms in the C2$\bar{c}$ structure) have no Sb neighbors and can be treated as Sb$^{3-}$. The Sb2 atoms in the R$3c$ structure (Sb3 atoms in the C2$\bar{c}$ structure) form dimers with $d_{\text{Sb-Sb}} = 2.82$ Å, which is characteristic of a Sb–Sb single bond, which is isoelectronic with a halogen dimer and carries a formal charge of $-2$. Six Sb$_1^{3-}$ and four Sb$_2^{2-}$ in Zn$_{13}$Sb$_{10}$ require 26 electrons that are provided by 13 Zn atoms. However, the presence of Zn–Zn bonds of 2.78 Å makes this phase electron deficient and, thus, metallic from the Zintl–Klemm closed shell approach. Recently, Haussermann et al. showed that this electron deficiency is overcome by the formation of interconnected structural units with distinctive bonding: rhombohedral rings made from two Zn and two Sb1 atoms. The four-center bonding within these rings is optimized with four electrons, that is, with less electrons which otherwise would be required if the constituent atoms of the rings were participating in two-center two-electron bonds.

The fact that Zn$_{13}$Sb$_{10}$ is indeed electron precise is recognized in the band structure (Figure 11). The band gap of $\sim$0.8 eV separates the valence and conduction bands. Assuming a rigid band model, the valence band is filled at 76 electrons/formula. The structural features, especially bonding characteristics of two different Sb atoms, are also recognizable in the density of states (DOS). The lower part ($-13$ to $-10.5$ eV) of the DOS contains five peaks. The two lower and two upper peaks are indicative of dimer formation within a linear atomic chain, and they are derived from the Sb2 5$s$ states with some Zn contribution. The larger, middle peak at $-11.5$ eV showing localized character typical of monomers comes from Sb1 5$s$ orbitals. Large DOS between $-10$ and $-9$ eV represent the localized Zn d orbitals that do not contribute much to either Zn–Sb or Zn–Zn bonding. The valence band ($-7.7$ to $-1.7$ eV) consists mostly of Sb 5$p$ and Zn 4$s$ orbitals and represents bonding states of the Zn–Sb, Zn–Zn, and Sb2–Sb2 interactions.

The ideal Zn$_{13}$Sb$_{10}$ composition implies full occupancy of the valence band and, thus, intrinsic semiconducting behavior. However, the resistance measurements for both polycrystalline and single-crystal samples (Figure 1) show metallic-type conductivity. This metallic-type behavior and a relatively large value of resistivity of the flux-grown crystal are characteristic of heavily doped semiconductors. In this material, this can occur from either Zn deficiencies ($p$-type doping) or excess of Sb atoms ($n$-type doping). From structural considerations, Zn deficiencies are more likely to be present in the structure and, thus, to dictate the nature of the electrical conductivity. This conclusion agrees with the results by Caillat et al., who established that the majority of the carriers in Zn$_4$Sb$_3$ are holes.

### Conclusions

XRD studies and resistance measurements on Zn$_n$Sb$_3$ indicated the presence of two low-temperature phase transitions, each being accompanied by a symmetry reduction. According to Landau theory, the first $R3c \rightarrow C2\bar{c}$ symmetry breaking may be second-order in nature. From theoretical considerations, the subsequent symmetry breaking can proceed along two routes: commensurate $C2\bar{c} \rightarrow C1$ or incommensurate $C2\bar{c} \rightarrow C1$. Our experimental results indicate a first-order nature and incommensurate pathway for this transition, both of which are consistent with the $C2\bar{c} \rightarrow C1$ symmetry reduction.

Quantitative microprobe analysis yielded only slight Bi doping of flux-grown crystals and proved that the composition of the Bi-free phase is better represented with the Zn$_{13}$Sb$_{10}$ formula. The Zn$_{13}$Sb$_{10}$ composition implies full occupancy of the valence band and semiconducting behavior of the resistance. However, the resistance measurements point to the presence of some empty states in the valence band. XRD studies and Seebeck coefficient measurements revealed instability of the Zn$_{13}$Sb$_{10}$ phase with respect to Zn losses at high temperatures in a vacuum.

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### Supporting Information Available: Crystallographic information (CIF). This material is available free of charge via the Internet at http://pubs.acs.org.